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NAVAL SURFACE WEAPONS CENTER DAHLGREN VA  
A METHOD TO CORRELATE THE UPPER AIR DENSITY WITH SURFACE DENSITY--ETC(U)  
JUL 82 L J MCANELLY

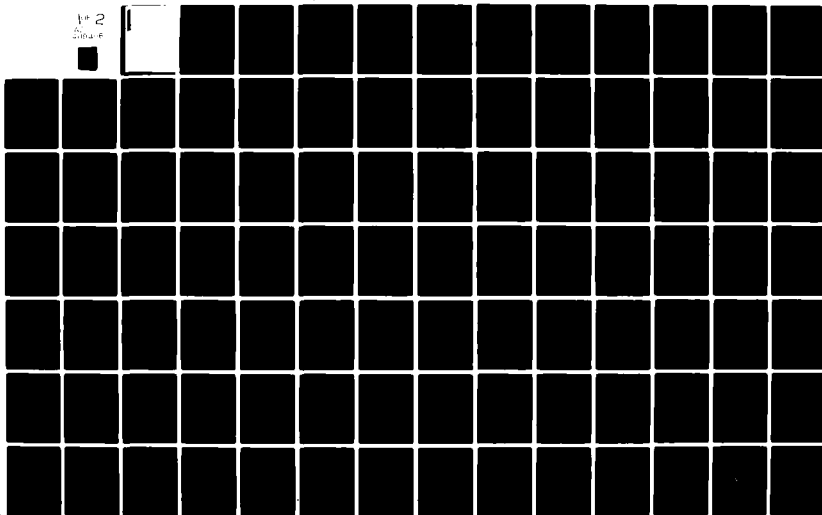
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20. ABSTRACT (Cont.)

Two exponential functions of altitude were used to express the density—one from surface to 36,000 ft, the other from 36,000 to 65,000 ft. The coefficients were selected in a manner that produces a continuous function from sea level to 65,000 ft. The coefficients of the two functions were determined using a non-linear least-squares technique.

Fluctuations in the density profiles below 5,000 ft altitude were noted and were investigated by fitting a sample of temperature and pressure data with a least-squares technique.

Ballistic densities for firing at surface targets were computed for altitudes to 50,000 ft. While the current projectiles in the Fleet may not reach an altitude of 50,000 ft, this may become a reality in the near future. The procedure presented in this report could very easily be modified to compute ballistic density when firing at air targets at altitudes up to 50,000 ft.

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FOREWORD

The range tables for Navy guns include a nomogram for computing ballistic density, which may be used when only the surface density is known. While these nomograms are intended for use when better estimates of ballistic density are not available, they are based on data prepared in 1922, despite the advent of radiosondes and the establishment of ocean weather stations.

Since there frequently are times when a radiosonde observation cannot be made in the immediate operating area just before firing, or a timely and applicable meteorological message from the Fleet Numerical Weather Center (FNWC) is not available, another method for obtaining ballistic densities would serve a useful purpose.

This report documents a study that shows that ballistic densities can be estimated from the surface density with a reasonable degree of accuracy. Data are also presented about the upper atmosphere which may be useful when further studies pertaining to the atmosphere are conducted.

The study was funded by the Naval Sea Systems Command Surface Weapons Aerodynamics and Structures Research and Development Block Program.

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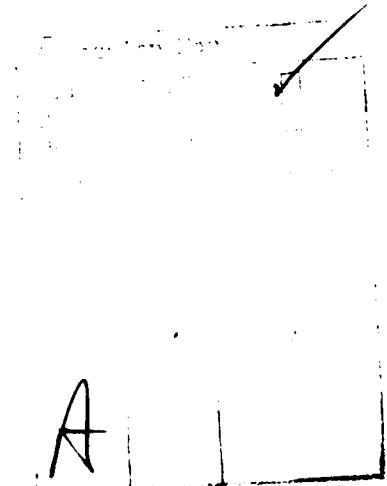
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The author would like to thank Dr. W. A. Kemper and Mr. Henry E. Castro for their help in preparing this report. Dr. Kemper provided valuable assistance in preparing the text of this report. Mr. Castro derived a nonlinear least-squares technique which was used to fit the observed density data. The technique is described in Appendix A.

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## INTRODUCTION

One of the basic premises of fire control systems in use in the Fleet today is a "Standard Atmosphere." Obviously, the same premise is also used in the preparation of ballistic tables for the Fleet. Since the conditions used as a basis for a standard atmosphere are rarely encountered on earth, corrections for nonstandard conditions are always in order. A procedure frequently used to correct for a nonstandard density involves a ballistic air density in the solution of fire control problems. The ballistic air density may be defined as a scale factor that, when multiplied by the standard air density at each altitude, produces a density structure that would cause the same displacement of a projectile impact point as the actual density structure.

The most reliable method of determining ballistic density is to use accurate, representative, and timely meteorological observations in the computation. There are, however, occasions when these measurements are not available, and alternate methods are necessary to provide the requisite information. It is a standard procedure to include a nomogram in the ballistic tables for the Fleet. The use of the nomogram is an alternative that is available to the Fleet for estimating the upper air density for naval gunfire when a ballistic meteorological forecast is not available. The nomograms may be used to estimate the ballistic density when the air temperature, pressure, and relative humidity at the surface are known.

The basic data used to prepare the nomograms were obtained from Table IV, The Ballistic Density Factor,<sup>1</sup> which was published in 1935. A footnote to this table states, "This table has been extracted from Table C of a pamphlet entitled Method for Determining Air Temperature and Ballistic Air Density, published by the Signal Corps (Meteorological Service), U.S. Army in 1922."

Fire control systems have been improved to the point where an accurate determination of the upper air density is required if the potential of the systems is to be fully utilized. The need for improving the nomograms or providing an alternate procedure to determine the ballistic density has long been recognized.

The work described in this report, stated briefly, consisted of (1) obtaining Rawinsonde data from various weather stations, (2) sorting the data according to



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surface densities and seasons, (3) fitting the upper air densities with a least-squares technique, and (4) computing ballistic densities.

Rawinsonde data used in the study were obtained from five maritime stations which took soundings daily at 0000 and 1200 hr G.m.t. over a period from 1968 to 1973. The data, consisting of both significant and mandatory levels, were provided by the National Climatic Center, Asheville, North Carolina. Mandatory levels are specified pressure altitudes, which are obtained by interpolation. Significant levels are the altitudes that are considered essential in defining a weather profile. Soundings that did not include surface density were not used in the study. Some of the obvious errors were eliminated in processing the data prior to performing the least-squares fit, but no attempt was made to eliminate errors in the basic data beyond that point.

The geodetic coordinates of the five stations used in the study are listed below:

<u>Station Name</u>	<u>Latitude</u>	<u>Longitude</u>
E	35° 0' N	48° 0' W
V	34° 0' N	164° 0' E
C	52° 45' N	35° 30' W
D	44° 0' N	41° 0' W
N	30° 0' N	140° 0' W

A map of the stations is shown in Figure 1.

No land-based stations were used in the analysis, even though naval gunfire support is conducted on beach areas. Since the density correlations are markedly affected by the nature of the terrain,<sup>2</sup> there is more than a probability that somewhat different results would be obtained for different littoral areas of the earth.

All computer programs used in the study were coded in FORTRAN EXTENDED and were executed with a Control Data Corporation (CDC) 6700 computer.

The purpose of performing the work described in this report was to establish a procedure to determine the correlation between upper air and surface densities and

LOCATION OF WEATHER STATIONS

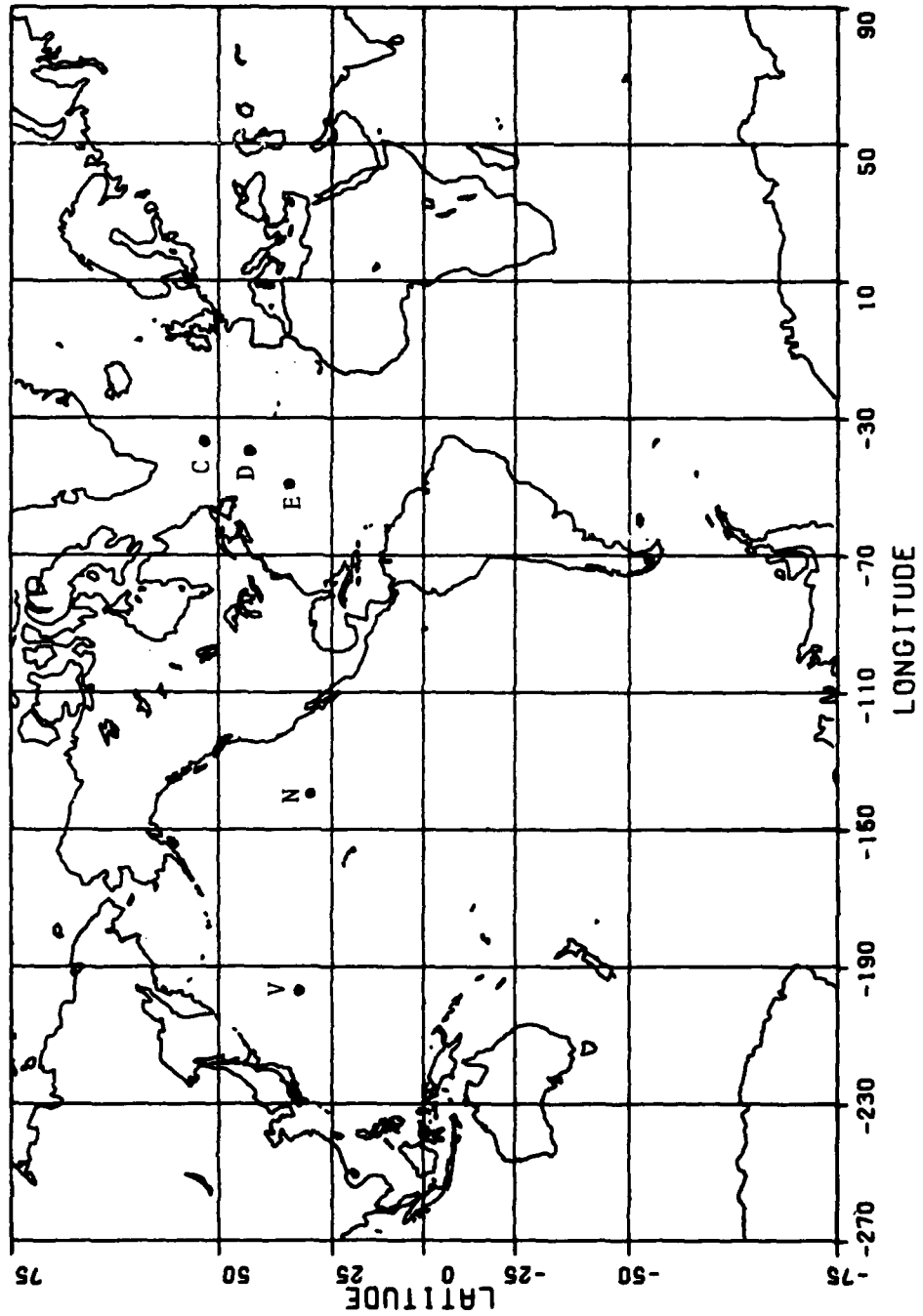


FIGURE 1. MAP OF STATIONS USED IN THE STUDY

to devise a method for estimating the ballistic air density based on surface conditions.

#### DETAILED PROCEDURE

The first step in the procedure was to compute the air density using the temperature, pressure, and relative humidity. The geopotential altitudes were converted to geometric altitudes. Sondes that did not include surface conditions were omitted. The data for each station were sorted into two groups according to the time of day and stored in permanent files with the Indexed-Sequential File Organization. This procedure permits accessing the data in either a sequential or random order. The sondes were assigned indices which were stored in separate sequential files. One file of indices was created with the corresponding surface densities in ascending numerical order, and a second file was created with the surface densities also sorted into the four seasons. A follow-up program was designed to skip specified segments when the files were read. This made it convenient to group the data in various ways without rearranging the Indexed-Sequential files.

The data were then selected in groups where the median surface density of each group varied by a percentage point from the U.S. Standard surface density as defined in Reference 3 (i.e., into classes by surface density ratios where the class interval was one percent). Since large variations were encountered in the frequency of the surface densities, it was necessary to eliminate some of the sondes in the mid-ranges. Several fits were made using various numbers of samples in each fit. No significant differences were obtained by using more than 25 samples; consequently, a further restriction was placed on each group that limited the number of sondes to 25. While some of the groups outside the mid-ranges had variations in surface densities of one percent, the actual number of samples was, in some cases, less than 25. In contrast, some of the groups of 25 samples in the mid-ranges had variations in surface densities of only a fraction of one percent.

Various functions were investigated to represent a mean density profile for each group of data. Comparisons were made of three different functions for representing the density in the altitude range from 0 to 36,089 ft:

1. a third-degree polynomial
2. a third-degree polynomial for the ratio of the observed density to the U.S. Standard density
3. an exponential function plus a linear term

While these three functions produced similar results, the exponential function was selected. The fitting technique is described in Appendix A. The following expression was used in the altitude range from 0 to 36,089 ft:

$$\rho = c_1 e^{(c_2 h)} + c_3 h \quad (1)$$

where,

$\rho$  is the density (lb/ft<sup>3</sup>)

$h$  is the altitude (ft)

$c_1$ ,  $c_2$ , and  $c_3$  are constants determined by the fit

A similar expression was used to fit the data in the region from 36,089- to 65,000-ft altitude:

$$\rho = \rho_{36089} e^{(c_4 * (h - 36089))} + c_5 * (h - 36089) \quad (2)$$

where,

$\rho_{36089}$  is the density at 36,089 ft, computed using equation (1) and the data up to 36,089 ft

$c_4$  and  $c_5$  are coefficients determined in the fit above 36,089 ft

A bias was noted in the lower altitudes with each of the three methods. After some experimenting, data below 3,500 ft were excluded from the fit to determine the coefficients. The fit was then extrapolated to mean sea level, and a linear correction was added from 0 to 3,500 ft, which made  $\rho$  equal to  $\rho_0$  at the surface:

$$\rho = c_1 e^{(c_2 h)} + c_3 h + (\rho_0 - c_1)(3500 - h)/3500 \quad (3)$$

where,

$\rho$  is the density (lb/ft<sup>3</sup>)

$c_1$ ,  $c_2$ , and  $c_3$  are the coefficients obtained with equation (1)

$h$  is the altitude (ft)

$\rho_0$  is the median of the observed surface densities (lb/ft<sup>3</sup>)

Although this procedure does not use any of the available data between surface and 3,500 ft in the least-squares fit to determine the coefficients  $c_1$ ,  $c_2$ , and  $c_3$ , residuals from the fit in this region are included in the analysis. Adding the linear correction made a significant improvement in the residuals from surface to 3,500 ft.

The upper boundary of 36,089 ft was selected from the zone where equation (1) was used in order to coincide with the breakpoint in the U.S. Standard atmosphere. While there are some seasonal, latitudinal, and diurnal variations in the isopycnic level where the density remains nearly constant, no attempt was made to explore this facet.

After fitting the observed density data, using equations (1) and (2), density profiles were computed using equations (2) and (3) with the coefficients obtained in the least-squares fit. Ballistic densities for each profile were computed with the equation,

$$\text{Ballistic Density} = \sum_{i=1}^n (WF_i * R_i) \quad (4)$$

where,

$n$  is the number of zones

$WF_i$  is the density weighting factor for the  $i$ th zone

$R_i$  is the ratio of the mean density of the  $i$ th zone of the profile to the U.S. Standard density at that altitude, which is the mid-point of the  $i$ th zone.

The density weighting factors used to compute the ballistic density were obtained by computing trajectories with ballistic parameters for the 5-Inch High Fragmentation Projectile fired with a Mk 73 charge, which produces an initial velocity of 2,950 ft/sec. The altitudes covered by each zone are presented in Table 1, and a tabulation of the weighting factors are presented in Table 2.

TABLE 1. ALTITUDE OF ZONES

<u>Zone</u>	<u>Altitude (ft)</u>	<u>Zone</u>	<u>Altitude (ft)</u>	<u>Zone</u>	<u>Altitude (ft)</u>
1	0 - 1,000	10	9,000 - 10,000	19	26,000 - 28,000
2	1,000 - 2,000	11	10,000 - 12,000	20	28,000 - 30,000
3	2,000 - 3,000	12	12,000 - 14,000	21	30,000 - 32,000
4	3,000 - 4,000	13	14,000 - 16,000	22	32,000 - 34,000
5	4,000 - 5,000	14	16,000 - 18,000	23	34,000 - 36,000
6	5,000 - 6,000	15	18,000 - 20,000	24	36,000 - 38,000
7	6,000 - 7,000	16	20,000 - 22,000	25	38,000 - 40,000
8	7,000 - 8,000	17	22,000 - 24,000	26	40,000 - 45,000
9	8,000 - 9,000	18	24,000 - 26,000	27	45,000 - 50,000

## FITTING A SAMPLE SET OF DATA WITH AN ALTERNATE PROCEDURE

An alternate method was used to fit a sample set of data in the region from surface to 36,000 ft. In this procedure, the virtual temperature was computed, using the observed temperature and relative humidity. Separate least-squares fits were then made to the virtual temperatures and pressures. The temperature and pressure profiles obtained in this manner were then used to compute the density. This procedure and the results are described in detail in Appendix B. The sample set of data was obtained from 25 sondes that had been selected previously for fitting with equation (1). The sondes were observed at Station E during the spring season, 1200 hr G.m.t., on days that had a surface density close to the U.S. Standard density at mean sea level.

TABLE 2. DENSITY WEIGHTING FACTORS

ZONES	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
1	1.000																										
2	0.375	0.625																									
3	0.231	0.265	0.485																								
4	0.192	0.194	0.210	0.404																							
5	0.156	0.157	0.159	0.176	0.349																						
6	0.136	0.135	0.134	0.136	0.151	0.307																					
7	0.122	0.119	0.118	0.117	0.119	0.133	0.272																				
8	0.111	0.108	0.105	0.104	0.104	0.106	0.117	0.244																			
9	0.102	0.099	0.097	0.095	0.095	0.095	0.095	0.106	0.220																		
10	0.095	0.092	0.090	0.087	0.086	0.085	0.084	0.087	0.086	0.200																	
11	0.084	0.081	0.079	0.077	0.075	0.073	0.072	0.071	0.070	0.072	0.247																
12	0.075	0.074	0.071	0.069	0.067	0.065	0.064	0.062	0.061	0.060	0.122	0.210															
13	0.069	0.067	0.065	0.063	0.062	0.060	0.058	0.056	0.055	0.053	0.105	0.106	0.180														
14	0.065	0.063	0.061	0.059	0.057	0.055	0.054	0.052	0.050	0.049	0.095	0.095	0.093	0.196													
15	0.061	0.059	0.057	0.055	0.053	0.052	0.050	0.049	0.047	0.046	0.088	0.085	0.081	0.082	0.135												
16	0.057	0.056	0.054	0.052	0.050	0.049	0.048	0.046	0.045	0.043	0.083	0.078	0.074	0.072	0.073	0.119											
17	0.055	0.053	0.051	0.050	0.048	0.047	0.045	0.044	0.042	0.041	0.079	0.074	0.070	0.067	0.064	0.065	0.104										
18	0.052	0.051	0.049	0.048	0.046	0.044	0.044	0.042	0.040	0.040	0.075	0.071	0.067	0.063	0.060	0.058	0.058	0.091									
19	0.050	0.049	0.047	0.045	0.044	0.043	0.041	0.040	0.039	0.038	0.072	0.068	0.065	0.061	0.059	0.055	0.053	0.052	0.079								
20	0.048	0.047	0.045	0.044	0.043	0.041	0.040	0.039	0.037	0.037	0.069	0.066	0.062	0.058	0.056	0.053	0.051	0.048	0.047	0.069							
21	0.047	0.045	0.044	0.042	0.041	0.040	0.039	0.038	0.036	0.035	0.067	0.063	0.060	0.056	0.053	0.050	0.049	0.047	0.045	0.043	0.060						
22	0.046	0.044	0.043	0.041	0.040	0.039	0.038	0.037	0.035	0.034	0.065	0.061	0.057	0.054	0.051	0.048	0.046	0.043	0.043	0.042	0.039	0.053					
23	0.045	0.044	0.042	0.041	0.039	0.038	0.037	0.036	0.034	0.033	0.064	0.060	0.055	0.053	0.049	0.046	0.043	0.042	0.040	0.038	0.036	0.046					
24	0.044	0.043	0.042	0.040	0.039	0.038	0.037	0.036	0.034	0.034	0.063	0.059	0.055	0.052	0.048	0.045	0.042	0.040	0.037	0.035	0.034	0.034	0.035				
25	0.043	0.042	0.041	0.040	0.038	0.037	0.036	0.034	0.034	0.032	0.062	0.058	0.054	0.050	0.047	0.044	0.041	0.039	0.036	0.034	0.033	0.031	0.032	0.031			
26	0.042	0.041	0.039	0.037	0.036	0.035	0.035	0.033	0.032	0.031	0.059	0.056	0.053	0.049	0.045	0.043	0.039	0.037	0.035	0.032	0.031	0.028	0.028	0.026	0.025	0.050	
27	0.041	0.040	0.039	0.037	0.036	0.035	0.034	0.033	0.032	0.030	0.059	0.055	0.051	0.047	0.044	0.042	0.038	0.037	0.034	0.032	0.029	0.027	0.025	0.024	0.023	0.049	0.027

The purpose of using the alternate method was to evaluate the method described in the section Procedure and to provide additional information about the atmosphere, particularly in the lower altitudes.

While this method is a good procedure for providing temperature, pressure, and density profiles, it is a more time-consuming method for obtaining density profiles than the method of making a least-squares fit to the densities.

The density profile obtained with this method did not result in a noticeably different profile, but it did provide additional information about the temperature and pressure. The pressure data from surface to 36,000-ft altitude were fit with a single function that has a continuous derivative. The temperature data were divided into three altitude zones. Separate least-squares fits were made to each zone in a manner that made the curve continuous but with a different lapse rate in each zone. The improvement in using the correction term in equation (3) to fit the density is largely due to the variations in the temperature lapse rate at the lower altitudes.

#### FITTING THE U.S. STANDARD ATMOSPHERE

In order to further test the least-squares method and the exponential representation of the density, a fit was made to the U.S. Standard density, using equations (1) and (2). Since the U.S. Standard temperature has a constant lapse rate from surface to 36,089-ft altitude, the correction term in equation (3) was not used. It should be noted that equations (1) and (2) were not intended to define the U.S. Standard density but were selected to fit the observed data. However, the standard deviations in the fit were only 0.14 and 0.28 percent in the zones from 0- to 36,089-ft, and 36,089- to 65,000-ft altitude, respectively. Since the density varies with altitude, the residuals were expressed as ratios of the U.S. Standard density at the corresponding altitude. A tabulation of the fit is presented in Tables 3 and 4.



TABLE 3. LEAST-SQUARES FIT OF U.S. STANDARD DENSITY  
0 - 36,000 ft

1 Altitude (ft)	2 U.S. Standard Density (lb/ft <sup>3</sup> )	3 L. S. Fit Density (lb/ft <sup>3</sup> )	4 Col. 2 - Col. 3 Col. 3
0.	0.076474	0.07665845	-0.00240610
500.	0.075362	0.07551388	-0.00201122
1,000.	0.074262	0.07438439	-0.00164533
1,500.	0.073174	0.07326977	-0.00130712
2,000.	0.072098	0.07216982	-0.00099517
2,500.	0.071035	0.07108433	-0.00069395
3,000.	0.069984	0.07001309	-0.00041553
3,500.	0.068945	0.06895591	-0.00015824
4,000.	0.067917	0.06791259	0.00006494
4,500.	0.066902	0.06688293	0.00028510
5,000.	0.065898	0.06586675	0.00047450
5,500.	0.064906	0.06486384	0.00064991
6,000.	0.063925	0.06387404	0.00079783
6,500.	0.062956	0.06289715	0.00093568
7,000.	0.061998	0.06193299	0.00104969
7,500.	0.061051	0.06098138	0.00114159
8,000.	0.060116	0.06004216	0.00122986
8,500.	0.059191	0.05911513	0.00128338
9,000.	0.058278	0.05820014	0.00133776
9,500.	0.057375	0.05729702	0.00136106
10,000.	0.056483	0.05640559	0.00137245
10,500.	0.055602	0.05552569	0.00137431
11,000.	0.054731	0.05465717	0.00135085
11,500.	0.053871	0.05379985	0.00132241
12,000.	0.053022	0.05295360	0.00129174
12,500.	0.052182	0.05211824	0.00122336
13,000.	0.051353	0.05129363	0.00115745
13,500.	0.050534	0.05047962	0.00107734
14,000.	0.049725	0.04967605	0.00098539
14,500.	0.048926	0.04888278	0.00088407
15,000.	0.048137	0.04809968	0.00077598
15,500.	0.047358	0.04732658	0.00066389
16,000.	0.046589	0.04656336	0.00055067
16,500.	0.045829	0.04580987	0.00041754
17,000.	0.045079	0.04506598	0.00028881
17,500.	0.044338	0.04433156	0.00014526
18,000.	0.043606	0.04360647	-0.00001072
18,500.	0.042884	0.04289057	-0.00015329

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TABLE 3. LEAST-SQUARES FIT OF U.S. STANDARD DENSITY  
0 - 36,000 ft (Continued)

1	2	3	4
Altitude	U.S. Standard	L. S. Fit	Col. 2 - Col. 3
(ft)	Density	Density	Col. 3
(ft)	(lb/ft <sup>3</sup> )	(lb/ft <sup>3</sup> )	
19,000.	0.042171	0.04218375	-0.00030232
19,500.	0.041468	0.04148588	-0.00043087
20,000.	0.040773	0.04079682	-0.00058376
20,500.	0.040087	0.04011645	-0.00073413
21,000.	0.039410	0.03944466	-0.00087867
21,500.	0.038742	0.03878132	-0.00101387
22,000.	0.038083	0.03812631	-0.00113606
22,500.	0.037432	0.03747953	-0.00126803
23,000.	0.036790	0.03684084	-0.00137995
23,500.	0.036156	0.03621014	-0.00149516
24,000.	0.035531	0.03558732	-0.00158251
24,500.	0.034914	0.03497226	-0.00166590
25,000.	0.034306	0.03436486	-0.00171279
25,500.	0.033705	0.03376501	-0.00177724
26,000.	0.033113	0.03317260	-0.00179668
26,500.	0.032529	0.03258753	-0.00179614
27,000.	0.031952	0.03200970	-0.00180254
27,500.	0.031384	0.03143900	-0.00174942
28,000.	0.030823	0.03087534	-0.00169508
28,500.	0.030270	0.03031861	-0.00160323
29,000.	0.029725	0.02976872	-0.00146858
29,500.	0.029187	0.02922557	-0.00131974
30,000.	0.028657	0.02868907	-0.00111786
30,500.	0.028134	0.02815913	-0.00089227
31,000.	0.027619	0.02763564	-0.00060224
31,500.	0.027110	0.02711853	-0.00031466
32,000.	0.026610	0.02660771	0.00008623
32,500.	0.026116	0.02610307	0.00049524
33,000.	0.025629	0.02560455	0.00095501
33,500.	0.025149	0.02511204	0.00147165
34,000.	0.024676	0.02462548	0.00205161
34,500.	0.024210	0.02414477	0.00270177
35,000.	0.023751	0.02366983	0.00342940
36,000.	0.022853	0.02273694	0.00510442

Mean of Column 4 -0.00000178

Standard Deviation of Column 4 0.00140643

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TABLE 4. LEAST-SQUARES FIT OF U.S. STANDARD DENSITY  
36,200 - 65,000 ft

1 Altitude (ft)	2 U.S. Standard Density (lb/ft <sup>3</sup> )	3 L. S. Fit Density (lb/ft <sup>3</sup> )	4 <u>Col. 2 - Col. 3</u> <u>Col. 3</u>
36200.	0.022666	0.02253574	0.00578032
37000.	0.021814	0.02169457	0.00550490
38000.	0.020794	0.02068713	0.00516582
39000.	0.019822	0.01972648	0.00484233
40000.	0.018895	0.01881043	0.00449577
41000.	0.018012	0.01793693	0.00418541
42000.	0.017170	0.01710398	0.00385968
43000.	0.016367	0.01630972	0.00351190
44000.	0.015602	0.01555234	0.00319287
45000.	0.014873	0.01483014	0.00289033
46000.	0.014178	0.01414147	0.00258344
47000.	0.013516	0.01348478	0.00231541
48000.	0.012884	0.01285858	0.00197664
49000.	0.012282	0.01226147	0.00167447
50000.	0.011709	0.01169208	0.00144691
51000.	0.011162	0.01114914	0.00115366
52000.	0.010641	0.01063141	0.00090240
53000.	0.010144	0.01013772	0.00061976
54000.	0.0096701	0.00966695	0.00032545
55000.	0.0092186	0.00921805	0.00005944
56000.	0.0087882	0.00879000	-0.00020437
57000.	0.0083780	0.00838182	-0.00045561
58000.	0.0079870	0.00799260	-0.00070018
59000.	0.0076142	0.00762145	-0.00095105
60000.	0.0072589	0.00726754	-0.00118830
61000.	0.0069202	0.00693006	-0.00142260
62000.	0.0065973	0.00660825	-0.00165751
63000.	0.0062895	0.00630139	-0.00188719
64000.	0.0059961	0.00600878	-0.00211035
65000.	0.0057164	0.00572976	-0.00233130

Mean of Column 4 0.00003016

Standard Deviation of Column 4 0.00284086

The following equations were used in the least-squares fit of the U.S.  
Standard density:

$$0 \leq h \leq 36089$$

$$\rho = c_1 e^{(c_2 h)} + c_3 h$$

$$36,089 \leq h \leq 65,000$$

$$\rho = \rho_{36089} e^{(c_4 * (h - 36089))} + c_5 * (h - 36089)$$

where

h is the altitude (ft)

The coefficients obtained in the least-squares fit are:

$$\begin{aligned} c_1 &= 0.0766584476 \text{ (lb/ft}^3\text{)} \\ c_2 &= -0.282539693789 \text{ E-4 (ft}^{-1}\text{)} \\ c_3 &= -0.138466611596 \text{ E-6 (lb/ft}^4\text{)} \\ \rho_{36089} &= 0.0226549960 \text{ (lb/ft}^3\text{)} \\ c_4 &= -0.475504250122 \text{ E-4 (ft}^{-1}\text{)} \\ c_5 &= 0.459663274698 \text{ E-11 (lb/ft}^3\text{)} \end{aligned}$$

## RESULTS

The coefficients that were obtained by fitting the density data, and the root mean squares (rms) or standard deviation of the residuals and their algebraic means are given in Appendix C for the five stations analyzed. Data are presented for two times of day (0000 and 1200 hr G.m.t.) for the four seasons and for the seasons combined for each station.

Profiles of the density ratios for station E are given in Appendix D. The ratios were obtained by evaluating the least-squares fit of the observed densities at specified altitudes and dividing the density in each case by the U.S. Standard

density for the same altitude. Profiles are shown for the two times of day for each of the four seasons and for the seasons combined.

Profiles of the ballistic densities obtained by multiplying the ratios with the density weighting factors using equation (4) are shown in Appendix E for station E for the same conditions. Density ratios and ballistic densities were computed for each of the five stations, but the profiles are shown only for station E in Appendixes D and E.

While the ballistic densities were computed for the 27 zones listed in Table 1, only an abbreviated tabulation is given in Appendix F. Data are presented for only two zones, 30,000 and 50,000 ft. The ballistic densities were computed with equation (4), using the density weighting factors given in Table 2. Data for the two zones are given for each of the five stations and for each surface condition where sufficient data were available to make a least-squares fit to the observed data.

#### DISCUSSION OF RESULTS

One question is of primary interest—is there sufficient correlation between surface density and that of the upper atmosphere to accurately predict the ballistic density for various altitudes from surface measurements? To answer this question, we first note that the density ratio curves given in Appendix D for station E are families of very similar curves. If some of the curves were missing, we could do a fair job of reproducing the curves by interpolation. This would seem to indicate, qualitatively at least, that one could predict the density ratios aloft from the starting point of the curve on the x-axis, which is the surface density ratio. The same is true of the curves given for ballistic density in Appendix E. It deserves mentioning that the points plotted in Appendix D are not the mean values of individual sondes but are values corresponding to the functional fit.

The sondes were grouped in order that a more reliable mean and standard deviation could be established. It is recognized that the curves in Appendix D do not reflect the errors of the means or the variations in the upper atmosphere within a

group of sondes. A total of 14,800 sondes were processed in this study in an attempt to establish reliable means and standard deviations. In every fit, the mean and standard deviation were computed. These are tabulated in Appendix C. A large majority of the means are only a small fraction of one percent. The standard deviations of the residuals are given in Table 5 according to percentiles. A total of 300 fits was made in each of the two altitude zones, 0 to 36,000 and 36,000 to 65,000 ft. The standard deviations of the residuals were arranged in numerical order without regard to station, season, or time of day. The standard deviation of the 50th percentile is 1.114 percent in the lower altitude zone.

TABLE 5. STANDARD DEVIATIONS OF THE RESIDUALS

<u>Percentile</u>	Altitude	Altitude
	0 - 36,000 (ft) (%)	36,000 - 65,000 (ft) (%)
10	0.675	2.019
20	0.799	2.293
30	0.908	2.586
40	1.000	2.832
50	1.114	3.067
60	1.227	3.295
70	1.424	3.584
80	1.577	3.959
90	1.703	4.298
100	2.257	6.377

Note: The standard deviations in this table were obtained by multiplying the standard deviations (SIGMA) in Appendix C by 100 in order to express them as a percentage instead of as a ratio.

It should also be remembered that there are variations in the surface densities because of grouping the data, which probably has a negligible effect on the means but makes a small contribution to the standard deviations. The noise level in the data appears to increase with altitude, which is to be expected. The residuals are much larger in the fits above 36,000 ft than they are at the lower altitudes, while the density should be more stable at the higher altitudes.

It may be noted that the ballistic density represents a weighted average of the density ratios. Accordingly, any fluctuations that are random, and that may be

present in the ratios of the true density to the mean density, would tend to average out in computing the ballistic density.

Another question that deserves consideration is—how important is geographic location, season, and time of day? Only five stations used in the study are located in wide ocean areas, far from land, and between 30° and 50° N latitude. Data were available for only two times of day, 0000 and 1200 hr G.m.t., which makes it difficult to determine the diurnal variations. Based on the data available, there does not seem to be much payoff for preparing separate tables for different times of day and different seasons for the geographic areas that might be represented by the five stations.

There does appear to be a significant difference between the correlates of stations E, N, and C, North latitudes 35°, 50°, and 52° 45', respectively. The ballistic density at 30,000 ft, corresponding to the same surface density, is about one-half percent higher at the lower latitude stations than at station C. The surface densities run higher at station C. The upper air density may decrease more rapidly than it does at the other stations, resulting in lower ballistic densities for the same surface density.

Data by season do not appear to correlate differently, except at station C. The largest difference noted here was for surface density 1.03, where the ballistic density at 30,000 ft was about one percent lower in summer than in other seasons.

While the procedure presented in this report has been used on only five stations that have an oceanic climate, it should be possible to use essentially the same procedure for processing data from stations where the climate is more affected by land masses. Some modifications might be required, since the temperature lapse rate might be quite different. The diurnal and seasonal variations in pressure and temperature are normally much larger over land masses than they are over large bodies of water.

A similar but earlier study<sup>2</sup> was made by the Army Electronics Command, Fort Monmouth, New Jersey. Data from land-based stations were used in this study and a number of tables were prepared for each geographic area, season, and time of day.

CONCLUSIONS

1. There does appear to be a good correlation between the surface density and the density at various altitudes over the mid-ocean areas studied.
2. The resulting correlations are different for different latitudes. They do not change appreciably with diurnal time or season over the areas studied.
3. The differences between surface and upper atmospheric conditions are much larger over littoral areas.
4. The procedure described in this report for determining the correlation between upper air density and the surface density may be used for a variety of stations with only minor modifications to the procedure.
5. While the procedure for estimating ballistic density was developed primarily for firing Navy guns, it may also be useful to predict the ballistic density for air-launched missiles.
6. It is estimated that the density ratios at altitudes not to exceed 36,000 ft may be predicted with an error not to exceed 1.0 percent, using the correlation between the surface density and the density of the upper atmosphere.
7. It is estimated that the ballistic density may be predicted with an error not to exceed 0.5 percent in 90 percent of the cases where the altitude does not exceed 36,000 ft.
8. It is estimated that the ballistic density may be predicted with an error between one and two percent where the altitude is between 36,000 and 50,000 ft. This error could be reduced somewhat if the data used in the study had been collected with present day equipment.



RECOMMENDATIONS

1. Correlations should be obtained for other latitudes, including both maritime and beach areas of strategic importance.
2. More data should be obtained for the extremely low and high surface densities.
3. A further study should be conducted to determine how the procedure of estimating the ballistic density, as described in this report, could be implemented in fire control systems and in preparation of range tables.
4. Consideration should be given to using the analytic expression for density in computer programs that simulate the trajectories of unguided missiles.

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REFERENCES

1. U.S. Naval Academy, *Range and Ballistic Tables*, 1935, p. 84.
2. Marvin J. Lowenthal, *The Accuracy of Ballistic Density Departure Tables 1934-1972*, ECOM-5436, OSD 1366 (April 1972).
3. Committee on Extension to the Standard Atmosphere, *U.S. Standard Atmosphere, 1976*, (Washington, D.C.: Government Printing Office, 1976).

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APPENDIX A

A NONLINEAR LEAST-SQUARES TECHNIQUE

## A NONLINEAR LEAST-SQUARES TECHNIQUE

Statement of the Problem

Let  $(x_i, y_i)$ ,  $i = 1, 2, \dots, N$  be a set of  $N$  data points and

$$f(x, a_1, a_2, \dots, a_M) \quad (A-1)$$

be a function with  $x$  as the independent variable.  $(a_j)$ ,  $j = 1, 2, \dots, M$  are parameters of the function and the function may not be linear in these parameters.

We would like to determine values of the  $M$  parameters such that

$$F(a_1, a_2, \dots, a_M) = \sum_{i=1}^{i=N} W_i [Y_i - f(x_i, a_1, a_2, \dots, a_M)]^2 \quad (A-2)$$

is a minimum. This is the least-squares solution, which is the same as minimizing the sum of the squares of the residuals. A weight  $W_i$  is assigned to each data point.

For simplicity of notation, we let

$$f_i(a) = f(x_i, a_1, a_2, \dots, a_M), \quad i = 1, 2, \dots, N \quad (A-3)$$

where  $a = (a_1, a_2, \dots, a_M)$ . The only restriction on the function  $f_i(a)$  is that the partial derivatives of the function with respect to the  $M$  parameters be continuous in all of the arguments.

This implies that  $f_i(a)$  is a function that can be differentiated.

We assume that these partial derivatives exist at a point  $\bar{a}$ , and in some neighborhood about  $\bar{a}$ , which includes the point  $a$ . Let

$$a = \bar{a} + \Delta a \quad (A-4)$$

where  $\bar{a} = (\bar{a}_1, \bar{a}_2, \dots, \bar{a}_M)$  and  $\Delta a = (\Delta a_1, \Delta a_2, \dots, \Delta a_M)$ .

If  $f_i(a)$  can be differentiated at  $\bar{a}$ , then the differential at  $\bar{a}$  is an approximation to  $f_i(a) - f_i(\bar{a})$  and  $f_i(a) - f_i(\bar{a}) = 0(\Delta a)(a \rightarrow \bar{a})$ .

Thus,

$$f_i(a) - f_i(\bar{a}) = \sum_{j=1}^{j=M} \frac{\partial f_i(\bar{a})}{\partial a_j} \Delta a_j + E(\Delta a) \quad (A-5)$$

where  $E(\Delta a) \rightarrow 0$  as  $\Delta a \rightarrow 0$  for  $i = 1, 2, \dots, N$ .

If the approximation  $\bar{a}$  is close enough to the solution  $a$ , then the problem is considered solved when

$$|a_j - \bar{a}_j| = |\Delta a_j| \leq T, \quad j = 1, 2, \dots, M \quad (A-6)$$

where  $T$  = desired precision for the solution.

#### Formulation of Solution

We now derive the formulation for finding  $\Delta a$ . The solution  $a$  is then equal to  $\bar{a} + \Delta a$ .

Using equation (A-5), we form the overdetermined system of equations ( $N > M$ )

$$Y_i = f_i(a) = f_i(\bar{a}) + \sum_{j=1}^{j=M} \frac{\partial f_i(\bar{a})}{\partial a_j} \Delta a_j \quad (A-7)$$

for data points  $i = 1, 2, \dots, N$ .

The system of equations used to find  $\Delta a$  becomes

$$\frac{\partial f_i(\bar{a})}{\partial a_1} \Delta a_1 + \frac{\partial f_i(\bar{a})}{\partial a_2} \Delta a_2 + \dots + \frac{\partial f_i(\bar{a})}{\partial a_M} \Delta a_M = Y_i - f_i(\bar{a}) \quad (A-8)$$

(i = 1, 2, ..., N).

The system of observational equations (A-8) can now be written in matrix form as given by

$$AX = Y \quad (A-9)$$

where,

$$\Delta = \begin{bmatrix} \frac{\partial f_1(\bar{a})}{\partial a_1} & \frac{\partial f_1(\bar{a})}{\partial a_2} & \dots & \frac{\partial f_1(\bar{a})}{\partial a_M} \\ \frac{\partial f_2(\bar{a})}{\partial a_1} & \frac{\partial f_2(\bar{a})}{\partial a_2} & \dots & \frac{\partial f_2(\bar{a})}{\partial a_M} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial f_N(\bar{a})}{\partial a_1} & \frac{\partial f_N(\bar{a})}{\partial a_2} & \dots & \frac{\partial f_N(\bar{a})}{\partial a_M} \end{bmatrix}$$

$$X = \begin{bmatrix} \Delta a_1 \\ \Delta a_2 \\ \vdots \\ \Delta a_M \end{bmatrix}$$

$$Y = \begin{pmatrix} y_1 - f_1(\bar{a}) \\ y_2 - f_2(\bar{a}) \\ \vdots \\ y_N - f_N(\bar{a}) \end{pmatrix}$$

The column matrix Y is called the residual matrix. Solving matrix equation (A-9) yields the normal equations in matrix form

$$A^T A X = A^T Y \quad (A-10)$$

If the residuals are to be weighted, we can include the weight matrix W where,

$$W = \begin{pmatrix} w_1 & & & \\ & w_2 & & \\ & & \ddots & \\ & & & w_N \end{pmatrix} \quad (A-11)$$

Completing the solution to the matrix equation (A-10) and upon including the weight matrix, we have

$$X = (A^T W A)^{-1} A^T W Y \quad (A-12)$$

X is the least-squares solution to the system of equations (A-8) with the weights included. Elements of the X matrix are now tested in absolute value against the tolerance T. If the tolerance test is satisfied, we are done and the least-square solution to equation (A-2) is given by

$$a_j = \bar{a}_j + \Delta a_j, j = 1, 2, \dots, M \quad (A-13)$$

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Whenever the tolerance test fails, equation (A-13) gives the next approximation and the iteration process is repeated with matrix equation (A-12) until the tolerance test is satisfied.

Remarks

Once an acceptable solution has been found, it may be desirable to know how well the function fits the given data. Analysis for how well the solution fits can usually be made by examining the residuals for each observation.

The variances for the solution (a) can be found from the variance, covariance matrix.

If the variances and residuals are large, a different approximating function  $f_i(a)$  may be tested.

When polynomials are used for testing, the residuals will drop off rapidly as the degree of the polynomial increases from one. Further increase in the degree of the polynomial will show little improvement of the residuals.



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APPENDIX B

AN ALTERNATE METHOD FOR COMPUTING DENSITY

## AN ALTERNATE METHOD FOR COMPUTING DENSITY

Since the procedure used to fit the observed densities provided little information as to why the correction term for altitudes below 3,500 ft improved the fit, an investigation was made using a sample set of data obtained from 25 sondes. The sondes were taken consecutively from the group that had been sorted according to season after the surface densities were arranged in numerical order. The median of the surface densities in the sample was equal to the U.S. Standard density at mean sea level. The sondes were released at station E during the spring season, 1200 hr G.m.t.

Separate least-squares fits were made to the pressure and temperature in the altitude range from 0 to 36,089 ft. No attempt was made to fit the temperature or pressure above 36,089-ft altitude.

The equation used to fit the pressure is similar to equation (1)

$$P = p_1 e^{(p_2 h)} + p_3 h \quad (B-1)$$

where

P is the pressure (mb)

h is the altitude (ft)

$p_1$ ,  $p_2$ , and  $p_3$  are constants determined in the least-squares fit

The observed temperatures were first converted to virtual temperatures with the equation

$$TV = \frac{T}{1.0 - \frac{0.3783 * RH * V}{P}} \quad (B-2)$$

where

TV is the virtual temperature ( $^{\circ}$ K)

T is the observed temperature ( $^{\circ}$ K)

RH is the observed relative humidity (dimensionless)

V is the saturation vapor pressure (mb)

P is the observed pressure (mb)

Several least-squares fits were made with the virtual temperature in the altitude range from 0 to 36,089 ft using polynomials that, in every case, produced large residuals below 5,000 ft. A big improvement was made by segmenting the data into three zones, 0 to 3,500, 3,501 to 6,000, and 6,001 to 36,089 ft. A one-degree polynomial least-squares fit was used in the two lower zones and a third-degree polynomial was used in the upper zone. The intersections of the equations are located at 3,731 and 5,270 ft which were used to define the boundaries of the zones.

The density was computed with the equation

$$\rho = P/(R \cdot T) \quad (B-3)$$

where

$\rho$  is the density (lb/ft<sup>3</sup>)

P is the pressure determined by a least-squares fit (mb)

T is the temperature determined by a least-squares fit (°K)

R is a constant, 45.981610868

Computing the density in this manner made a small reduction in the mean of the residuals but no improvement in the standard deviation. While a single function fits the pressure from sea level to 36,089 ft, the nonlinearity in the temperature profile is quite apparent. The lapse rate in the temperature based on the least-squares fit from sea level to 3,731 ft is 2.60°C per 1,000 ft and 0.358°C per 1,000 ft from 3,731 to 5,270 ft using the intersections of the equations to define the zone boundaries. The average lapse rate based on the least-squares fit in the zone from 5,270 to 36,089 ft is 1.99°C per 1,000 ft. The latter value is in good agreement with the lapse rate of 1.98°C per 1,000 ft from sea level to 36,089 ft that was used to define the U.S. Standard atmosphere.

Profiles of the temperature and pressure obtained with the least-squares fit are shown in Figures B-1 and B-2, respectively. A profile of the density computed

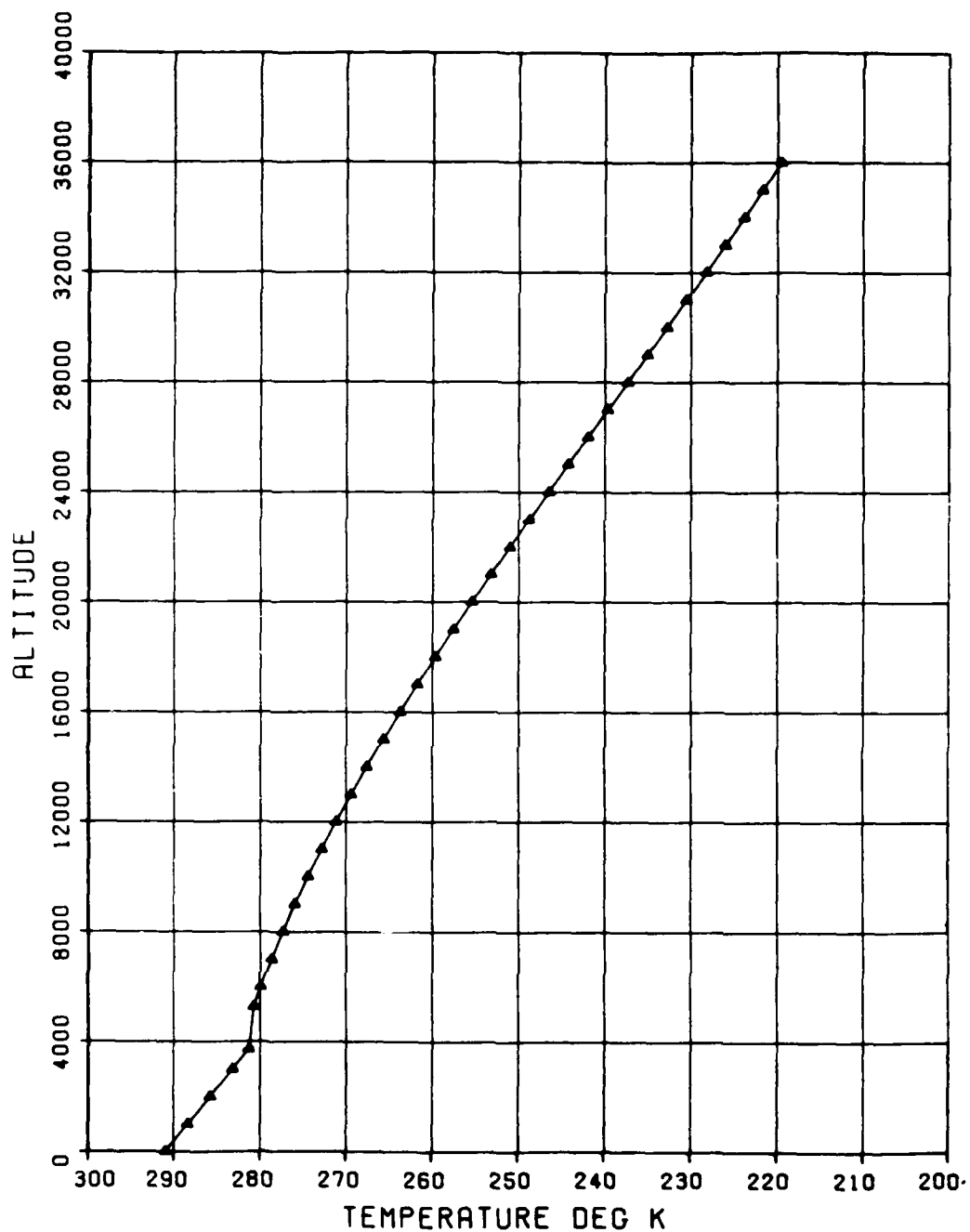


FIGURE B-1. STATION F SPRING 1200 hr G.m.t.  
Temperature profile based on three least-squares fits, linear 0 - 3,500, linear 3,500 - 6,000, and third-degree polynomial 6,000 - 3,600 ft. The equations were spliced at 3,730 and 5,270 ft.

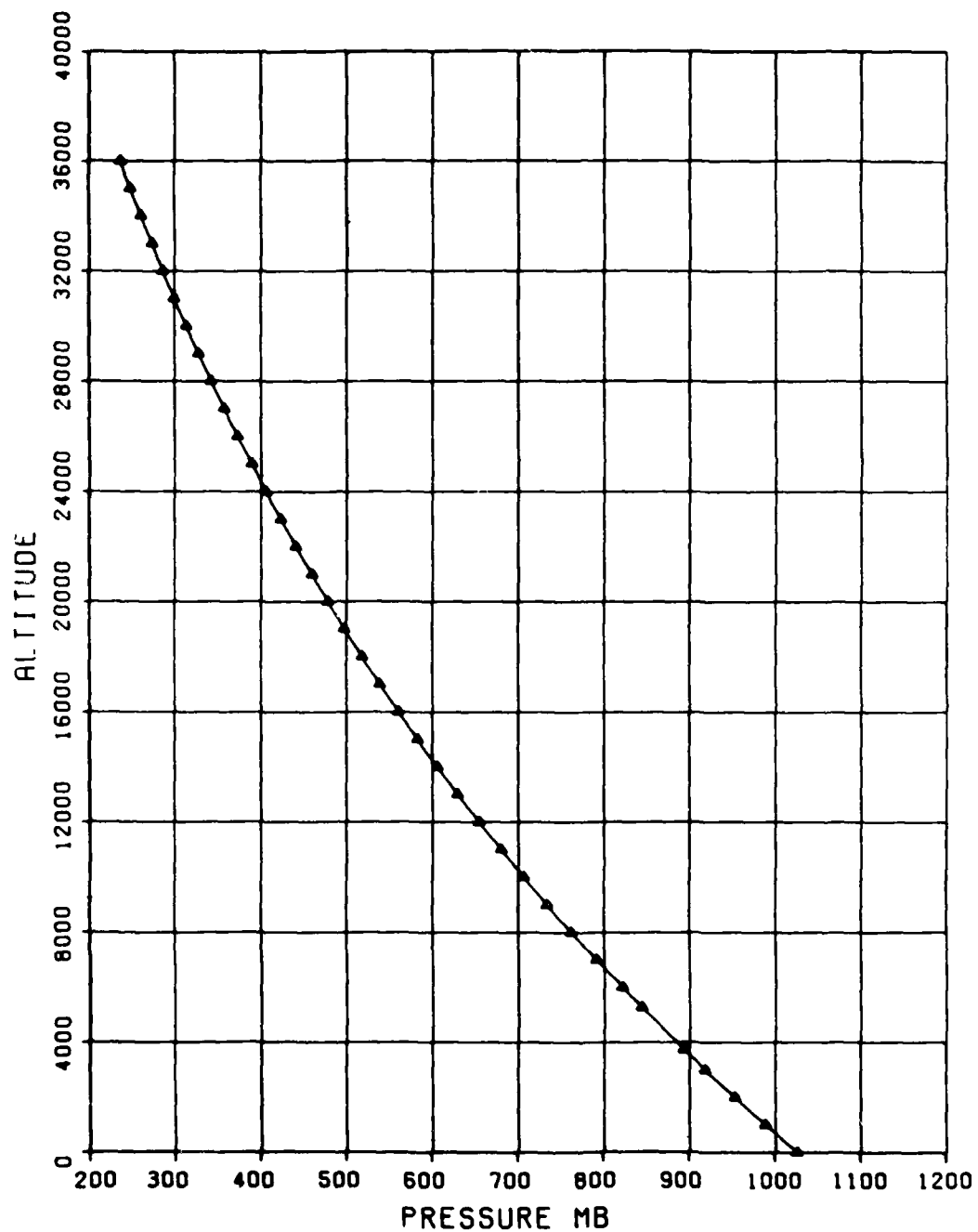


FIGURE B-2. STATION E 1200 hr G.m.t.  
Pressure profile based on a least-squares fit with an exponential function.

with equation (7) is shown in Figure B-3. For comparison, Figure B-4 is a profile of the density computed with equations (1) and (3) where the coefficients were obtained by making a least-squares fit to the observed densities. Very little difference can be seen when curves of Figures B-3 and B-4 are superimposed.

From these results—(1) the small difference in the residuals between the two methods of calculating densities, and (2) indiscernible difference in the two curves obtained—it appears that there is no advantage in computing density from smoothed temperature and pressure data versus smoothed density data. It may be noted that the first method requires 11 undetermined constants, the latter only 4.

The method of making separate least-squares fits to the temperature and pressure does provide a much clearer explanation as to why the correction term in equation (3) improved the fit to the density. The reason is the large variations in the lapse rate of the temperature at the lower altitudes.

The equations used to fit the temperature are

Altitude (ft)

0 - 3,500	Temperature = $a_0 + a_1 h$
3,500 - 6,000	Temperature = $a'_0 + a'_1 h$
6,000 - 36,000	Temperature = $a''_0 + a''_1 h + a''_2 h^2 + a''_3 h^3$

where

temperature is the virtual temperature °K

h is the altitude in feet

The altitudes of intersections are 3,731 and 5,270 ft.

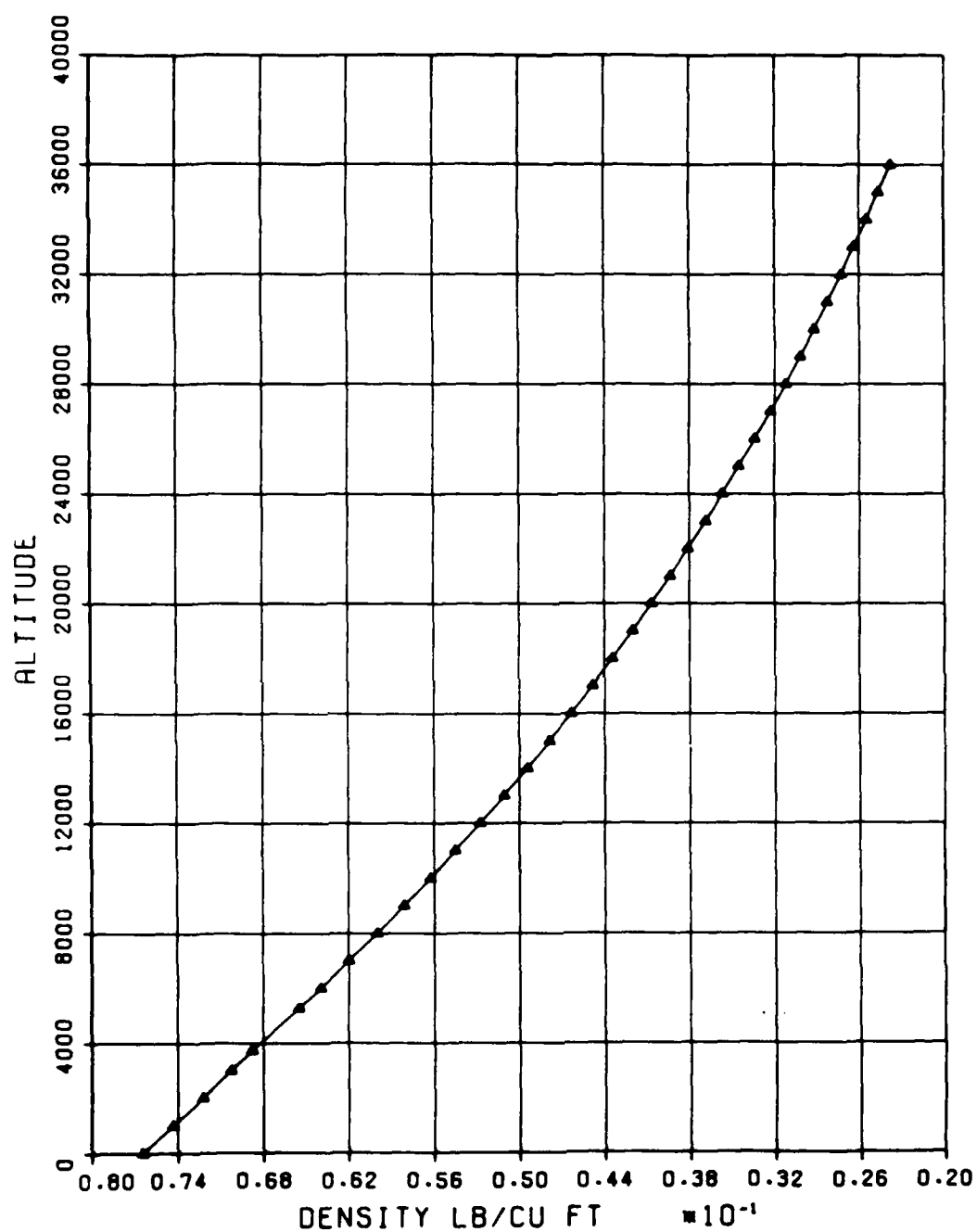


FIGURE B-3.  
Density profile computed from the data of Figures B-1 and B-2.

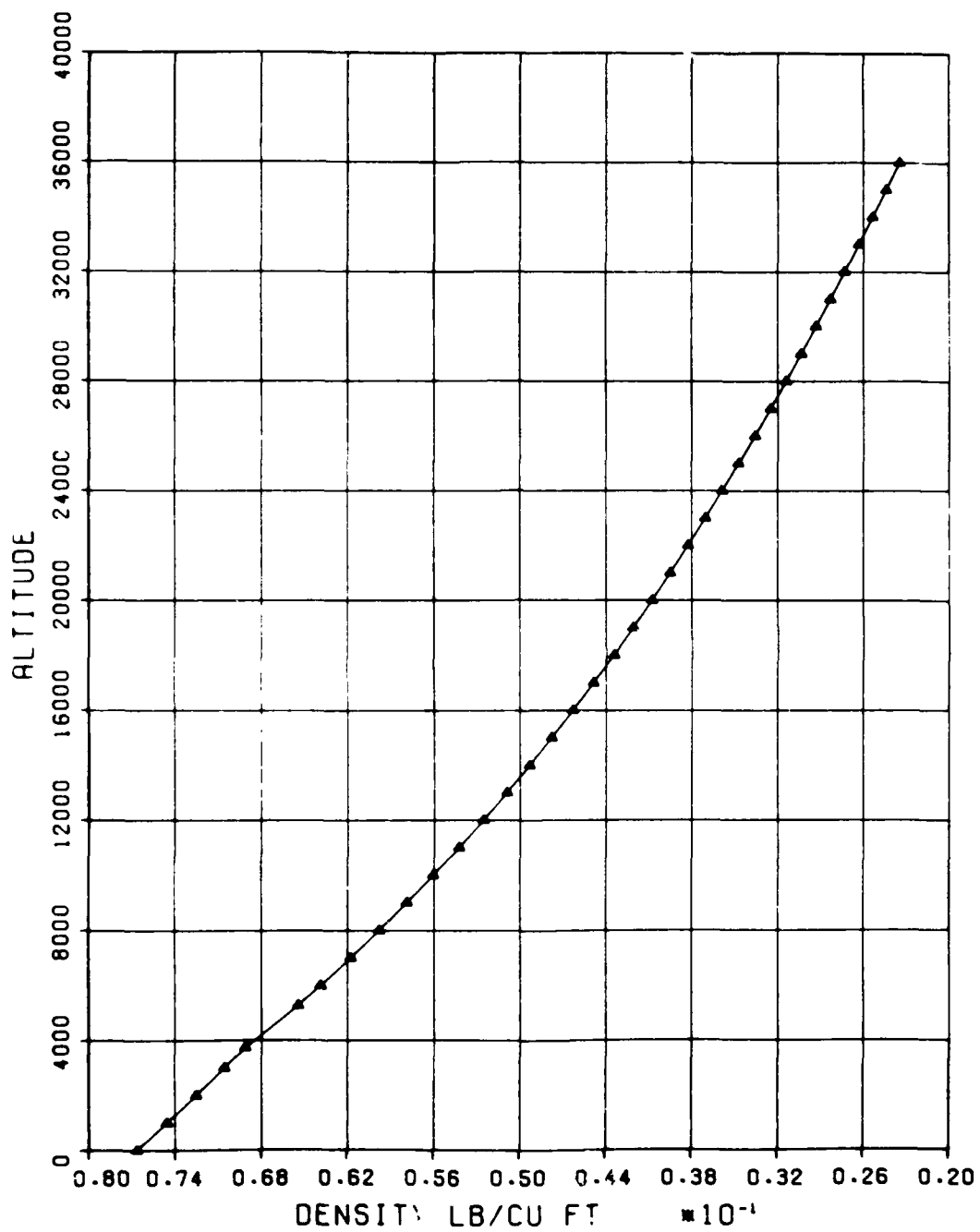


FIGURE B-4. STATION E SPRING 1200 h.r. G.m.t.  
Density profile computed directly from a least-squares fit to the density.



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The coefficients obtained in the least-squares fit are

$$\begin{aligned} a_0 &= 0.29098019920169 \text{ E}+3 \\ a_1 &= -0.26010921095663 \text{ E}-2 \\ a'_0 &= 0.28261034232183 \text{ E}+3 \\ a'_1 &= -0.35814511053088 \text{ E}-3 \\ a''_0 &= 0.28474414363984 \text{ E}+3 \\ a''_1 &= -0.42144325442356 \text{ E}-3 \\ a''_2 &= -0.69303432938534 \text{ E}-7 \\ a''_3 &= 0.85246672752231 \text{ E}-12 \end{aligned}$$

The mean and standard deviations of the residuals divided by the computed values are

Altitude (ft)	Mean	Sigma	N
0 - 3,500	-0.00000002	0.00603867	98
3,500 - 6,000	0.00000000	0.01019354	76
6,000 - 36,000	-0.00000008	0.01654041	357
0 - 36,000	-0.00000362	0.01433263	531

N is the number of data points in the fit.

The temperature profile is shown in Figure B-1.

The equation used to fit the pressure is

$$P = c_1 * e^{(c_2 h)} + c_3 h$$

where

P is pressure in mb

h is the altitude in feet

The coefficients obtained in the least-squares fit are

$$c_1 = 0.1025894426895 \text{ E}+4$$

$$c_2 = -0.3512226501974 \text{ E}-4$$

$$c_3 = -0.1469124958633 \text{ E}-2$$

The mean and standard deviation of the residuals divided by the computed values are

<u>Altitude (ft)</u>	<u>Mean</u>	<u>Sigma</u>	<u>N</u>
0 - 36,000	-0.00000270	0.01171363	531

N is the number of data points in the fit.

The pressure profile is shown in Figure B-2.

The density profile shown in Figure B-3 was computed with the equation

$$\rho = P/(R \cdot t)$$

where

$\rho$  is the density (lb/ft<sup>3</sup>)

P is the pressure (mb)

T is the virtual temperature (°K)

R is a constant, 45.981610868

The mean and standard deviation of the residuals divided by the computed value are

<u>Altitude (ft)</u>	<u>Mean</u>	<u>Sigma</u>	<u>N</u>
0 - 36,000	0.00009937	0.01129087	531

The density profile shown in Figure B-4 for altitudes below 3,500 ft was computed with the equation,

$$\rho = c_1 e^{(c_2 h)} + c_3 h + (\rho_0 - c_1) \left| \frac{3500 - h}{3500} \right|$$

and for altitudes equal to or greater than 3,500 ft was computed with the equation

$$\rho = c_1 e^{(c_2 h)} + c_3 h$$

which is the same procedure described previously in the report. The coefficients used to create the profile are

$$\begin{aligned} c_1 &= 0.076640263730 \text{ (lb/ft}^3\text{)} \\ c_2 &= -0.304780287061 \text{ E-4 (ft}^{-1}\text{)} \\ \rho_0 &= 0.076474 \text{ (lb/ft}^3\text{)} \\ c_3 &= -0.517405589378 \text{ E-7 (lb/ft}^4\text{)} \end{aligned}$$

The mean and standard deviation of the residuals divided by the computed value are

<u>Altitude (ft)</u>	<u>Mean</u>	<u>Sigma</u>
0 - 36,000	0.00048651	0.01160715

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APPENDIX C

COEFFICIENTS OBTAINED BY FITTING OBSERVED DENSITY

TR 82-81

In this appendix, four lines of data appear for each group of sondes that were used in the least-squares fit.

Lines 1 and 2:

<u>Item</u>	<u>Identification</u>	<u>Description</u>
1	N	Number of data points that met tolerances
2	JE	Number of points used in fit
3	AMEAN	Mean of the residuals
4	SIGMA	Standard deviation of the residuals

Line 1 is for the altitude range from 0 to 36,089 ft, and Line 2 is for the altitude range 36,089 to 65,000 ft. The first five items in Lines 3 and 4 are coefficients  $C_1$ ,  $C_2$ , and  $C_3$  for equation (1), which were obtained by making a least-squares fit in the altitude range 3,500 to 36,089 ft, and coefficients  $C_4$  and  $C_5$  for equation (2), which were obtained by making a least-squares fit in the altitude range 36,089 to 65,000. The coefficients are listed in the order of their subscripts. The next item on Line 4 is the median of the surface densities of the sondes used in the fit. The last item is a counter and has no significance.

Data points refer to the individual altitudes where temperature, pressure, and humidity were recorded. The residuals were expressed as a ratio of the residual to the density obtained with the least-squares fit as stated previously. No data points were eliminated in the least-squares fit; but tolerances on the residuals were specified, and the number of points that met the tolerances were recorded. The tolerance used in the lower altitude region was 0.025, and in the higher region it was 0.150. A few tests were made to eliminate bad data points before the least-squares fit was performed.

## STATION E 00MR FOUR SEASONS

## WINTER

106 N	106 JE	.00009371	AMEAN	.00499973	SIGMA
37 N	37 JE	.00053558	AMEAN	.01342884	SIGMA
.075079281683	-.294862954960E-04			-.697033163821E-07	-.450744290603E-04
-.159550178886E-07	.07418000	1			
535 N	547 JE	.00004310	AMEAN	.01235709	SIGMA
173 N	176 JE	-.00032082	AMEAN	.03395270	SIGMA
.075748131856	-.305428508314E-04			-.518345657782E-07	-.409038381380E-04
-.449743040887E-07	.07494500	2			
547 N	553 JE	.00006191	AMEAN	.00879245	SIGMA
198 N	198 JE	-.00192602	AMEAN	.02936409	SIGMA
.076519989588	-.301148012167E-04			-.627915978676E-07	-.451529783579E-04
-.147871540870E-07	.07570900	3			
565 N	592 JE	.00021436	AMEAN	.00852413	SIGMA
230 N	230 JE	-.00062556	AMEAN	.03150237	SIGMA
.077508432763	-.305740514838E-04			-.500335521527E-07	-.457665151713E-04
-.980870348999E-08	.07647400	4			
624 N	632 JE	.00033378	AMEAN	.00948879	SIGMA
240 N	240 JE	.00009101	AMEAN	.03334458	SIGMA
.078881310762	-.323681211507E-04			-.199368741673E-07	-.459076070910E-04
-.162405407298E-07	.07723900	5			
106 N	107 JE	.00001313	AMEAN	.00984285	SIGMA
46 N	46 JE	-.00164000	AMEAN	.02560609	SIGMA
.080252489385	-.338561615734E-04			.560937162076E-08	-.507730626667E-04
.150172841422E-07	.07800300	6			

## SPRING

85 N	85 JE	-.00012323	AMEAN	.00419959	SIGMA
33 N	33 JE	-.00032452	AMEAN	.03489420	SIGMA
.074353885262	-.284235206192E-04			-.941032720434E-07	-.380570178375E-04
-.727382338584E-07	.07418000	7			
716 N	721 JE	.00013955	AMEAN	.00629754	SIGMA
271 N	271 JE	.00186141	AMEAN	.03009369	SIGMA
.075733087556	-.300418665094E-04			-.551187072110E-07	-.394703344566E-04

--.625403819063E-07		.07494500	8	AMEAN	.01023382	SIGMA
594 N	605 JE	.00023908	8	AMEAN	.02999432	SIGMA
220 N	220 JE	.00131510	8	AMEAN	.02999432	SIGMA
.076742754647	--.306838920088E-04		3	AMEAN	.00960208	SIGMA
--.423100572783E-07	.07570900		3	AMEAN	.03557140	SIGMA
529 N	535 JE	.00046346	3	AMEAN	.00960208	SIGMA
205 N	205 JE	--.00008578	3	AMEAN	.03557140	SIGMA
.077239352033	--.312365997541E-04		19	AMEAN	.01277639	SIGMA
--.368989089084E-07	.07647400		19	AMEAN	.02579073	SIGMA
115 N	117 JE	.00084830	19	AMEAN	.02579073	SIGMA
44 N	44 JE	.00242485	11	AMEAN	.02579073	SIGMA
.078432436906	--.319666630560E-04		11	AMEAN	.02579073	SIGMA
--.126913193672E-07	.07723900		11	AMEAN	.02579073	SIGMA
SUMMER						
39 N	39 JE	.00003057	12	AMEAN	.00442968	SIGMA
13 N	13 JE	.00188364	12	AMEAN	.01798935	SIGMA
.074002617454	--.299262474105E-04		12	AMEAN	.00495224	SIGMA
--.135069282391E-06	.07265000		12	AMEAN	.01876588	SIGMA
557 N	557 JE	.00005280	13	AMEAN	.00495224	SIGMA
172 N	172 JE	.00196325	13	AMEAN	.01876588	SIGMA
.674411095244	--.294635397582E-04		13	AMEAN	.00495224	SIGMA
--.114884418235E-06	.07341500		13	AMEAN	.01876588	SIGMA
582 N	583 JE	.00025465	14	AMEAN	.00495224	SIGMA
167 N	167 JE	.00180320	14	AMEAN	.01876588	SIGMA
.075116341423	--.293381346612E-04		14	AMEAN	.00495224	SIGMA
--.100301112936E-06	.07418000		14	AMEAN	.01876588	SIGMA
601 N	601 JE	.00008318	15	AMEAN	.00495224	SIGMA
167 N	167 JE	.00170748	15	AMEAN	.01876588	SIGMA
.076057514114	--.302017801983E-04		15	AMEAN	.00495224	SIGMA
--.888873039486E-07	.07494500		15	AMEAN	.01876588	SIGMA
65 N	66 JE	.00044599	16	AMEAN	.00495224	SIGMA
33 N	33 JE	.00145388	16	AMEAN	.01876588	SIGMA
.076583644671	--.324380267945E-04		16	AMEAN	.00495224	SIGMA
--.103389959675E-06	.07570900		16	AMEAN	.01876588	SIGMA

FALL

76 N	76 JE	.00032131	AMEAN	.00639478	SIGMA
30 N	30 JE	.00088378	AMEAN	.03100741	SIGMA
.074885189662	-.297345986104E-04		-.570098172919E-07	-.3680	21504810E-04
-.017375737339E-07	.07341500	17			
552 N	557 JE	.00031220	AMEAN	.00706654	SIGMA
185 N	185 JE	.00001647	AMEAN	.03334804	SIGMA
.075059277710	-.296044770631E-04		-.623120720704E-07	-.366529441989E-04	
-.018355014763E-07	.07418000	18			
566 N	568 JE	.00016250	AMEAN	.00716179	SIGMA
219 N	219 JE	.00047250	AMEAN	.03144311	SIGMA
.075989491796	-.306654221840E-04		-.394741248165E-07	-.396086519246E-04	
-.606540996052E-07	.07494500	19			
579 N	584 JE	.00020431	AMEAN	.00897739	SIGMA
231 N	231 JE	-.00060221	AMEAN	.02636899	SIGMA
.077258445293	-.315266459161E-04		-.259998924279E-07	-.440922788535E-04	
-.260602884661E-07	.07570900	20			
124 N	124 JE	-.00023166	AMEAN	.00855050	SIGMA
41 N	41 JE	-.00215124	AMEAN	.02388429	SIGMA
.078307086422	-.317086362801E-04		-.337162163019E-07	-.486503319257E-04	
-.169464336075E-08	.07647400	21			

STATION E 00HR GMT SEASONS COMBINED

55 N	55 JE	-.00013503	AMEAN	.00438076	SIGMA
21 N	21 JE	.00153047	AMEAN	.01751126	SIGMA
.073916454338	-.297183718810E-04		-.526446694885E-07	-.288613372848E-04	
-.153449666026E-06	.07265000	1			
542 N	543 JE	.00007340	AMEAN	.00521675	SIGMA
168 N	168 JE	.00182577	AMEAN	.02135036	SIGMA
.074461986973	-.294345939445E-04		-.586052812264E-07	-.341636027919E-04	
-.103945419144E-06	.07341500	2			
561 N	561 JE	.00034351	AMEAN	.00811733	SIGMA
174 N	174 JE	.00078476	AMEAN	.02222567	SIGMA
.075164029585	-.296631277419E-04		-.573271511476E-07	-.366071002444E-04	
-.798583058256E-07	.07418000	3			
629 N	633 JE	.00006990	AMEAN	.00743407	SIGMA



238 N	239 JE	.00077494	AMEAN	.03043555	SIGMA
.076003913198	--.305940735172E-04			--.416309714657E-07	--.404390289412E-04
--.504645843921E-07	.07494500				
539 N	550 JE	.00024759	AMEAN	.01056239	SIGMA
161 N	161 JE	.00111095	AMEAN	.02725811	SIGMA
.076678434996	--.308753218587E-04			--.446318169070E-07	--.421188254661E-04
--.406749569099E-07	.07570900				
585 N	592 JE	.00015789	AMEAN	.00839561	SIGMA
226 N	226 JE	--.00095049	AMEAN	.03406700	SIGMA
.077586192104	--.311540064632E-04			--.422547625365E-07	--.450706163171E-04
--.180519540787E-07	.07647400				
548 N	555 JE	.00046953	AMEAN	.01040882	SIGMA
225 N	225 JE	.00093183	AMEAN	.03213343	SIGMA
.078649231085	--.323476217940E-04			--.168946267275E-07	--.457746168953E-04
--.188835761990E-07	.07723900				
155 N	157 JE	.00015486	AMEAN	.01001072	SIGMA
70 N	70 JE	--.00117266	AMEAN	.02554801	SIGMA
.080008865235	--.332939606239E-04			--.482455101442E-08	--.507021981509E-04
.138064671447E-07	.07800300				
31 N	40 JE	--.00142227	AMEAN	.02145617	SIGMA
16 N	16 JE	.00136873	AMEAN	.01188424	SIGMA
.080111899019	--.346798589829E-04			.402026625526E-07	--.490576876369E-04
--.570790632045E-08	.07876800				

STATION E 12HR FOUR SEASONS

WINTER					
155 N	155 JE	--.00088078	AMEAN	.00489720	SIGMA
37 N	37 JE	.00023310	AMEAN	.02602642	SIGMA
.075030877430	--.309326914800E-04			--.550372354609E-07	--.395274000844E-04
--.543206237525E-07	.07418000				
545 N	557 JE	--.00018071	AMEAN	.01084876	SIGMA
218 N	218 JE	--.00065341	AMEAN	.03285415	SIGMA
.076197196680	--.303223535418E-04			--.601704522812E-07	--.459187309579E-04
--.588017794425E-08	.07494500				

591 N 594 JE .00011055 AMEAN .00709901 SIGMA  
 249 N 249 JE -.00085312 AMEAN .02425483 SIGMA  
 .077022282557 -.310423451067E-04 -.428056661647E-07 -.461343999269E-04  
 -.795508850802E-08 .07570900  
 335 N 335 JE .00026528 AMEAN .00999285 SIGMA  
 146 N 146 JE .0002409 AMEAN .02278905 SIGMA  
 .077820361702 -.314542580480E-04 -.347222888008E-07 -.432410190256E-04  
 -.332274942909E-07 .07647400  
 611 N 617 JE .00029613 AMEAN .00906797 SIGMA  
 254 N 254 JE -.00133092 AMEAN .02851303 SIGMA  
 .079158387943 -.330580221397E-04 -.215356284127E-08 -.483625659055E-04  
 -.807231527157E-09 .07723900

## SPRING

219 N 219 JE -.00005360 AMEAN .00389571 SIGMA  
 95 N 95 JE .00121376 AMEAN .03599471 SIGMA  
 .075123190148 -.295923492901E-04 -.685606999806E-07 -.415998156953E-04  
 -.406396599472E-07 .07418000  
 572 N 576 JE .00011338 AMEAN .00738243 SIGMA  
 240 N 240 JE .00083964 AMEAN .03431977 SIGMA  
 .075830354575 -.302078603356E-04 -.543715278413E-07 -.402946907470E-04  
 -.534843663219E-07 .07494500  
 524 N 528 JE .00039618 AMEAN .01730689 SIGMA  
 214 N 214 JE .00163039 AMEAN .02414344 SIGMA  
 .076640263730 -.304790287061E-04 -.517405589378E-07 -.410525537453E-04  
 -.484707804362E-07 .07570900  
 522 N 531 JE .00048651 AMEAN .01160715 SIGMA  
 253 N 255 JE .00024623 AMEAN .02951284 SIGMA  
 .077487922568 -.313676919544E-04 -.353021223364E-07 -.438039057253E-04  
 -.292856394714E-07 .07647400  
 101 N 102 JE .00157844 AMEAN .01217757 SIGMA  
 27 N 27 JE .00001065 AMEAN .01501577 SIGMA  
 .078733576672 -.330111444168E-04 .166763630605E-08 -.474730682042E-04  
 -.844893833634E-08 .07723900

## SUMMER

562 N	562 JE	.0003631	AMEAN	.0057620	SIGMA
242 N	242 JE	.0018701	AMEAN	.0217020	SIGMA
.074541372461	-.296703645956E-04			-.554732911082E-07	-.335399439230E-04
-.109059773373E-06	.07341500	11			
532 N	532 JE	.00029180	AMEAN	.00516922	SIGMA
171 N	171 JE	.00100929	AMEAN	.0145597	SIGMA
.075214489043	-.294920244574E-04			-.616491043396E-07	-.361677762944E-04
-.840571249790E-07	.07418000	12			
504 N	507 JE	.00030070	AMEAN	.0225664	SIGMA
196 N	196 JE	.00189725	AMEAN	.02122023	SIGMA
.075858349635	-.299037346719E-04			-.568828999155E-07	-.353067485094E-04
-.940225706960E-07	.07494500	13			

## FALL

101 N	103 JE	.00036658	AMEAN	.01249749	SIGMA
28 N	28 JE	.00178426	AMEAN	.01635500	SIGMA
.075386975714	-.316199839816E-04			-.126806169228E-07	-.382494516627E-04
-.716522639671E-07	.07341500	14			
504 N	505 JE	.00024980	AMEAN	.00557367	SIGMA
257 N	257 JE	.00105104	AMEAN	.02811453	SIGMA
.075244152320	-.304716383621E-04			-.390097796857E-07	-.364552200297E-04
-.862710989754E-07	.07418000	15			
500 N	503 JE	.00028466	AMEAN	.00855190	SIGMA
198 N	198 JE	.00073576	AMEAN	.02917977	SIGMA
.075879139253	-.306557368546E-04			-.391173189122E-07	-.377710286554E-04
-.744068380949E-07	.07494500	16			
537 N	541 JE	.00035236	AMEAN	.01060197	SIGMA
225 N	225 JE	.00026563	AMEAN	.02507368	SIGMA
.077099881194	-.309308827165E-04			-.463637399804E-07	-.407976746180E-04
-.502856873135E-07	.07570900	17			
189 N	192 JE	.00001691	AMEAN	.01039020	SIGMA
81 N	81 JE	.00041722	AMEAN	.03495259	SIGMA
.078636487486	-.333117573130E-04			.306983969321E-08	-.434169559436E-04
-.392624149192E-07	.07647400	18			

STATION E 12HR GMT SEASONS COMBINED

83 N	83 JE	--.00021132	AMEAN	.00500070	SIGMA
40 N	40 JE	.00209744	AMEAN	.02342494	SIGMA
.074046594670	--.297621698012E-04	.07265000	1	--.561603633550E-07	--.304381710796E-04
--.132484417091E-06					
564 N	566 JE	.00007565	AMEAN	.00749577	SIGMA
229 N	229 JE	.00177311	AMEAN	.02145995	SIGMA
.074764931991	--.300376322102E-04	.07341500	2	--.475062967547E-07	--.340757002530E-04
--.104346667670E-06					
559 N	559 JE	.00019089	AMEAN	.00622409	SIGMA
226 N	227 JE	.00093570	AMEAN	.03109516	SIGMA
.075164001806	--.297553589230E-04	.07418000	3	--.575532631951E-07	--.378655930475E-04
--.718505014332E-07					
546 N	548 JE	.00026285	AMEAN	.00781521	SIGMA
175 N	175 JE	--.00023137	AMEAN	.03879552	SIGMA
.075999033383	--.305589095068E-04	.07494500	4	--.459294593779E-07	--.389371012515E-04
--.640440113895E-07					
549 N	553 JE	.00033323	AMEAN	.00928353	SIGMA
229 N	229 JE	.00091878	AMEAN	.02443316	SIGMA
.076847976664	--.308670522879E-04	.07570900	5	--.448103227586E-07	--.423018423799E-04
--.389831276971E-07					
539 N	549 JE	.00057035	AMEAN	.01217471	SIGMA
256 N	258 JE	.00015215	AMEAN	.03158384	SIGMA
.077741410559	--.314122542703E-04	.07647400	6	--.384551540687E-07	--.425026724634E-04
--.384231841904E-07					
266 N	268 JE	.00014534	AMEAN	.00842401	SIGMA
97 N	97 JE	--.00210771	AMEAN	.02880938	SIGMA
.079161559258	--.332958045749E-04	.07723900	7	--.372624763272E-09	--.489518104223E-04
.688395383325E-08					
123 N	124 JE	--.00022082	AMEAN	.00996760	SIGMA
75 N	75 JE	--.00243365	AMEAN	.02582058	SIGMA
.080305994829	--.346243599295E-04	.07800300	8	.248231111476E-07	--.513815102647E-04
.178521124110E-07					

## STATION V 00HR FOUR SEASONS

WINTER					
83 N	83 JE	.00003488	AMEAN	.00867984	SIGMA
27 N	27 JE	-.00009238	AMEAN	.01895347	SIGMA
.074525310138	-.294218657930E-04			-.889947170139E-07	-.357431352087E-04
-.759650134623E-07	.07416000				
429 N	468 JE	.00021326	AMEAN	.01663872	SIGMA
165 N	165 JE	-.00054370	AMEAN	.02743251	SIGMA
.0758402533696	-.287994758650E-04			-.126614671712E-06	-.377219365718E-04
-.589023875855E-07	.07494500				
521 N	579 JE	.00017659	AMEAN	.01462575	SIGMA
223 N	223 JE	.00087728	AMEAN	.03009421	SIGMA
.076734353922	-.300731732332E-04			-.882602213997E-07	-.401466385334E-04
-.475488083265E-07	.07570900				
485 N	537 JE	.00021426	AMEAN	.01723800	SIGMA
173 N	173 JE	-.00154323	AMEAN	.02983285	SIGMA
.077994143861	-.302072669337E-04			-.108472239971E-06	-.375602452599E-04
-.615770739966E-07	.07647400				
484 N	547 JE	.00016713	AMEAN	.01588830	SIGMA
179 N	179 JE	-.00004863	AMEAN	.03214428	SIGMA
.079468035421	-.319857227511E-04			-.684759761459E-07	-.432629505650E-04
-.263435881045E-07	.07723900				
121 N	128 JE	.00000446	AMEAN	.01377598	SIGMA
39 N	39 JE	.00018888	AMEAN	.02886136	SIGMA
.080502548356	-.326935671221E-04			-.623200361131E-07	-.438780590958E-04
-.202332989177E-07	.07800300				
SPRING					
331 N	331 JE	-.00021690	AMEAN	.00665090	SIGMA
135 N	135 JE	.00179898	AMEAN	.02282032	SIGMA
.074453385033	-.305400405068E-04			-.389115214548E-07	-.293581924203E-04
-.145083536797E-06	.07418000				
554 N	554 JE	.00022910	AMEAN	.00674795	SIGMA
224 N	224 JE	.00089275	AMEAN	.02677927	SIGMA
.075297620599	-.307737336106E-04			-.381636865587E-07	-.342898622142E-04

--.992698633533E-07		.07494500	8		
496 N	499 JE	.00069663	AMEAN	.00841648	SIGMA
233 N	233 JE	.00117567	AMEAN	.02706887	SIGMA
.076375355053	--.319260019310E-04		--.151112583285E-07	--.365229419267E-04	
--.826885916713E-07	.07570900	9			
486 N	491 JE	.00079095	AMEAN	.01025155	SIGMA
183 N	183 JE	.00025417	AMEAN	.02994907	SIGMA
.077403076367	--.319212861014E-04		--.265096729784E-07	--.420671940430E-04	
--.382377037819E-07	.07647400	10			
450 N	479 JE	.00069546	AMEAN	.01556209	SIGMA
218 N	218 JE	.00075293	AMEAN	.03164796	SIGMA
.078506446170	--.329034979386E-04		--.121449057635E-07	--.425025201965E-04	
--.344639618665E-07	.07723900	11			
77 N	80 JE	.00111974	AMEAN	.01556016	SIGMA
32 N	32 JE	.00045779	AMEAN	.03555065	SIGMA
.080158620606	--.338559601999E-04		--.791389394562E-08	--.437431445873E-04	
--.250120355242E-07	.07800300	12			
SUMMER					
257 N	252 JE	.00049459	AMEAN	.00518061	SIGMA
130 N	130 JE	.00046939	AMEAN	.01562624	SIGMA
.073834695782	--.299075280005E-04		--.469988143453E-07	--.293497892563E-04	
--.146006104824E-06	.07265000	13			
537 N	537 JE	.00041293	AMEAN	.00536209	SIGMA
246 N	246 JE	.00111684	AMEAN	.01991504	SIGMA
.074398672355	--.298644556726E-04		--.509673466174E-07	--.303159600471E-04	
--.137255272276E-06	.07341500	14			
474 N	484 JE	.00011263	AMEAN	.00864456	SIGMA
204 N	204 JE	.00108644	AMEAN	.02436276	SIGMA
.074653295496	--.303068679490E-04		--.423049486968E-07	--.381955326060E-04	
--.140801919785E-06	.07418000	15			
223 N	223 JE	.00050054	AMEAN	.00726032	SIGMA
81 N	81 JE	.00155510	AMEAN	.02114007	SIGMA
.075490897693	--.312039232458E-04		--.287569972084E-07	--.295621761640E-04	
--.149857332670E-06	.07494500	16			
79 N	79 JE	.00110488	AMEAN	.00704344	SIGMA

28 N 28 JE .00220634 AMEAN .02351338 SIGMA  
 .076452825232 --.322150969424E-04 --.105782531427E-07 --.305438953662E-04  
 --.143182030283E-06 .07570900 17

## FALL

63 N 66 JE .00089652 AMEAN .01184406 SIGMA  
 29 N 29 JE .00072779 AMEAN .03187706 SIGMA  
 .074529973823 --.298053874036E-04 --.675775141757E-07 --.323187648035E-04  
 --.110701869053E-06 .07265000 18  
 473 N 483 JE .00057329 AMEAN .01183236 SIGMA  
 202 N 202 JE .00025734 AMEAN .02593735 SIGMA  
 .074470020403 --.303310851642E-04 --.424962721334E-07 --.326282530301E-04  
 --.108744669638E-06 .07341500 19  
 558 N 575 JE .00042831 AMEAN .00967863 SIGMA  
 252 N 252 JE .00096085 AMEAN .02890084 SIGMA  
 .075196633828 --.307456039839E-04 --.387826647628E-07 --.318198270188E-04  
 --.118934036614E-06 .07418000 20  
 488 N 508 JE .00041327 AMEAN .01128679 SIGMA  
 196 N 197 JE .00034275 AMEAN .03069611 SIGMA  
 .076475725405 --.313048960551E-04 --.394490967851E-07 --.351120856390E-04  
 --.896076790981E-07 .07494500 21  
 513 N 532 JE .00029409 AMEAN .01134144 SIGMA  
 188 N 188 JE .00070575 AMEAN .02676650 SIGMA  
 .077303846377 --.310324373275E-04 --.565250578697E-07 --.364050371350E-04  
 --.770845504180E-07 .07570900 22  
 233 N 249 JE .00055884 AMEAN .01366360 SIGMA  
 100 N 101 JE .00136592 AMEAN .03400048 SIGMA  
 .078009883524 --.307006562986E-04 --.808890673004E-07 --.381294677370E-04  
 --.597978694152E-07 .07647400 23

## STATION V 00HR GMT SEASONS COMBINED

224 N 227 JE .00066458 AMEAN .00693522 SIGMA  
 111 N 111 JE .00104679 AMEAN .02385175 SIGMA  
 .073742726211 --.295084259006E-04 --.509910915601E-07 --.294580426712E-04  
 --.141212329378E-06 .07265000 1  
 548 N 550 JE .00038254 AMEAN .00960745 SIGMA

250 N	250 JE	.00096174	AMEAN	.01855027	SIGMA
.074285321915	-.296404591366E-04			-.552296924611E-07	-.303731981129E-04
-.137345456879E-06	.07341500				
463 N	467 JE	.00018092	AMEAN	.00891575	SIGMA
192 N	192 JE	.00112189	AMEAN	.02788104	SIGMA
.074568129060	-.302857871537E-04			-.433444133352E-07	-.311252305886E-04
-.129308750209E-06	.07418000				
493 N	497 JE	.00024288	AMEAN	.00947701	SIGMA
216 N	221 JE	-.00062345	AMEAN	.04046570	SIGMA
.075483116503	-.307409426338E-04			-.445518593752E-07	-.348111024533E-04
-.951991274713E-07	.07494500				
477 N	495 JE	.00037819	AMEAN	.01217347	SIGMA
204 N	205 JE	.00052841	AMEAN	.03139579	SIGMA
.076819784822	-.31082842379E-04			-.537445699170E-07	-.367416884154E-04
-.756635078414E-07	.07570900				
503 N	543 JE	.00045160	AMEAN	.01605234	SIGMA
184 N	184 JE	-.00065091	AMEAN	.03406634	SIGMA
.377727660911	-.306318303699E-04			-.841716006234E-07	-.382500798133E-04
-.577647836360E-07	.07647400				
446 N	512 JE	.00028312	AMEAN	.01638828	SIGMA
187 N	187 JE	-.00104431	AMEAN	.04069482	SIGMA
.079205506138	-.322837087475E-04			-.484228059255E-07	-.443498196073E-04
-.207590944958E-07	.07723900				
186 N	209 JE	.00046880	AMEAN	.01594894	SIGMA
64 N	64 JE	.00042416	AMEAN	.03376212	SIGMA
.080135279840	-.333287227749E-04			-.314208332089E-07	-.417557878261E-04
-.398084367770E-07	.07800300				

STATION V 12HR FOUR SEASONS

WINTER					
285 N	317 JE	.00030677	AMEAN	.01389208	SIGMA
102 N	102 JE	.00101340	AMEAN	.02943109	SIGMA
.075624332070	-.288980828583E-04			-.115006992028E-06	-.366286477706E-04
-.787878194283E-07	.07494500				



519 N	576 JE	.00020244	AMEAN	.01463718	SIGMA
193 N	193 JE	.00103998	AMEAN	.02591571	SIGMA
.076592440859	--.290187241174E-04			.123699243857E-06	--.394272586162E-04
--.503765266151E-07	.07570900				
509 N	579 JE	.00004082	AMEAN	.01632378	SIGMA
152 N	152 JE	--.00211796	AMEAN	.02925557	SIGMA
.070091441643	--.303107641353E-04			.109506561549E-06	--.391140301400E-04
--.525701369006E-07	.07647400				
570 N	629 JE	.00003183	AMEAN	.01599494	SIGMA
195 N	195 JE	.00041099	AMEAN	.03493443	SIGMA
.079076168276	--.305858446441E-04			.117209879059E-06	--.370609323949E-04
--.633789232041E-07	.07723900				
182 N	204 JE	--.00006701	AMEAN	.01797914	SIGMA
94 N	94 JE	--.00157198	AMEAN	.03135920	SIGMA
.079311925241	--.320815241337E-04			.558804140712E-07	--.457126158970E-04
--.131787896224E-07	.07800300				
SPRING					
300 N	303 JE	--.00021213	AMEAN	.00930673	SIGMA
85 N	85 JE	.00157153	AMEAN	.02060211	SIGMA
.074230130565	--.298791450222E-04			.534506280813E-07	--.277019360474E-04
--.161386253839E-06	.07418000				
543 N	548 JE	.00005107	AMEAN	.00703155	SIGMA
206 N	206 JE	.00009827	AMEAN	.03336226	SIGMA
.075190085455	--.305547370120E-04			.419669367707E-07	--.341220992138E-04
--.101092077309E-06	.07494500				
487 N	496 JE	--.00008614	AMEAN	.00936743	SIGMA
164 N	164 JE	.00007403	AMEAN	.02716496	SIGMA
.076059077338	--.309897347071E-04			.382261335649E-07	--.351303490689E-04
--.969264363965E-07	.07570900				
526 N	533 JE	.00023203	AMEAN	.00942645	SIGMA
218 N	218 JE	.00054277	AMEAN	.02378035	SIGMA
.076812831882	--.314493026731E-04			.304295412045E-07	--.390781476125E-04
--.584487887916E-07	.07647400				
542 N	565 JE	.00063635	AMEAN	.01231613	SIGMA
221 N	221 JE	--.00032297	AMEAN	.02670419	SIGMA

.078348772632 --.329248708264E-04 --.965242606402E-08 --.398181269436E-04  
 --.553552965304E-07 10  
 143 N .07723900 AMEAN .01714368 SIGMA  
 51 N .00062537 AMEAN .02688810 SIGMA  
 .079480793954 --.331029840753E-04 --.228922596025E-07 --.390172357285E-04  
 --.588398704511E-07 11  
 .07800300

## SUMMER

126 N 127 JE .00023698 AMEAN .00413199 SIGMA  
 38 N 38 JE .00105025 AMEAN .01445720 SIGMA  
 .073355349458 --.292781907647E-04 --.600468763146E-07 --.289717760913E-04  
 --.154414768888E-06 .07265000 12  
 604 N 607 JE .00030155 AMEAN .00915839 SIGMA  
 216 N 216 JE .00168599 AMEAN .02121952 SIGMA  
 .074245712057 --.297030779395E-04 --.545794300023E-07 --.296797941819E-04  
 --.144049673135E-06 .07341500 13  
 547 N 548 JE .00005213 AMEAN .00795139 SIGMA  
 176 N 176 JE .00167458 AMEAN .02182120 SIGMA  
 .074593316277 --.302018333619E-04 --.438049492357E-07 --.289880035472E-04  
 --.153736994234E-06 .07418000 14  
 195 N 196 JE --.00023128 AMEAN .00884931 SIGMA  
 46 N 46 JE .00218660 AMEAN .02346876 SIGMA  
 .075704831336 --.312511926059E-04 --.307202293925E-07 --.298732976122E-04  
 --.142391587713E-06 .07494500 15

## FALL

220 N 221 JE .00037170 AMEAN .00686836 SIGMA  
 72 N 72 JE --.00053397 AMEAN .02929456 SIGMA  
 .074150371571 --.298353277870E-04 --.522245911671E-07 --.315744162615E-04  
 --.120286746520E-06 .07341500 15  
 584 N 593 JE .00029615 AMEAN .00811517 SIGMA  
 198 N 198 JE .00029319 AMEAN .01879306 SIGMA  
 .074767015987 --.303353314597E-04 --.416035915692E-07 --.322001929381E-04  
 --.114552776729E-06 .07418000 17  
 550 N 566 JE .00008180 AMEAN .01145630 SIGMA

171 N	172 JE	-.00099932	AMEAN	.03163180	SIGMA
.076526226097	-.315506128979E-04			-.328688028215E-07	-.3336927796765E-04
-.101684380686E-06	.07494500	18			
466 N	505 JE	-.00020139	AMEAN	.01887042	SIGMA
170 N	170 JE	.00052249	AMEAN	.02430470	SIGMA
.077353337800	-.318795221812E-04			-.295590629490E-07	-.382940424519E-04
-.656092084431E-07	.07570900	19			
155 N	166 JE	.00013526	AMEAN	.01594979	SIGMA
74 N	74 JE	-.00215964	AMEAN	.03295328	SIGMA
.078088812927	-.310313464471E-04			-.653790474402E-07	-.417386199789E-04
-.321056579520E-07	.07647400	20			

STATION V 12HR GMT SEASONS COMBINED

196 N	199 JE	.00014989	AMEAN	.00881123	SIGMA
52 N	52 JE	-.00130513	AMEAN	.03787252	SIGMA
.073916084886	-.299941326198E-04			-.512751042208E-07	-.326702082618E-04
-.110910166248E-06	.07265000	1			
606 N	608 JE	.00005083	AMEAN	.00553411	SIGMA
223 N	223 JE	.00145157	AMEAN	.02018565	SIGMA
.074344613703	-.299237524076E-04			-.491276302453E-07	-.306214146130E-04
-.132444009455E-06	.07341500	2			
553 N	558 JE	.00002111	AMEAN	.00915739	SIGMA
136 N	136 JE	.00145313	AMEAN	.02055577	SIGMA
.074615985705	-.300478828571E-04			-.487287328771E-07	-.287255332136E-04
-.154070808624E-06	.07418080	3			
515 N	524 JE	.00005604	AMEAN	.00934670	SIGMA
190 N	191 JE	-.00045776	AMEAN	.03998293	SIGMA
.075612658474	-.308948293335E-04			-.411247744334E-07	-.3522348123944E-04
-.897293631605E-07	.07494500	4			
502 N	541 JE	-.00005692	AMEAN	.01781205	SIGMA
154 N	154 JE	.00036173	AMEAN	.03583327	SIGMA
.076479454601	-.309778902949E-04			-.488688248723E-07	-.391820661612E-04
-.591521615776E-07	.07570900	5			
511 N	554 JE	-.00003103	AMEAN	.01597897	SIGMA
162 N	162 JE	-.00126697	AMEAN	.03087900	SIGMA
.077362991056	-.309130357396E-04			-.660007329748E-07	-.390862848781E-04

--.503331035570E-07		.07647400	5		
530 N	613 JE	.00031629	AMEAN	.01719421	SIGMA
208 N	210 JE	.00043205	AMEAN	.03064943	SIGMA
.070605242601	--.300037050470E-04		--.910561324970E-07	--.306665155905E-04	
--.526174608366E-07	.07723900	7			
230 N	250 JE	.00027643	AMEAN	.01725935	SIGMA
90 N	90 JE	--.00237092	AMEAN	.03106101	SIGMA
.079803779345	--.324015477912E-04		--.548742909066E-07	--.449476121309E-04	
--.177757622013E-07	.07000300	8			

STATION D 00HR FOUR SEASONS

WINTER

202 N	203 JE	.00017445	AMEAN	.00795148	SIGMA
55 N	55 JE	-.00137327	AMEAN	.02585585	SIGMA
.075201199460	-.290747156754E-04			-.948909371982E-07	-.491624571050E-04
.128203755981E-07	.07494500		1		
566 N	585 JE	.00032453	AMEAN	.01221101	SIGMA
250 N	250 JE	-.00095379	AMEAN	.03567010	SIGMA
.076289924511	-.302175594887E-04			-.762590474069E-07	-.499645097517E-04
.135187872263E-07	.07570900		2		
647 N	696 JE	.00005214	AMEAN	.01592157	SIGMA
209 N	214 JE	-.00079727	AMEAN	.04651559	SIGMA
.076988092343	-.297318476159E-04			-.998512339638E-07	-.456948677989E-04
-.127959762734E-07	.07647400		3		
651 N	676 JE	.00035674	AMEAN	.01337308	SIGMA
196 N	199 JE	-.00047310	AMEAN	.03863474	SIGMA
.077913812130	-.313971154573E-04			-.486401006075E-07	-.487132054156E-04
.405458322190E-08	.07723900		4		
601 N	662 JE	.00062950	AMEAN	.01782020	SIGMA
272 N	275 JE	-.00011937	AMEAN	.04359514	SIGMA
.078642416241	-.300762517468E-04			-.113385451167E-06	-.457861220678E-04
-.111375163742E-07	.07800300		5		
615 N	672 JE	.00060939	AMEAN	.01632273	SIGMA
260 N	263 JE	-.00270465	AMEAN	.04367981	SIGMA
.079821689538	-.314446922648E-04			-.857169991886E-07	-.486738593932E-04
.624845074843E-08	.07876800		6		
612 N	686 JE	.00027257	AMEAN	.01592085	SIGMA
222 N	225 JE	-.00244300	AMEAN	.03884276	SIGMA
.081422814858	-.328373602449E-04			-.559935324546E-07	-.493557037266E-04
.100500780010E-07	.07953390		7		
147 N	160 JE	.00024923	AMEAN	.01663688	SIGMA
59 N	60 JE	-.00471553	AMEAN	.03700982	SIGMA
.081991710164	-.335173208507E-04			-.364176559349E-07	-.545142973373E-04
.375759098503E-07	.08030000		8		

SPRING	697 N	705 JE	.00001026	AMEAN	.00864568	SIGMA
	262 N	263 JE	-.00019727	AMEAN	.04851942	SIGMA
	.075982188328	-.299702669149E-04		-.707753781816E-07	-.445813325599E-04	
	-.227176979176E-07	.07570900	9			
	658 N	662 JE	.00022529	AMEAN	.00779777	SIGMA
	292 N	292 JE	.00183909	AMEAN	.02846675	SIGMA
	.076497780574	-.306487884592E-04		-.472888872135E-07	-.439073634353E-04	
	-.305971782366E-07	.07647408	10			
	678 N	690 JE	.00065131	AMEAN	.01185496	SIGMA
	282 N	282 JE	.00004972	AMEAN	.03492715	SIGMA
	.077739578662	-.312147204712E-04		-.506442565393E-07	-.4774624688695E-04	
	-.187751107567E-08	.07723900	11			
	583 N	595 JE	.00073548	AMEAN	.01159167	SIGMA
	279 N	280 JE	-.00112547	AMEAN	.03196412	SIGMA
	.078398883466	-.322587317971E-04		-.225450085039E-07	-.493369079129E-04	
	.680950634553E-08	.07800300	12			
	201 N	204 JE	.00121485	AMEAN	.00875655	SIGMA
	83 N	83 JE	-.00264956	AMEAN	.02664039	SIGMA
	.0790336780259	-.329132182930E-04		-.513487590337E-06	-.520922389709E-04	
	.203057602270E-07	.07876800	13			
SUMMER	706 N	707 JE	-.00006319	AMEAN	.00550582	SIGMA
	242 N	242 JE	.00209705	AMEAN	.02516438	SIGMA
	.074969594627	-.305047860707E-04		-.406054457413E-07	-.376283418714E-04	
	-.759892016452E-07	.07418000	14			
	689 N	692 JE	.00017126	AMEAN	.00730451	SIGMA
	276 N	276 JE	.00131022	AMEAN	.02410012	SIGMA
	.075490655603	-.300823446374E-04		-.527421842881E-07	-.379863018943E-04	
	-.718087206402E-07	.07494500	15			
	667 N	673 JE	.00046256	AMEAN	.00843615	SIGMA
	234 N	234 JE	.00078373	AMEAN	.03066944	SIGMA
	.076279888693	-.306946496876E-04		-.443561733820E-07	-.397301785651E-04	
	-.578053413702E-07	.07570900	16			
	701 N	705 JE	.00044688	AMEAN	.00851868	SIGMA

270 M 270 JE .00001311 AMEAN .02920657 SIGMA  
 .077430505001 -.324678357097E-04 -.424573305965E-08 -.407746595060E-04  
 -.519912791900E-07 .07647400 17

## FALL

127 M 130 JE .00006332 AMEAN .00804976 SIGMA  
 51 M 51 JE .00042924 AMEAN .01921827 SIGMA  
 .074513790040 -.281427146752E-04 -.114849322489E-06 -.456952206212E-04  
 -.110373459210E-07 .07418000 18  
 574 M 587 JE .00009833 AMEAN .01020100 SIGMA  
 214 M 214 JE .00116902 AMEAN .04111387 SIGMA  
 .075289849626 -.293700168556E-04 -.832818361345E-07 -.415458514951E-04  
 -.426769294110E-07 .07494500 19  
 692 M 710 JE .00008485 AMEAN .00973025 SIGMA  
 219 M 219 JE .00000905 AMEAN .03748946 SIGMA  
 .076267439200 -.303959040614E-04 -.588657804061E-07 -.418084904645E-04  
 -.405929120611E-07 .07570900 20  
 665 M 686 JE .00047098 AMEAN .01222730 SIGMA  
 202 M 285 JE -.00100485 AMEAN .04031502 SIGMA  
 .077242774614 -.309923111008E-04 -.506504126904E-07 -.440222591979E-04  
 -.258058625642E-07 .07647400 21  
 685 M 696 JE .00847447 AMEAN .01093540 SIGMA  
 247 M 251 JE -.00151753 AMEAN .03649158 SIGMA  
 .078626273706 -.330010932570E-04 -.150243854752E-07 -.470429172136E-04  
 -.61621330209E-08 .07723900 22  
 463 M 490 JE .00026837 AMEAN .01474414 SIGMA  
 136 M 140 JE -.00223830 AMEAN .04534904 SIGMA  
 .079786041044 -.327418318175E-04 -.385140908387E-07 -.458347364458E-04  
 -.133804609540E-07 .07800300 23  
 232 M 237 JE .00014125 AMEAN .01103572 SIGMA  
 94 M 94 JE -.00346199 AMEAN .03080120 SIGMA  
 .081004339323 -.356381647524E-04 .403034286791E-07 -.510665115701E-04  
 .14351788132E-07 .07876800 24

STATION D 00HR GMT SEASONS COMBINED  
 102 M 102 JE .00011239 AMEAN .00724097 SIGMA

51 N	51 JE	.00124714	AMEAN	.01695610	SIGMA
.073979445476	--.302712074454E-04			--.448561089766E-07	--.379174319098E-04
--.683772625809E-07	.07341500	1			
685 N	695 JE	.00000386	AMEAN	.00924868	SIGMA
239 N	249 JE	.00068748	AMEAN	.04539054	SIGMA
.074682535858	--.297035064228E-04			--.664535440846E-07	--.396828988418E-04
--.565749764122E-07	.07418000	2			
657 N	665 JE	--.00004133	AMEAN	.00798397	SIGMA
253 N	255 JE	.00118412	AMEAN	.03500768	SIGMA
.075575819316	--.303915252036E-04			--.496792772127E-07	--.384794088793E-04
--.681120246631E-07	.07494500	3			
692 N	709 JE	.00015133	AMEAN	.00973602	SIGMA
244 N	251 JE	--.00030336	AMEAN	.04513063	SIGMA
.076223204820	--.302030861720E-04			--.612360403518E-07	--.414820141261E-04
--.437664639842E-07	.07570900	4			
702 N	723 JE	.00019145	AMEAN	.01201187	SIGMA
278 N	286 JE	--.00014462	AMEAN	.03981874	SIGMA
.077073453784	--.308710441991E-04			--.509744883712E-07	--.436832236911E-04
--.28425746426E-07	.07647400	5			
666 N	680 JE	.00043718	AMEAN	.00987463	SIGMA
264 N	264 JE	--.00084249	AMEAN	.02955455	SIGMA
.077833998787	--.316471711787E-04			--.344856485515E-07	--.495702127057E-04
.884999950345E-08	.07723900	6			
631 N	668 JE	.00047499	AMEAN	.01416375	SIGMA
263 N	272 JE	--.00229513	AMEAN	.04178764	SIGMA
.079107665996	--.320999149108E-04			--.473864353122E-07	--.482303704820E-04
.289688176300E-08	.07800300	7			
629 N	683 JE	.00059020	AMEAN	.01622123	SIGMA
251 N	255 JE	--.00239037	AMEAN	.04196134	SIGMA
.079944624730	--.324052045828E-04			--.523191868652E-07	--.491021792742E-04
.750858512163E-08	.07876200	8			
613 N	687 JE	.00051533	AMEAN	.01594820	SIGMA
239 N	245 JE	--.00194374	AMEAN	.03958906	SIGMA
.081889156758	--.328678362293E-04			--.565750788939E-07	--.493951123231E-04
.107113888380E-07	.07953300	9			
169 N	183 JE	.00027336	AMEAN	.01611873	SIGMA



60 M 61 JE --.00472267 AMEAN .03755074 SIGMA  
 .001800292213 --.336675316663E-04 --.293347044346E-07 --.551969779364E-04  
 .408634836773E-07 .00030000 10

## STATION D 12HR FOUR SEASONS

WINTER  
 245 M 252 JE .00020543 AMEAN .01075730 SIGMA  
 76 M 76 JE --.00180414 AMEAN .02240202 SIGMA  
 .075696723767 --.296927579965E-04 --.937895666281E-07 --.486743066601E-04  
 .866948688293E-08 .07494500 1  
 570 M 594 JE .00010631 AMEAN .01182782 SIGMA  
 211 M 214 JE --.00151847 AMEAN .03822676 SIGMA  
 .076045751111 --.286210650055E-04 --.127122912961E-06 --.470241082587E-04  
 --.784226828954E-09 .07570900 2  
 572 M 588 JE --.001010630 AMEAN .01281770 SIGMA  
 245 M 252 JE --.00089019 AMEAN .04387340 SIGMA  
 .077259886996 --.304970244682E-04 --.739845416645E-07 --.470384723104E-04  
 --.382941112750E-08 .07647400 3  
 610 M 652 JE .00045741 AMEAN .01577219 SIGMA  
 274 M 275 JE --.00027503 AMEAN .04282107 SIGMA  
 .077699973561 --.302034034172E-04 --.901166413743E-07 --.463424988997E-04  
 --.832498267076E-08 .07723900 4  
 599 M 657 JE .00048676 AMEAN .01607011 SIGMA  
 287 M 288 JE --.00102863 AMEAN .03846283 SIGMA  
 .078947603181 --.308109303553E-04 --.961857083851E-07 --.483569760312E-04  
 .603486340781E-08 .07800300 5  
 580 M 666 JE .00079728 AMEAN .01780286 SIGMA  
 233 M 237 JE --.00189451 AMEAN .03921588 SIGMA  
 .079682994294 --.314227117251E-04 --.837977888897E-07 --.495772900225E-04  
 .132230398180E-07 .07876800 6  
 498 M 536 JE .00058122 AMEAN .01518017 SIGMA  
 188 M 188 JE --.00322845 AMEAN .03814613 SIGMA  
 .080746972925 --.316811749629E-04 --.859430568349E-07 --.516888154792E-04  
 .239024257520E-07 .07953300 7

255 M 260 JE .00051770 AMEAN .01113911 SIGMA  
 90 M 90 JE -.00397070 AMEAN .02553950 SIGMA  
 .002405704303 -.347371900970E-04 -.466387019041E-08 -.543409476729E-04  
 .336993037232E-07 .00030000 8

SPRING

403 M 417 JE .00020360 AMEAN .01062315 SIGMA  
 189 M 192 JE -.00144051 AMEAN .04073963 SIGMA  
 .075044109371 -.208563190972E-04 -.101593040090E-06 -.440553373763E-04  
 -.161971917202E-07 .07494500 9  
 635 M 635 JE -.00002202 AMEAN .00052228 SIGMA  
 272 M 272 JE .00030354 AMEAN .03410877 SIGMA  
 .076100040134 -.298719156259E-04 -.743126936749E-07 -.458586213209E-04  
 -.12844550091E-07 .07570900 10  
 659 M 665 JE .00052909 AMEAN .00944259 SIGMA  
 315 M 317 JE .00124044 AMEAN .03320026 SIGMA  
 .076716770510 -.307249494260E-04 -.515915733920E-07 -.437925001029E-04  
 -.287519954136E-07 .07647400 11  
 663 M 675 JE .00067643 AMEAN .01022552 SIGMA  
 314 M 314 JE -.00035225 AMEAN .03555745 SIGMA  
 .077402199658 -.311805104180E-04 -.463571132521E-07 -.469000142706E-04  
 -.600255232731E-08 .07723900 12  
 639 M 651 JE .00101609 AMEAN .01230473 SIGMA  
 270 M 273 JE -.00000199 AMEAN .03253444 SIGMA  
 .078277609904 -.322321307660E-04 -.247620136957E-07 -.473306105450E-04  
 -.603320793135E-08 .07800300 13  
 251 M 264 JE .00094984 AMEAN .01218156 SIGMA  
 120 M 120 JE -.00129767 AMEAN .02919986 SIGMA  
 .079551330863 -.335096806654E-04 .941510732266E-10 -.501753848106E-04  
 .115324999073E-07 .07876000 14

SUMMER

115 M 115 JE .00010420 AMEAN .00503920 SIGMA  
 50 M 50 JE .00165030 AMEAN .02100200 SIGMA  
 .074212112946 -.298854870770E-04 -.600736758420E-07 -.377735791430E-04  
 -.711009701309E-07 .07341500 15

658 N	658 JE	.00021064	AMEAN	.00626715	SIGMA
280 N	280 JE	.00117701	AMEAN	.02372541	SIGMA
.074962523776	-.301041376707E-04	.07418000	16	-.526680054073E-07	-.392155793939E-04
-.601031392698E-07					
622 N	629 JE	.00030950	AMEAN	.00757546	SIGMA
253 N	253 JE	.00195630	AMEAN	.02831583	SIGMA
.075626273937	-.304630156589E-04	.07494500	17	-.481856923327E-07	-.372848474903E-04
-.770408044900E-07					
653 N	653 JE	.00069009	AMEAN	.00743414	SIGMA
253 N	253 JE	.00076047	AMEAN	.02047481	SIGMA
.076410184654	-.313068666525E-04	.07570900	18	-.248364145673E-07	-.391995701413E-04
-.638318044199E-07					
695 N	701 JE	.00076420	AMEAN	.00993039	SIGMA
281 N	281 JE	.00076539	AMEAN	.03112714	SIGMA
.077231803078	-.318277364320E-04	.07647400	19	-.232135557289E-07	-.405036936893E-04
-.514483283211E-07					

FALL

288 N	289 JE	.00002769	AMEAN	.00629417	SIGMA
131 N	131 JE	-.00007733	AMEAN	.03029892	SIGMA
.074702463755	-.295728962160E-04	.07418000	20	-.755680302420E-07	-.442471655223E-04
-.225039431792E-07					
601 N	611 JE	.00019601	AMEAN	.00922337	SIGMA
275 N	275 JE	.00061465	AMEAN	.03463331	SIGMA
.075623162903	-.302091588067E-04	.07494500	21	-.617721728559E-07	-.430336787028E-04
-.318498604062E-07					
619 N	625 JE	.00019251	AMEAN	.00849939	SIGMA
277 N	277 JE	.00062156	AMEAN	.03118798	SIGMA
.076096133738	-.305355209281E-04	.07570900	22	-.497897998839E-07	-.423864381247E-04
-.358914987815E-07					
616 N	637 JE	.00042148	AMEAN	.01134444	SIGMA
244 N	245 JE	.0006509	AMEAN	.03576894	SIGMA
.077308465867	-.317215272635E-04	.07647400	23	-.290137114986E-07	-.450572113957E-04
-.210260508949E-07					
581 N	599 JE	.00057282	AMEAN	.01213544	SIGMA
251 N	252 JE	-.00021597	AMEAN	.03641984	SIGMA

.070374222534 --.321306131371E-04 --.341790866952E-07 --.459166580456E-04  
 --.133059375145E-07 24  
 504 N 523 JE .07723900 AMEAN .01200552 SIGMA  
 190 N 190 JE --.00286648 AMEAN .03233828 SIGMA  
 .079450197125 --.331145560273E-04 --.156423351570E-07 --.402443095251E-04  
 .024376717580E-09 25  
 230 N 246 JE .07800300 AMEAN .01513175 SIGMA  
 73 N 73 JE .00069645 AMEAN .03973437 SIGMA  
 .080253098401 --.330941000345E-04 --.332928806894E-07 --.454886158652E-04  
 --.176261962349E-07 26  
 .07876800

STATION D 12HR GMT SEASONS COMBINED

129 N 129 JE .00020562 AMEAN .00649157 SIGMA  
 50 N 50 JE .00160527 AMEAN .02089677 SIGMA  
 .073947459705 --.297475484235E-04 --.613793362679E-07 --.379134215541E-04  
 --.700848771960E-07 1  
 645 N 645 JE .07341500 AMEAN .00797800 SIGMA  
 268 N 268 JE .00025545 AMEAN .02974363 SIGMA  
 .075037773768 --.301867328750E-04 --.544953975909E-07 --.391665897824E-04  
 --.599752474604E-07 2  
 606 N 624 JE .07410000 AMEAN .01011612 SIGMA  
 288 N 288 JE --.00010805 AMEAN .04278541 SIGMA  
 .075794907465 --.304581834864E-04 --.579937745210E-07 --.401044632266E-04  
 --.533733600017E-07 3  
 603 N 611 JE .07494500 AMEAN .01114166 SIGMA  
 252 N 260 JE .00033465 AMEAN .04261765 SIGMA  
 .076431893417 --.308604202217E-04 --.452009365738E-07 --.425419486363E-04  
 --.358610591715E-07 4  
 627 N 643 JE .07570900 AMEAN .00999630 SIGMA  
 275 N 275 JE .00065522 AMEAN .03442630 SIGMA  
 .076833579646 --.311245839960E-04 --.407364048835E-07 --.43866086520E-04  
 --.277739740326E-07 5  
 629 N 640 JE .07647400 AMEAN .01204562 SIGMA  
 299 N 301 JE .00043754 AMEAN .04127314 SIGMA  
 .077647641755 --.310449587155E-04 --.525758297977E-07 --.463573941307E-04  
 --.115294993614E-07 6  
 .07723900

611 N	659 JE	.00056601	AMEAN	.01533323	SIGMA
262 N	265 JE	-.00229007	AMEAN	.04311119	SIGMA
.078632795282	-.309978824237E-04		-.799679745070E-07	-.470567255843E-04	
.882893395758E-09	.07800300		7		
579 N	660 JE	.00079341	AMEAN	.01832358	SIGMA
237 N	241 JE	-.00182545	AMEAN	.04138472	SIGMA
.079667559885	-.317473686701E-04		-.691300877585E-07	-.480452745885E-04	
.528108716149E-08	.07876800		8		
557 N	606 JE	.00067609	AMEAN	.01593925	SIGMA
209 N	216 JE	-.00195685	AMEAN	.04470457	SIGMA
.080841350228	-.321567148268E-04		-.734357462963E-07	-.405759732423E-04	
.578107126228E-08	.07953300		9		
316 N	324 JE	.00064744	AMEAN	.01164233	SIGMA
128 N	128 JE	-.00384582	AMEAN	.02470010	SIGMA
.082178321242	-.344272633121E-04		-.1171602035563E-07	-.545775692865E-04	
.373347423114E-07	.08030000		10		

STATION N 00HR FOUR SEASONS

WINTER

345 N	354 JE	.00046784	AMEAN	.01277273	SIGMA
100 N	100 JE	.00035050	AMEAN	.03305866	SIGMA
.074932573411	-.209664839751E-04		AMEAN	-.907062614042E-07	-.401320092619E-04
-.432496420354E-07	.07410000		1		
404 N	424 JE	.00093351	AMEAN	.01350650	SIGMA
130 N	130 JE	.00033612	AMEAN	.03230926	SIGMA
.075821804059	-.304773527736E-04		AMEAN	-.549714751728E-07	-.371139256056E-04
-.695240263965E-07	.07494500		2		
529 N	544 JE	.00064400	AMEAN	.01022277	SIGMA
214 N	214 JE	-.00094971	AMEAN	.02771327	SIGMA
.076774683103	-.310458698615E-04		AMEAN	-.402242185578E-07	-.411085015938E-04
-.408129281402E-07	.07570900		3		
476 N	488 JE	.00048655	AMEAN	.01159683	SIGMA
207 N	207 JE	-.00191957	AMEAN	.02523630	SIGMA
.077507358099	-.310505861373E-04		AMEAN	-.425443860768E-07	-.457557943174E-04
-.119070622443E-07	.07647400		4		
257 N	260 JE	.00018189	AMEAN	.01061343	SIGMA
115 N	115 JE	-.00035825	AMEAN	.02473042	SIGMA
.077929503260	-.306917238119E-04		AMEAN	-.559683519077E-07	-.451326136383E-04
-.149642714959E-07	.07723900		5		

SPRING

76 N	76 JE	.00035731	AMEAN	.00561433	SIGMA
36 N	36 JE	.00142004	AMEAN	.02450052	SIGMA
.075654815018	-.315169202752E-04		AMEAN	-.172611994834E-07	-.360314804333E-04
-.670703099174E-07	.07410000		6		
391 N	395 JE	.08114896	AMEAN	.00933454	SIGMA
159 N	159 JE	.00062977	AMEAN	.02508924	SIGMA
.075707743701	-.308288027213E-04		AMEAN	-.324142943320E-07	-.367173603616E-04
-.811608589937E-07	.07494500		7		
415 N	417 JE	.00107964	AMEAN	.00790353	SIGMA
190 N	191 JE	.00168097	AMEAN	.02531245	SIGMA
.076538955003	-.320358221826E-04		AMEAN	-.571234535200E-06	-.395916039285E-04

--.587602122498E-07 .07570900 8  
 473 N 477 JE .00062862 AMEAN .00965470 SIGMA  
 216 N 216 JE .00071256 AMEAN .02587751 SIGMA  
 .077975240090 --.332043337042E-04 .141194064881E-07 --.414036835365E-04  
 --.479817391152E-07 .07647400 9

SUMMER  
 86 N 86 JE .00050511 AMEAN .00697220 SIGMA  
 38 N 38 JE --.00013753 AMEAN .01937327 SIGMA  
 .075535259549 --.309685695473E-04 --.306198727746E-07 --.366148693386E-04  
 --.77711141469E-07 .07341500 10  
 499 N 500 JE .00065237 AMEAN .00881852 SIGMA  
 210 N 210 JE --.00036426 AMEAN .01657734 SIGMA  
 .075730182801 --.316902020105E-04 --.661927279529E-08 --.373989493867E-04  
 --.732340776367E-07 .07418000 11  
 509 N 512 JE .00067512 AMEAN .00786210 SIGMA  
 225 N 225 JE .00033057 AMEAN .01636805 SIGMA  
 .076026825917 --.321332465206E-04 .221925538649E-08 --.372119981242E-04  
 --.742153084865E-07 .07494500 12  
 79 N 80 JE .00076989 AMEAN .00995070 SIGMA  
 47 N 47 JE .00050203 AMEAN .01360942 SIGMA  
 .076855794453 --.327921631762E-04 .127480820621E-07 --.362235526017E-04  
 --.833916604657E-07 .07570900 13

FALL  
 509 N 517 JE .00090886 AMEAN .01095847 SIGMA  
 205 N 205 JE --.00020505 AMEAN .02194951 SIGMA  
 .075320852767 --.301301961779E-04 --.534707210572E-07 --.378152118514E-04  
 --.67444076983E-07 .07418000 14  
 509 N 514 JE .00053165 AMEAN .00785829 SIGMA  
 244 N 244 JE .0007612 AMEAN .01868371 SIGMA  
 .076184221139 --.316049427799E-04 --.134210731908E-07 --.384000143882E-04  
 --.656956906729E-07 .07494500 15  
 514 N 517 JE .00054794 AMEAN .00849138 SIGMA  
 207 N 207 JE .00034522 AMEAN .01802577 SIGMA  
 .077141286508 --.324277190137E-04 .211285060479E-08 --.382398588320E-04

--.702552948529E-07      .07570900      16  
 298 N      301 JE      .00053115 AMEAN      .01060601 SIGMA  
 114 N      110 JE      -.00302350 AMEAN      .03117406 SIGMA  
 .077979441775      -.329076317293E-04      .003854016458E-08      -.419353872145E-04  
 --.410690823436E-07      .07647400      17

## STATION N 00HR GMT SEASONS COMBINED

193 N      196 JE      .00059901 AMEAN      .00770411 SIGMA  
 81 N      81 JE      .00140063 AMEAN      .02737500 SIGMA  
 .074772745343      -.292840188176E-04      -.769555847219E-07      -.357981841708E-04  
 --.843081358996E-07      .07341500      1  
 505 N      508 JE      .00077450 AMEAN      .01012429 SIGMA  
 225 N      225 JE      .00080690 AMEAN      .02065777 SIGMA  
 .075441973594      -.309651835058E-04      -.269140521320E-07      -.371015521651E-04  
 --.755086937952E-07      .07418000      2  
 457 N      463 JE      .00072367 AMEAN      .01157901 SIGMA  
 203 N      203 JE      -.00080806 AMEAN      .02272181 SIGMA  
 .076083585197      -.316479053785E-04      -.148231771513E-07      -.369145902227E-04  
 --.758774223599E-07      .07494500      3  
 471 N      478 JE      .00056307 AMEAN      .00863241 SIGMA  
 201 N      201 JE      .00060300 AMEAN      .02609989 SIGMA  
 .077107991364      -.322352124808E-04      -.573989527846E-08      -.384291371919E-04  
 --.600784656505E-07      .07570900      4  
 494 N      501 JE      .00060673 AMEAN      .01046365 SIGMA  
 220 N      220 JE      -.00065669 AMEAN      .03168519 SIGMA  
 .077608343235      -.319793465455E-04      -.164267239312E-07      -.429934349899E-04  
 --.335113692327E-07      .07647400      5  
 450 N      455 JE      .00026036 AMEAN      .01066228 SIGMA  
 189 N      190 JE      -.00045643 AMEAN      .02525807 SIGMA  
 .078143248904      -.311601577852E-04      -.425103792811E-07      -.467613205198E-04  
 --.485214530445E-08      .07723900      6

## STATION N 12HR FOUR SEASONS

WINTER



253 N	266 JE	.00012515	AMEAN	.01324440	SIGMA
52 N	52 JE	-.00050380	AMEAN	.02652525	SIGMA
.074842185239	-.278788340118E-04			-.127590352902E-06	-.374373158199E-04
-.667674470411E-07	.07418000		1		
434 N	441 JE	.00124579	AMEAN	.01613937	SIGMA
142 N	142 JE	-.00208673	AMEAN	.03966920	SIGMA
.075929740824	-.303605365228E-04			-.520655392390E-07	-.412316993071E-04
-.405054530282E-07	.07494500		2		
545 N	556 JE	.00038929	AMEAN	.01130152	SIGMA
186 N	186 JE	-.00034443	AMEAN	.02644061	SIGMA
.076768432217	-.312141380307E-04			-.357895097081E-07	-.411699824997E-04
-.426223401289E-07	.07570900		3		
562 N	573 JE	.00039599	AMEAN	.01016334	SIGMA
195 N	195 JE	-.00111202	AMEAN	.02230670	SIGMA
.077734520967	-.321811291935E-04			-.104199289985E-07	-.432945122233E-04
-.301424653271E-07	.07647400		4		
538 N	553 JE	.00019871	AMEAN	.01149774	SIGMA
209 N	209 JE	-.00150558	AMEAN	.02524695	SIGMA
.078569654683	-.316913278125E-04			-.329570634335E-07	-.480361450707E-04
.363203426825E-08	.07723900		5		

SPRING

435 N	432 JE	.00053366	AMEAN	.00516552	SIGMA
171 N	171 JE	.00134851	AMEAN	.02353535	SIGMA
.075847480322	-.312871613980E-04			-.193255695740E-07	-.368794128407E-04
-.810753583840E-07	.07494500		6		
467 N	476 JE	.00075289	AMEAN	.01078124	SIGMA
168 N	168 JE	.00090877	AMEAN	.02761551	SIGMA
.076122678564	-.313609283261E-04			-.170844941807E-07	-.372978468853E-04
-.813955281313E-07	.07570900		7		
541 N	545 JE	.00035642	AMEAN	.00822514	SIGMA
221 N	221 JE	.00055497	AMEAN	.02292963	SIGMA
.077569058569	-.321888135725E-04			-.102805036195E-07	-.419140461907E-04
-.420062806457E-07	.07647400		8		
45 N	45 JE	.0002663	AMEAN	.00757987	SIGMA
21 N	21 JE	-.00016645	AMEAN	.01187628	SIGMA

.079058291264 --.337326096006E-04 .203471861346E-07 --.456574546014E-04  
 --.154134699482E-07 .07723900 9

## SUMMER

531 N 532 JE .00034984 AMEAN .00600680 SIGMA  
 199 N 199 JE .00022131 AMEAN .01758167 SIGMA  
 .075195491347 --.308811208996E-04 --.245752448530E-07 --.357351490862E-04  
 --.078270900551E-07 .07418000 10  
 595 N 597 JE .00042195 AMEAN .00828590 SIGMA  
 237 N 237 JE --.00056185 AMEAN .02051213 SIGMA  
 .076142060438 --.318526175551E-04 --.778746183145E-08 --.373945922702E-04  
 --.721054863622E-07 .07494500 11  
 263 N 264 JE .00038331 AMEAN .00907915 SIGMA  
 114 N 114 JE .00061448 AMEAN .01597999 SIGMA  
 .076938962304 --.329374171815E-04 .169217378851E-07 --.373712659850E-04  
 --.766033659373E-07 .07570900 12

## FALL

521 N 527 JE .00028236 AMEAN .00789974 SIGMA  
 187 N 187 JE --.00028816 AMEAN .02351643 SIGMA  
 .075515245795 --.308091972139E-04 --.339832387851E-07 --.372551586503E-04  
 --.751815191809E-07 .07418000 13  
 580 N 587 JE .00029775 AMEAN .00934841 SIGMA  
 242 N 242 JE --.00035018 AMEAN .02670535 SIGMA  
 .075918521053 --.308154681982E-04 --.344195581842E-07 --.381333862908E-04  
 --.674910099363E-07 .07494500 14  
 591 N 595 JE .00026909 AMEAN .00843854 SIGMA  
 239 N 239 JE --.00012962 AMEAN .02988190 SIGMA  
 .077219041680 --.321229246281E-04 --.775475155999E-08 --.485588803617E-04  
 --.546451515696E-07 .07570900 15  
 483 N 493 JE .00053540 AMEAN .01018878 SIGMA  
 234 N 234 JE --.00102617 AMEAN .02268718 SIGMA  
 .077841688354 --.324190161673E-04 --.256857871999E-08 --.420993310119E-04  
 --.413863499833E-07 .07647400 16

STATION N 12HR GMT SEASONS COMBINED

538 N	542 JE	.00024575	AMEAN	.00751044	SIGMA
200 N	200 JE	.00028534	AMEAN	.02154154	SIGMA
.075289761035	-.307229523672E-04			-.323276086511E-07	-.364432945210E-04
-.816138323838E-07	.07418000		1		
558 N	560 JE	.00019904	AMEAN	.00798989	SIGMA
198 N	200 JE	-.00078250	AMEAN	.02750753	SIGMA
.076029127723	-.314262046169E-04			-.157347485333E-07	-.384523685198E-04
-.663887198135E-07	.07494500		2		
482 N	486 JE	.00026024	AMEAN	.01039125	SIGMA
153 N	153 JE	.00018145	AMEAN	.02647167	SIGMA
.076604744956	-.315083080805E-04			-.203766372661E-07	-.385194270053E-04
-.696603225845E-07	.07570900		3		
569 N	575 JE	.00034650	AMEAN	.00989138	SIGMA
213 N	213 JE	.00000030	AMEAN	.02258485	SIGMA
.077768282888	-.325445363147E-04			-.877500014765E-09	-.432113049894E-04
-.328195805065E-07	.07647400		4		
362 N	367 JE	.00028249	AMEAN	.01064500	SIGMA
149 N	149 JE	-.00019117	AMEAN	.02104073	SIGMA
.078691408977	-.325574661978E-04			-.855772750355E-08	-.462939688556E-04
-.115366800166E-07	.07723900		5		

## STATION C 00HR FOUR SEASONS

WINTER

116 N	141 JE	.00126952	AMEAN	.02177890	SIGMA
57 N	62 JE	.00211216	AMEAN	.06277720	SIGMA
.075360925297	-.275572222504E-04		-.200713475929E-06	-.413516053863E-04	
-.372740240722E-07	.07494500				
171 N	190 JE	.00051293	AMEAN	.01524810	SIGMA
59 N	59 JE	-.00331024	AMEAN	.01910416	SIGMA
.074775334714	-.258155391981E-04		-.240502058860E-06	-.489006589924E-04	
.138082095314E-07	.07570900				
581 N	616 JE	-.00012704	AMEAN	.01454856	SIGMA
192 N	196 JE	-.00400198	AMEAN	.04031813	SIGMA
.075971117835	-.287312048184E-04		-.135673319214E-06	-.504574631009E-04	
.168030006980E-07	.07647400				
546 N	595 JE	.00027232	AMEAN	.01748873	SIGMA
218 N	220 JE	-.01622203	AMEAN	.04316938	SIGMA
.077106645223	-.295541198246E-04		-.123883678984E-06	-.504891189695E-04	
.157795253951E-07	.07723900				
536 N	604 JE	-.00010520	AMEAN	.01915953	SIGMA
172 N	179 JE	-.00318761	AMEAN	.05272502	SIGMA
.077914884648	-.290628183349E-04		-.149349665417E-06	-.498378099807E-04	
.140946495443E-07	.07800300				
473 N	545 JE	.00053707	AMEAN	.01938740	SIGMA
177 N	178 JE	-.00206350	AMEAN	.03916397	SIGMA
.078874009513	-.297979857503E-04		-.138828377576E-06	-.478867214484E-04	
.214294550984E-08	.07876800				
536 N	597 JE	.00016121	AMEAN	.01745227	SIGMA
202 N	208 JE	-.00058131	AMEAN	.04297706	SIGMA
.080176842168	-.312679640321E-04		-.103212535187E-06	-.491983789699E-04	
.661117577379E-08	.07953300				
544 N	580 JE	.00057462	AMEAN	.01424153	SIGMA
183 N	185 JE	-.00210043	AMEAN	.04214261	SIGMA
.081540630907	-.330672711686E-04		-.513902999155E-07	-.512787023508E-04	
.153135889295E-07	.08030000				

SPRING									
112 N	119 JE	.00015274	AMEAN	.01263836	SIGMA				
40 N	40 JE	-.00262858	AMEAN	.01634909	SIGMA				
.075049432207	-.264739645731E-04	.07570908	9	-.217119525372E-06	-.461637525465E-04				
.615762891060E-08									
397 N	431 JE	.00013706	AMEAN	.01602730	SIGMA				
133 N	133 JE	-.00147809	AMEAN	.03584016	SIGMA				
.076532932459	-.297199788035E-04	.07647480	10	-.111711889434E-06	-.493093917482E-04				
.151704953332E-07									
520 N	557 JE	-.00044136	AMEAN	.01383060	SIGMA				
190 N	190 JE	-.00108500	AMEAN	.03423068	SIGMA				
.076932020242	-.299919591061E-04	.07723900	11	-.100326256716E-06	-.487317160567E-04				
.115813422709E-07									
611 N	643 JE	-.00000036	AMEAN	.01453319	SIGMA				
238 N	238 JE	-.00040533	AMEAN	.03649474	SIGMA				
.077550899087	-.314226748153E-04	.07806300	12	-.554447515007E-07	-.483063381137E-04				
.336085104320E-08									
573 N	597 JE	.00041183	AMEAN	.01498374	SIGMA				
198 N	201 JE	-.00079198	AMEAN	.02786059	SIGMA				
.078348449460	-.313220122889E-04	.07876800	13	-.598990495202E-07	-.502270348586E-04				
.151819968970E-07									
467 N	535 JE	.00091901	AMEAN	.01749101	SIGMA				
160 N	168 JE	-.00100238	AMEAN	.02964265	SIGMA				
.080199647439	-.322069546225E-04	.07953300	14	-.715872135145E-07	-.489754574673E-04				
.856678871500E-08									
348 N	375 JE	.00060149	AMEAN	.01559159	SIGMA				
113 N	115 JE	-.00208809	AMEAN	.03854776	SIGMA				
.080508429643	-.320822596816E-04	.08030000	15	-.408991403385E-07	-.522967915027E-04				
.204746085702E-07									
SUMMER									
469 N	491 JE	.00021151	AMEAN	.01227337	SIGMA				
160 N	160 JE	-.00131275	AMEAN	.02710242	SIGMA				
.075144901493	-.289405409807E-04	.07570900	16	-.114335727585E-06	-.456971494182E-04				
-.395641637973E-08									
679 N	698 JE	.00012914	AMEAN	.01048297	SIGMA				

226 N 226 JE --.00142879 AMEAN .02710947 SIGMA  
 .076047852727 --.301548811847E-04 --.754052536408E-07 --.472749372994E-04  
 .222060792569E-08 .07647400 17  
 592 N 621 JE .00000582 AMEAN .01477847 SIGMA  
 170 N 171 JE .00030270 AMEAN .03842247 SIGMA  
 .077100334883 --.312494979834E-04 --.574327406769E-07 --.451418862102E-04  
 --.167388992987E-07 .07723980 18  
 647 N 665 JE .00062791 AMEAN .01318128 SIGMA  
 214 N 214 JE --.00040739 AMEAN .03364658 SIGMA  
 .077384929601 --.314225907145E-04 --.472152672564E-07 --.430918978062E-04  
 --.302638638547E-07 .07800308 19  
 412 N 437 JE .00077457 AMEAN .01227418 SIGMA  
 163 N 163 JE --.00055841 AMEAN .03165494 SIGMA  
 .077785490101 --.321807373466E-04 --.268095111126E-07 --.437323282191E-04  
 --.286243545441E-07 .07876888 20

# FALL

159 N 167 JE .00025371 AMEAN .01244965 SIGMA  
 52 N 52 JE --.00246044 AMEAN .01574213 SIGMA  
 .074051425143 --.264080134963E-04 --.195214059218E-06 --.475888686654E-04  
 .110569676827E-07 .07494500 21  
 126 N 141 JE .00037929 AMEAN .01574286 SIGMA  
 52 N 52 JE --.00088878 AMEAN .02932760 SIGMA  
 .075236226109 --.276078246712E-04 --.170896331347E-06 --.476351778662E-04  
 .570707349095E-08 .07578988 22  
 622 N 665 JE .00008284 AMEAN .01518229 SIGMA  
 216 N 217 JE .00004649 AMEAN .03958908 SIGMA  
 .076114733102 --.288795964964E-04 --.130772678029E-06 --.431955709789E-04  
 --.251010716276E-07 .07647400 23  
 621 N 659 JE .00012373 AMEAN .01386572 SIGMA  
 221 N 221 JE --.00193252 AMEAN .03029742 SIGMA  
 .077152817523 --.304548724495E-04 --.846158711023E-07 --.492155122474E-04  
 .964118941603E-08 .07723980 24  
 601 N 661 JE .00025035 AMEAN .01725350 SIGMA  
 230 N 234 JE .00061092 AMEAN .04435176 SIGMA  
 .078161830693 --.305443726102E-04 --.982396884887E-07 --.438857829728E-04

--.236392904457E-07	.07800380	25							
629 N	680 JE	AMEAN						.01528576	SIGMA
205 N	205 JE	AMEAN						.04469303	SIGMA
.079444944914	--.316569706641E-04	--.724893923213E-07						--.489495564258E-04	
.75965530984E-08	.07876800	26							
570 N	598 JE	AMEAN						.01426663	SIGMA
176 N	176 JE	AMEAN						.03852541	SIGMA
.000349887916	--.334878249907E-04	--.204264573137E-07						--.48794988835E-04	
.227369269087E-08	.07953300	27							
STATION C 00MR GMT SEASONS COMBINED									
241 N	278 JE	AMEAN						.01919266	SIGMA
105 N	106 JE	AMEAN						.05060921	SIGMA
.074042283265	--.277239381386E-04	--.172601591504E-06						--.469218243608E-04	
.178077968485E-08	.07494500	1							
542 N	602 JE	AMEAN						.01577089	SIGMA
209 N	212 JE	AMEAN						.04477083	SIGMA
.075196358816	--.279315360067E-04	--.139439236787E-06						--.449826084170E-04	
.029075927716E-08	.07570900	2							
661 N	698 JE	AMEAN						.01496071	SIGMA
232 N	234 JE	AMEAN						.03241584	SIGMA
.075987225441	--.296563753482E-04	--.970172631318E-07						--.456377518538E-04	
.671588990091E-08	.07647400	3							
584 N	624 JE	AMEAN						.01648565	SIGMA
181 N	189 JE	AMEAN						.05331415	SIGMA
.077000062284	--.301489912137E-04	--.947070406343E-07						--.466026949549E-04	
.542557404957E-08	.07723900	4							
641 N	687 JE	AMEAN						.01683484	SIGMA
212 N	215 JE	AMEAN						.04486199	SIGMA
.078104612716	--.315760618925E-04	--.528216917681E-07						--.466756313567E-04	
.391824812570E-08	.07800300	5							
618 N	679 JE	AMEAN						.01522870	SIGMA
230 N	239 JE	AMEAN						.04240741	SIGMA
.078587864990	--.316645158143E-04	--.559654636406E-07						--.478246143359E-04	
.163746659431E-08	.07876800	5							
511 N	579 JE	AMEAN						.01817861	SIGMA

178 N 187 JE --.00165116 AMEAN .04670829 SIGMA  
 .080096709270 -.327360963074E-04 -.4990081A6073E-07 -.407423622906E-04  
 .453306587395E-08 .07953300 7  
 567 N 603 JE .00062077 AMEAN .01537770 SIGMA  
 199 N 201 JE -.00270503 AMEAN .04040811 SIGMA  
 .080922328601 -.330978026930E-04 -.305322167309E-07 -.521727000000E-04  
 .191537477098E-07 .00030000 8

# STATION C 12HR FOUR SEASONS

WINTER  
 80 N 82 JE .00134301 AMEAN .01134504 SIGMA  
 30 N 30 JE .00095520 AMEAN .00706741 SIGMA  
 .073710830266 -.228346300486E-04 -.356642813504E-06 -.436358975351E-04  
 -.366736136159E-08 .07494500 1  
 86 N 95 JE .00035411 AMEAN .01629710 SIGMA  
 16 N 16 JE -.00677772 AMEAN .02167341 SIGMA  
 .075313240159 -.255896664690E-04 -.261199629377E-06 -.544099852939E-04  
 .497229030730E-07 .07570900 2  
 435 N 491 JE .00025563 AMEAN .01800248 SIGMA  
 180 N 181 JE .00067104 AMEAN .04074680 SIGMA  
 .076252243737 -.276656681083E-04 -.193180943720E-06 -.470060522977E-04  
 -.344016191205E-09 .07647400 3  
 555 N 610 JE -.00021973 AMEAN .01606956 SIGMA  
 201 N 202 JE -.00190853 AMEAN .04170670 SIGMA  
 .076997300009 -.296754468676E-04 -.117550015200E-06 -.400604597396E-04  
 .107464264562E-07 .07723900 4  
 505 N 557 JE .00003111 AMEAN .02221290 SIGMA  
 198 N 202 JE -.00062715 AMEAN .04964564 SIGMA  
 .078127126125 -.300672933800E-04 -.116072607540E-06 -.400420022374E-04  
 .624477074092E-08 .07800300 5  
 524 N 581 JE .00016652 AMEAN .01024548 SIGMA  
 171 N 181 JE -.00102017 AMEAN .04403108 SIGMA  
 .078030334584 -.304322137129E-04 -.100017602351E-06 -.490529138647E-04  
 .355767448199E-08 .07876800 6



509 N 579 JE .00023797 AMEAN .01025127 SIGMA  
 198 N 201 JE -.00193491 AMEAN .04040026 SIGMA  
 .080026425065 -.314015657689E-04  
 .158253550920E-07 .07953300 7  
 462 N 507 JE .00044219 AMEAN .01505672 SIGMA  
 188 N 193 JE -.00514461 AMEAN .04184472 SIGMA  
 .081564556731 -.345650743688E-04  
 .348177951998E-07 .08030000 8  
 248 N 300 JE .00054457 AMEAN .02000038 SIGMA  
 102 N 103 JE .00002256 AMEAN .04183130 SIGMA  
 .082406667024 -.332052043176E-04  
 .990922803992E-08 .08106200 9

## SPRING

301 N 318 JE .00021295 AMEAN .01312645 SIGMA  
 100 N 101 JE -.00399661 AMEAN .02888628 SIGMA  
 .076139446930 -.290719417376E-04  
 .177910747801E-07 .07647400 10  
 466 N 512 JE -.0007597 AMEAN .01625396 SIGMA  
 215 N 215 JE .00030544 AMEAN .03645622 SIGMA  
 .076796243733 -.303097511508E-04  
 .303262689850E-08 .07723900 11  
 432 N 465 JE .00070738 AMEAN .01670197 SIGMA  
 172 N 173 JE -.00307566 AMEAN .03916070 SIGMA  
 .077609601382 -.303358690007E-04  
 .169009328774E-07 .07800300 12  
 587 N 614 JE .00045419 AMEAN .01463366 SIGMA  
 201 N 202 JE -.00182689 AMEAN .03157577 SIGMA  
 .078803975761 -.317247663821E-04  
 .180347218276E-07 .07876800 13  
 539 N 569 JE .00051507 AMEAN .01421517 SIGMA  
 223 N 223 JE -.00287111 AMEAN .03516092 SIGMA  
 .080244267007 -.330443121277E-04  
 .210546766941E-07 .07953300 14  
 375 N 423 JE .00079344 AMEAN .01703104 SIGMA  
 178 N 178 JE .00061106 AMEAN .02692804 SIGMA

.080623726684 --.326331959913E-04 --.538423372070E-07 --.493483936595E-04  
 .939045747715E-08 .38030000 15

## SUMMER

355 N 373 JE --.00004070 AMEAN .01342809 SIGMA  
 133 N 133 JE --.00132252 AMEAN .03320106 SIGMA  
 .075130339656 --.29013303429E-04 --.112139295423E-06 --.452178922265E-04  
 --.769563380559E-08 .07570900 16  
 595 N 605 JE --.00005210 AMEAN .01126172 SIGMA  
 246 N 247 JE --.0037549 AMEAN .03526878 SIGMA  
 .076092496624 --.304555925747E-04 --.706356968813E-07 --.452472080410E-04  
 --.105488633346E-07 .07647400 17  
 526 N 556 JE --.00012696 AMEAN .01330268 SIGMA  
 208 N 208 JE .00074210 AMEAN .03680023 SIGMA  
 .076796692980 --.314243847545E-04 --.438332611923E-07 --.427053419662E-04  
 --.335411697701E-07 .07723900 18  
 593 N 615 JE .00018075 AMEAN .01192169 SIGMA  
 214 N 217 JE --.00254871 AMEAN .03748987 SIGMA  
 .078824874917 --.321760576239E-04 --.333785297614E-07 --.470653046258E-04  
 --.259236554952E-08 .07800400 19  
 326 N 352 JE .00209961 AMEAN .01280475 SIGMA  
 150 N 150 JE --.00024834 AMEAN .02887523 SIGMA  
 .077839369956 --.323533648650E-04 --.235594993941E-07 --.450320023136E-04  
 --.160776775489E-07 .07876800 20

## FALL

91 N 95 JE .00023884 AMEAN .01072141 SIGMA  
 8 N 8 JE --.00577191 AMEAN .03899301 SIGMA  
 .074822179924 --.285948341695E-04 --.134221747253E-06 --.526137260707E-04  
 .339944892122E-07 .07494500 21  
 240 N 254 JE .00009585 AMEAN .01303679 SIGMA  
 80 N 81 JE --.00157849 AMEAN .03842507 SIGMA  
 .075341895531 --.282316684595E-04 --.148372222206E-06 --.478050503915E-04  
 .122672991922E-07 .07570900 22  
 609 N 667 JE --.00011848 AMEAN .01724950 SIGMA  
 253 N 253 JE --.00082682 AMEAN .03643744 SIGMA

.076114410248	--.296093170327E-04	--.103369417468E-06	--.472212404955E-04
--.452156102704E-09	.07647400	23	
641 N	693 JE	AMEAN	.01576146 SIGMA
234 N	248 JE	AMEAN	.05140103 SIGMA
.077254028385	--.301630756097E-04	--.996926969734E-07	--.445653'64658E-04
--.164632400067E-07	.07723900	24	
585 N	632 JE	AMEAN	.01508314 SIGMA
215 N	220 JE	AMEAN	.04574497 SIGMA
.078267436987	--.310176646715E-04	--.784668460403E-07	--.488185339044E-04
.982118832183E-08	.07800300	25	
598 N	625 JE	AMEAN	.01390782 SIGMA
234 N	237 JE	AMEAN	.04656462 SIGMA
.079354746731	--.326738597128E-04	--.385244129582E-07	--.471460913078E-04
--.637494363270E-08	.07876800	26	
493 N	562 JE	AMEAN	.01687016 SIGMA
193 N	194 JE	AMEAN	.04464628 SIGMA
.080686454931	--.335045549947E-04	--.299049815553E-07	--.507972961023E-04
.150010379997E-07	.07953300	27	
STATION C 12HR SEAPONS COMBINED			
163 N	185 JE	AMEAN	.01990139 SIGMA
39 N	43 JE	AMEAN	.06377341 SIGMA
.074132127585	--.261809486929E-04	--.217797523168E-06	--.453675680083E-04
--.450423881798E-08	.07494500	1	
507 N	540 JE	AMEAN	.01514852 SIGMA
166 N	172 JE	AMEAN	.04653447 SIGMA
.075358915305	--.284656154898E-04	--.139066016458E-06	--.462685745843E-04
--.645572242094E-09	.07570900	2	
587 N	624 JE	AMEAN	.01661918 SIGMA
225 N	233 JE	AMEAN	.04869516 SIGMA
.076271591388	--.305183898072E-04	--.754774798930E-07	--.459876125065E-04
--.511324646356E-08	.07647400	3	
540 N	564 JE	AMEAN	.01371726 SIGMA
193 N	199 JE	AMEAN	.04790721 SIGMA
.076979459084	--.308788279965E-04	--.673526331249E-07	--.427948518739E-04
--.328083986666E-07	.07723900	4	

516 M	536 JE	--.00013569	AMEAN	.01543790	SIGMA
183 M	187 JE	--.00199122	AMEAN	.04531566	SIGMA
.077486628838	--.308534920123E-04	--.676901069213E-07		--.473520275576E-04	
--.104028983355E-09	.07800300	5			
586 N	620 JE	.00035943	AMEAN	.01491915	SIGMA
228 M	228 JE	--.00116632	AMEAN	.04044945	SIGMA
.079059615607	--.320533910711E-04	--.586325706788E-07		--.484418142981E-04	
.421052420233E-08	.07876000	6			
538 M	589 JE	.00043485	AMEAN	.01567976	SIGMA
225 M	226 JE	--.00274972	AMEAN	.03937568	SIGMA
.080582865266	--.336062385385E-04	--.296460825201E-07		--.512731628622E-04	
.164357581508E-07	.07953380	7			
560 N	589 JE	.00086630	AMEAN	.01236586	SIGMA
260 N	260 JE	--.00322612	AMEAN	.03194724	SIGMA
.081189039600	--.344179522903E-04	--.163738061022E-08		--.540332986874E-04	
.308686457900E-07	.08030000	8			
299 N	342 JE	.00043411	AMEAN	.01869886	SIGMA
100 M	102 JE	--.00096213	AMEAN	.04136389	SIGMA
.082547643058	--.339103645200E-04	--.422930034466E-07		--.513851322245E-04	
.189108876961E-07	.08106200	9			

TR 82-81

APPENDIX D

DENSITY RATIO PROFILES FROM STATION E

## DENSITY RATIO PROFILES FOR STATION E

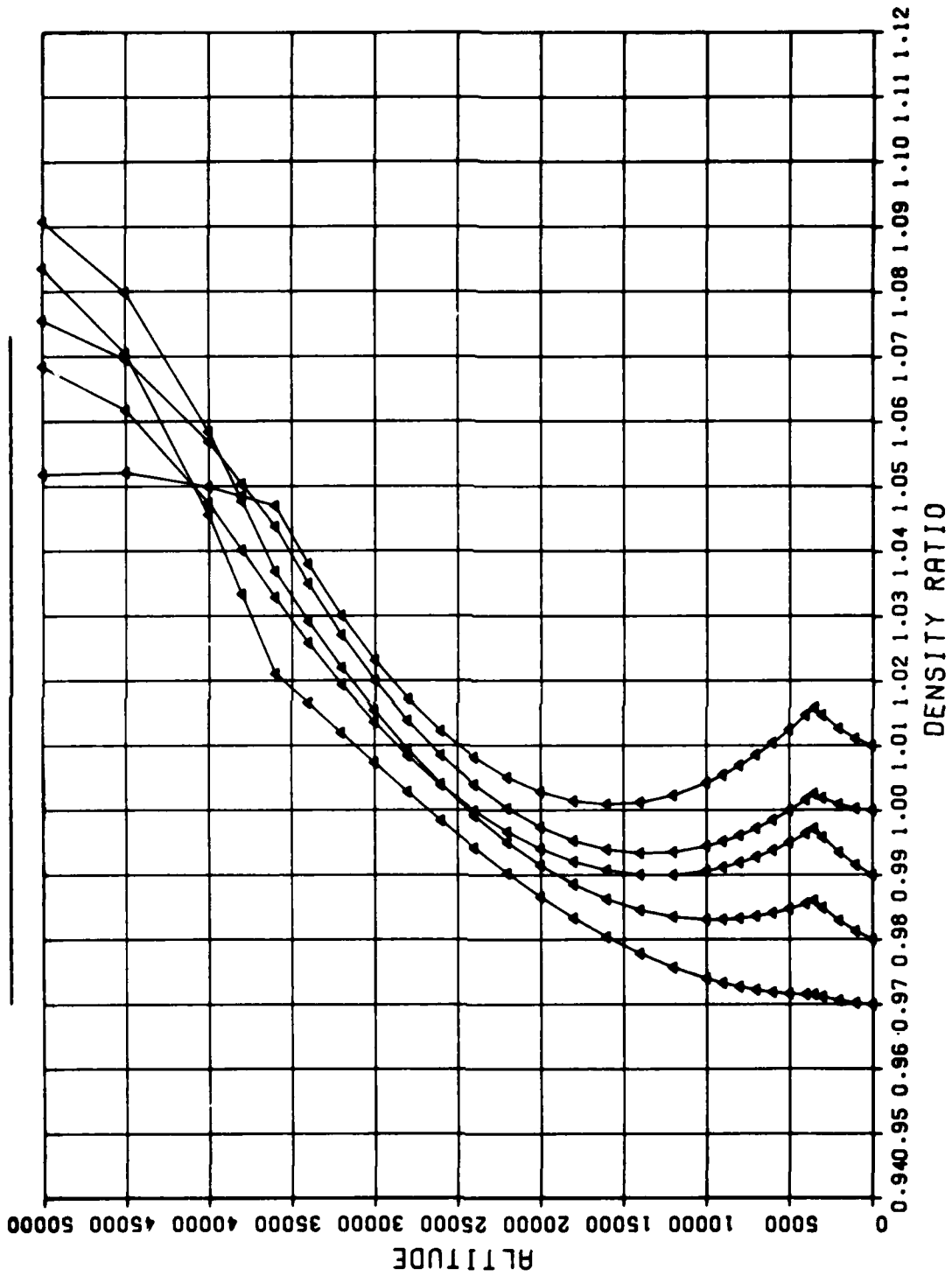
Station E is in the mid-Atlantic east of Bermuda. The uniformity and the shape of the density profiles indicate that the U.S. Standard atmosphere does not represent the atmosphere over station E too well for the period sampled. Almost all the curves above 3,500 ft are fishhook shaped. Below 3,500 ft, the density ratios increase with altitude. The lapse rate is larger than standard, which is referred to in meteorology as a "superadiabat." From 3,500 to 35,000 ft, the density ratio curves are all concave, as seen from the right. That is, density to about 15,000 ft decreases with altitude more than in the standard atmosphere. Above 15,000 ft, the density ratios increase with altitude. Density ratios are all greater than one above 30,000 ft, and they grow larger, regardless of surface density ratios. Overall, when density is two percent below standard at the surface, it averages three percent above standard at 35,000 ft. Above 35,000 ft, the curves are more erratic, which is probably due to the higher noise level in the observations.

Some seasonal differences are apparent in this region. For example, in summer, both at 2100 hr and 0900 hr local time, the density ratios increase linearly from 35,000 to 45,000 ft to a value of 11 percent above standard. This seasonal behavior may be associated with the seasonal change in the height and temperature of the tropopause.

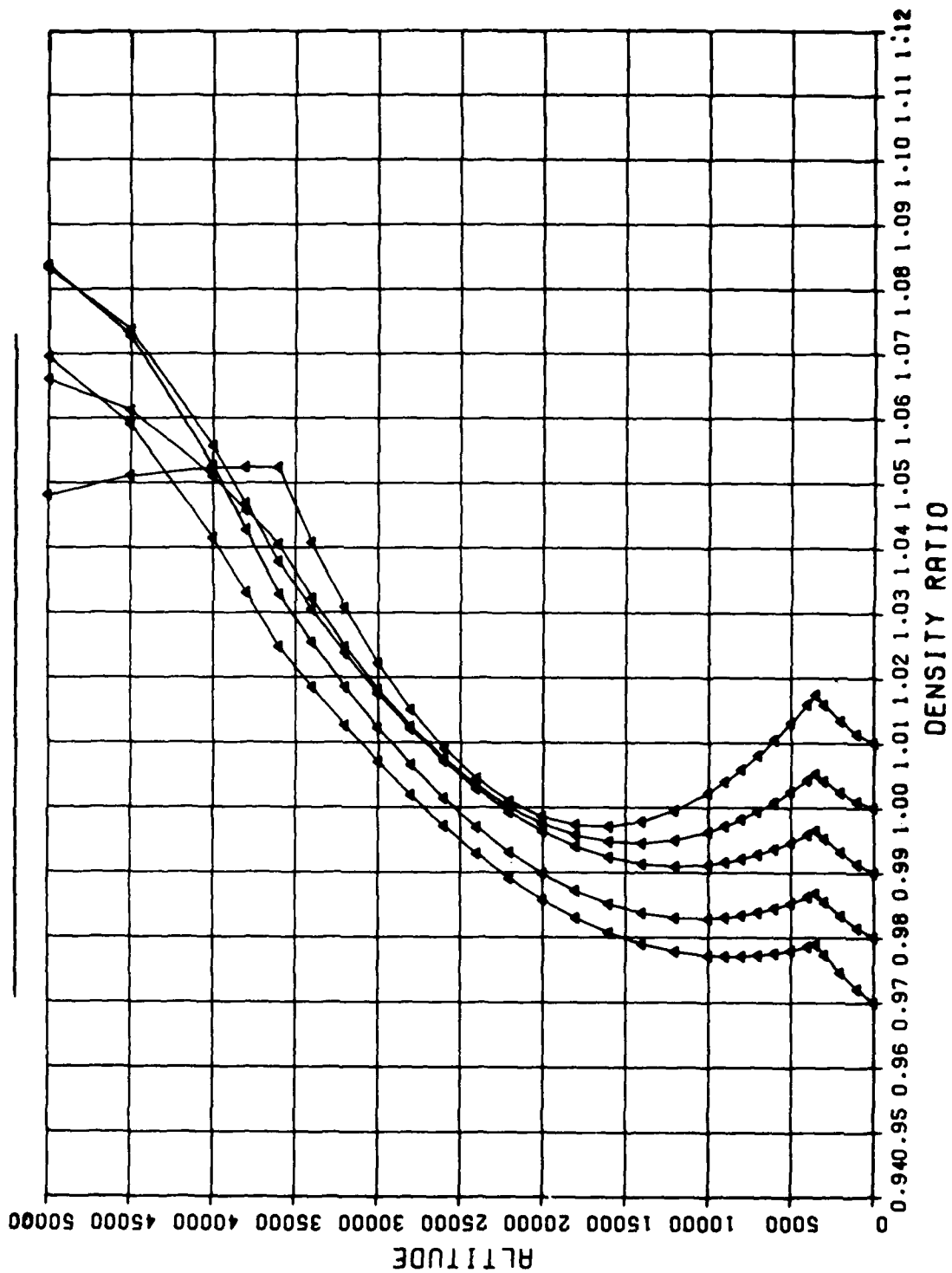
The diurnal differences are very small. When the 9 a.m. and 9 p.m. curves are superimposed, the coincidence of the curves is remarkable. This could mean that there are no diurnal changes in density; or that, as the surface temperature and density change diurnally, the density aloft changes in a corresponding manner, and the correlation is preserved. It could also be due to the fact that 9 a.m. and 9 p.m. temperatures are nearly the same. At stations N and V, the sonde times would likely correspond to greater differences in surface temperature and density.

The values for surface density reflect the seasonal changes in temperature. Surface density class medians ranged from 0.95 to 0.98 in summer; in winter, they ranged from 0.97 to 1.02.

Station E  
Spring 0000 hr G.m.t.  
(20 hr 48 min local time)

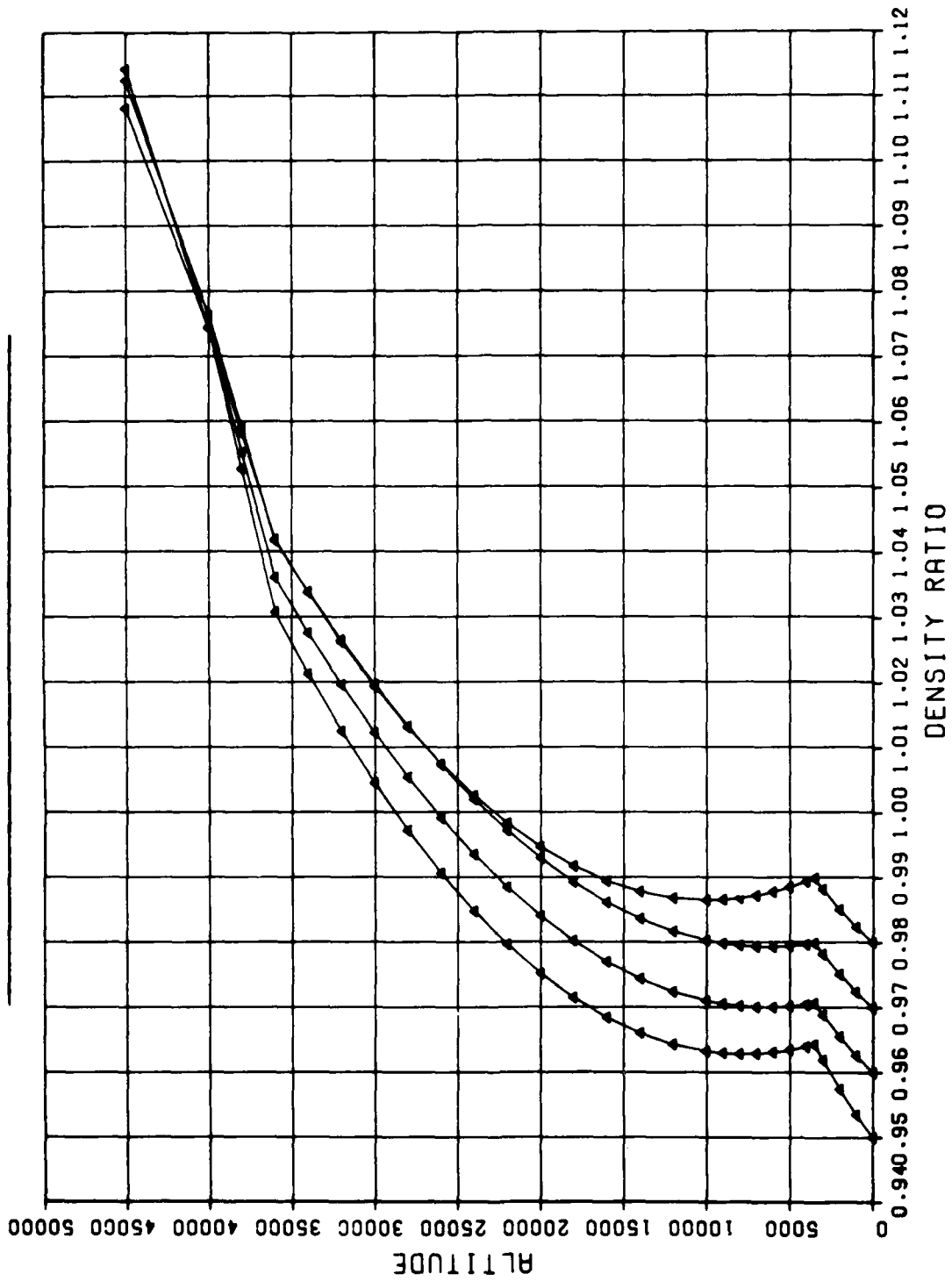


Station E  
Spring 1200 hr G.m.t.  
(8 hr 48 min local time)

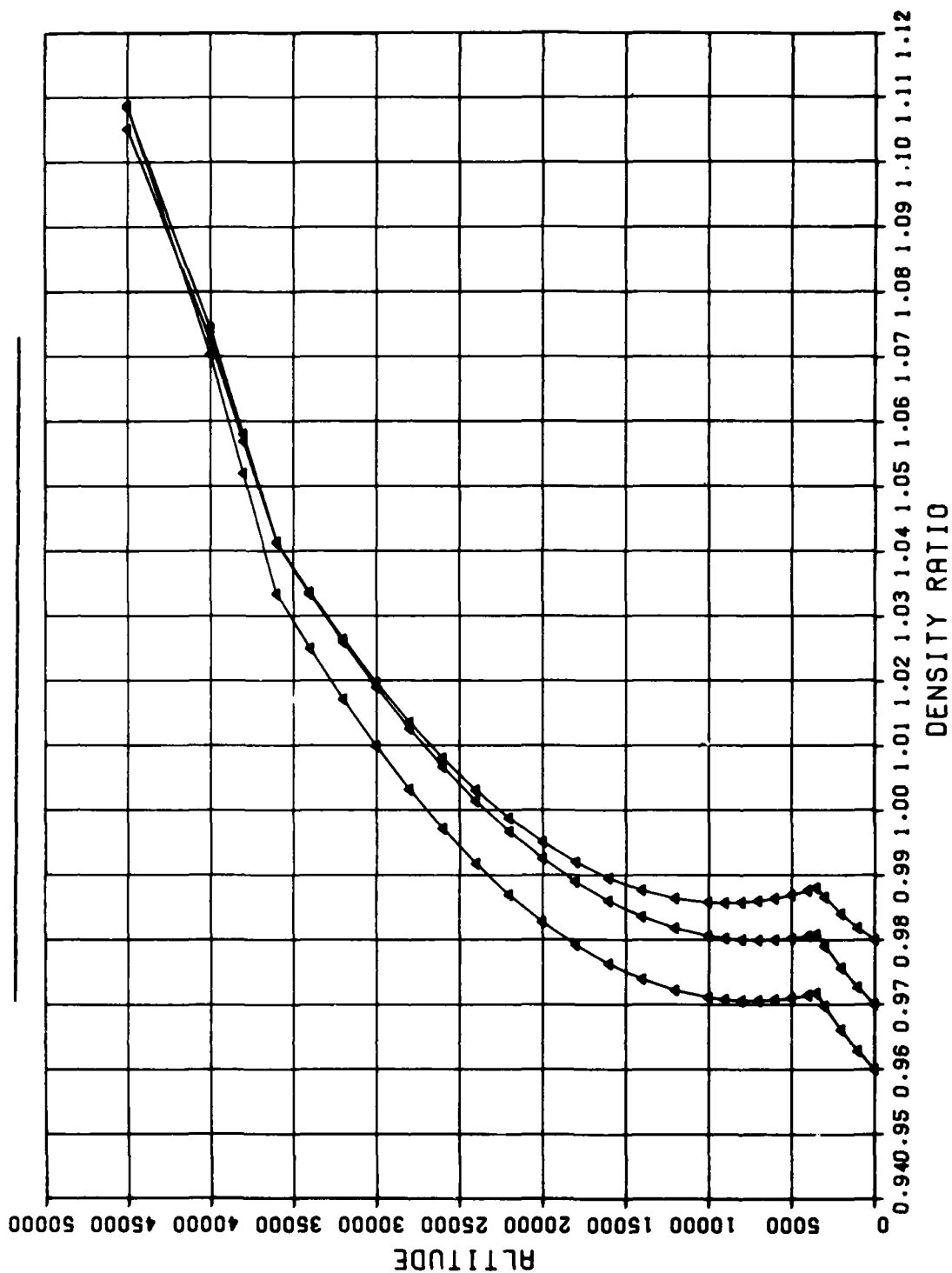




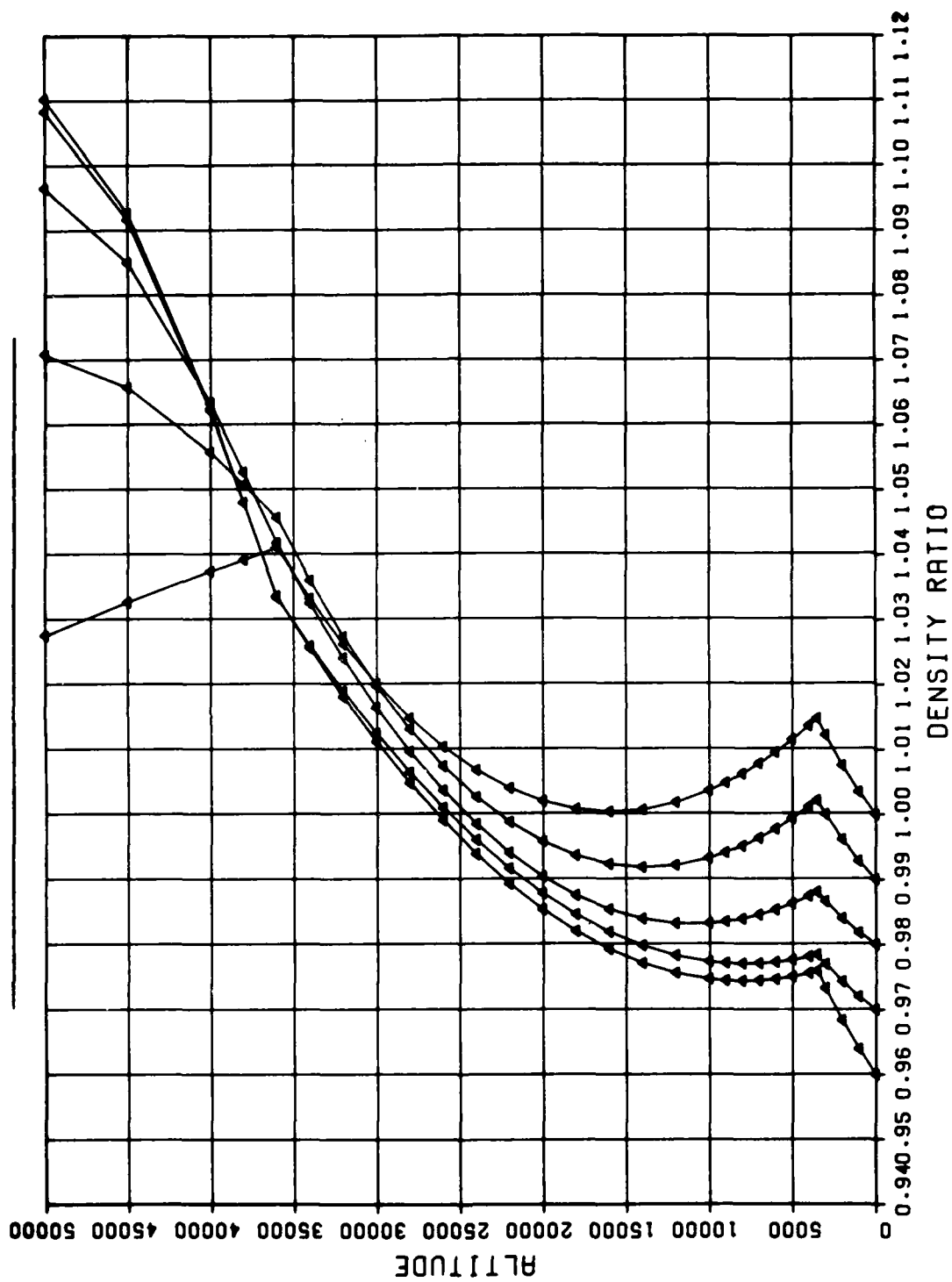
Station E  
Summer 0000 hr G.m.t.  
(20 hr 48 min local time)



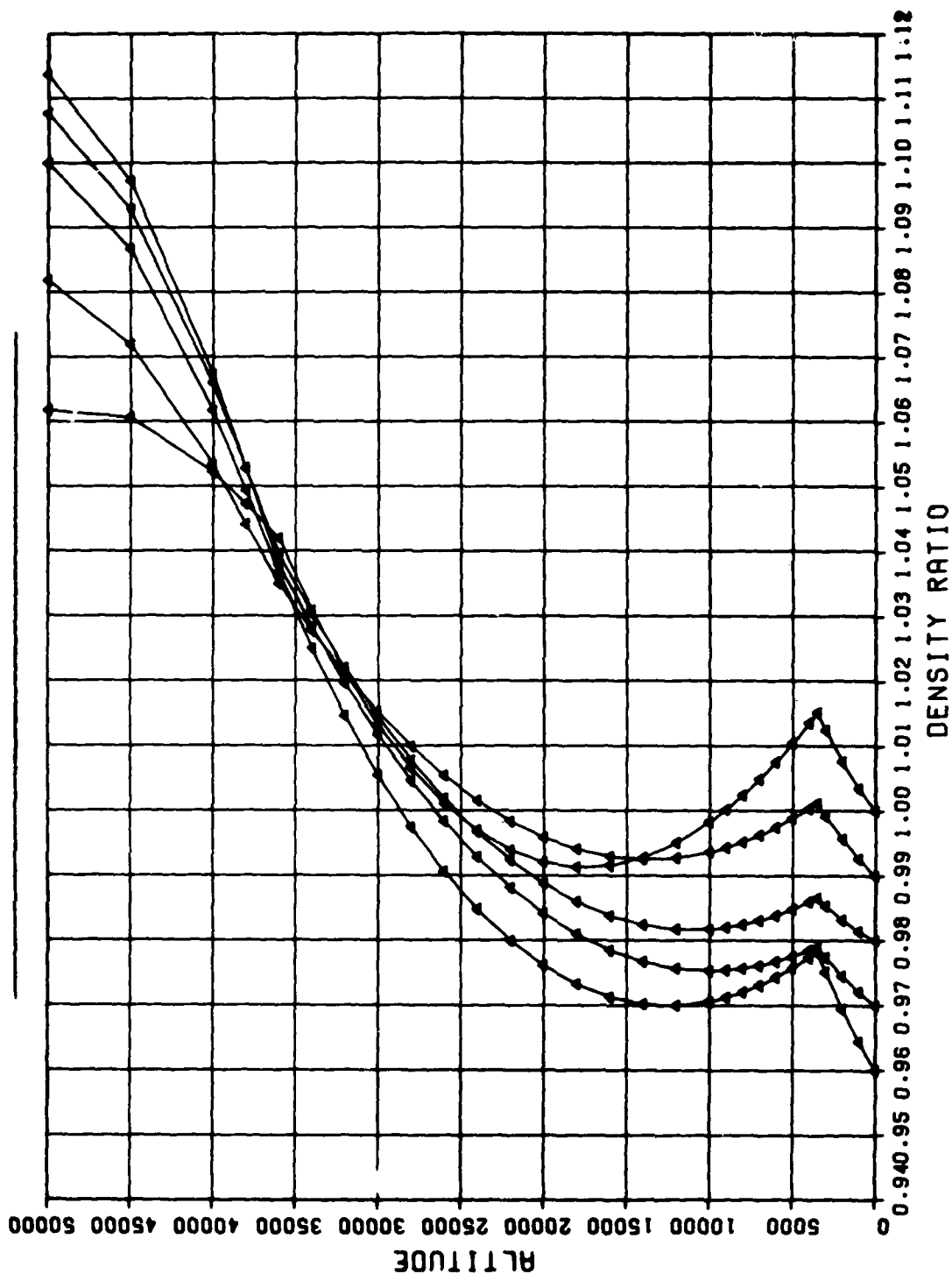
Station E  
 Summer 1200 hr G.m.t.  
 (8 hr 48 min local time)

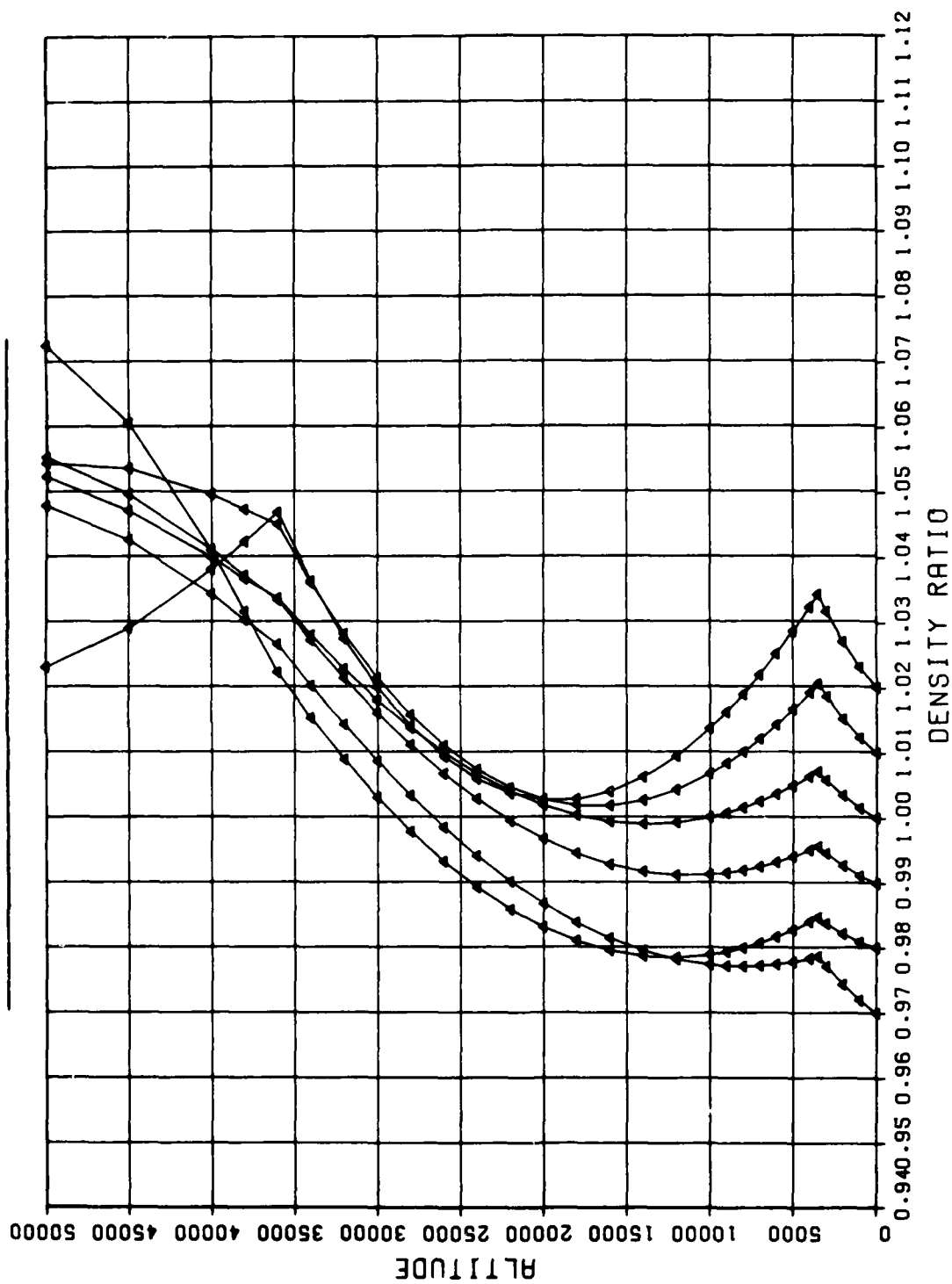


Station E  
Fall 0000 hr G.m.t.  
(20 hr 48 min local time)

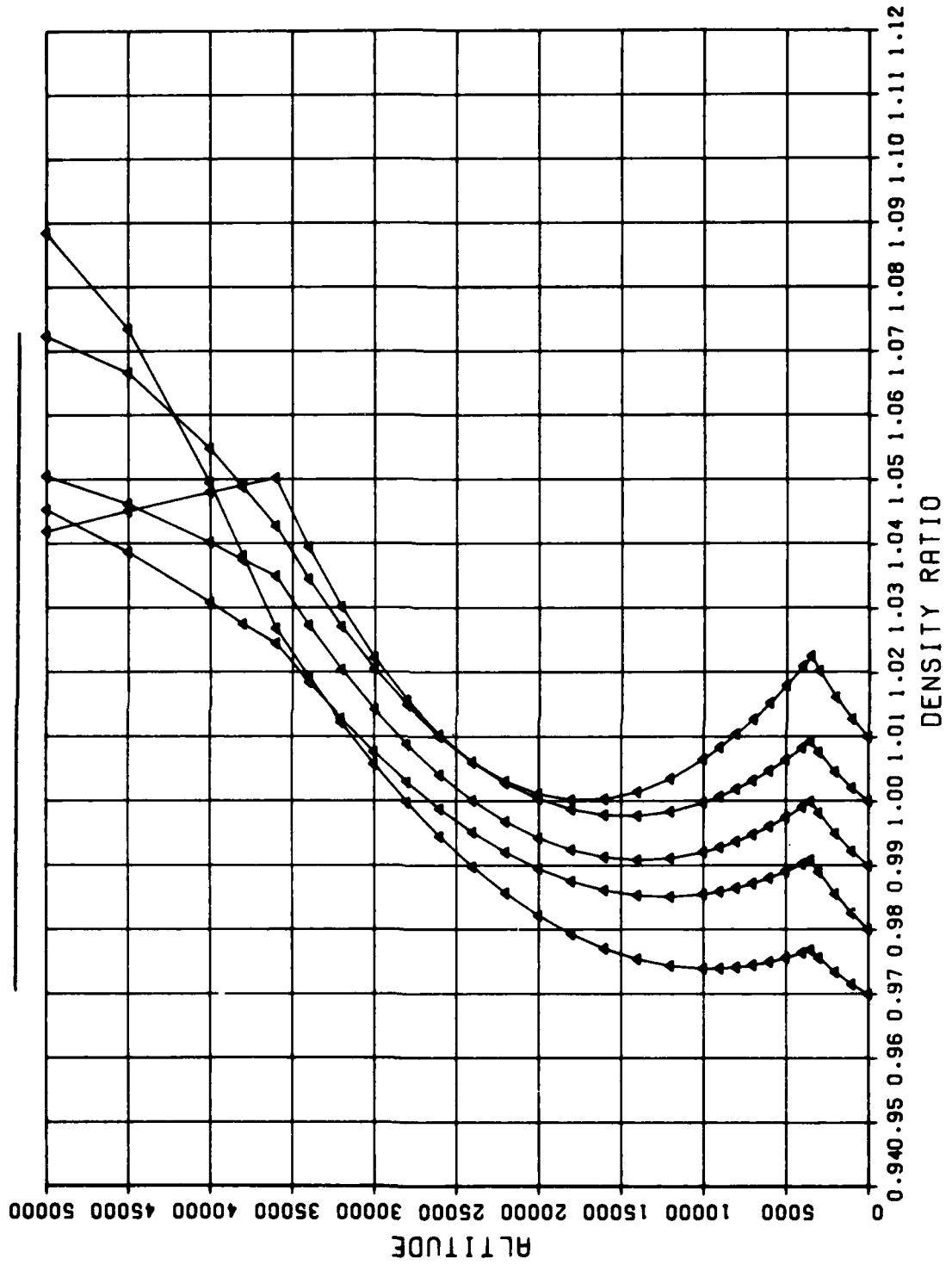


Station E  
Fall 1200 hr G.m.t.  
(8 hr 48 min local time)

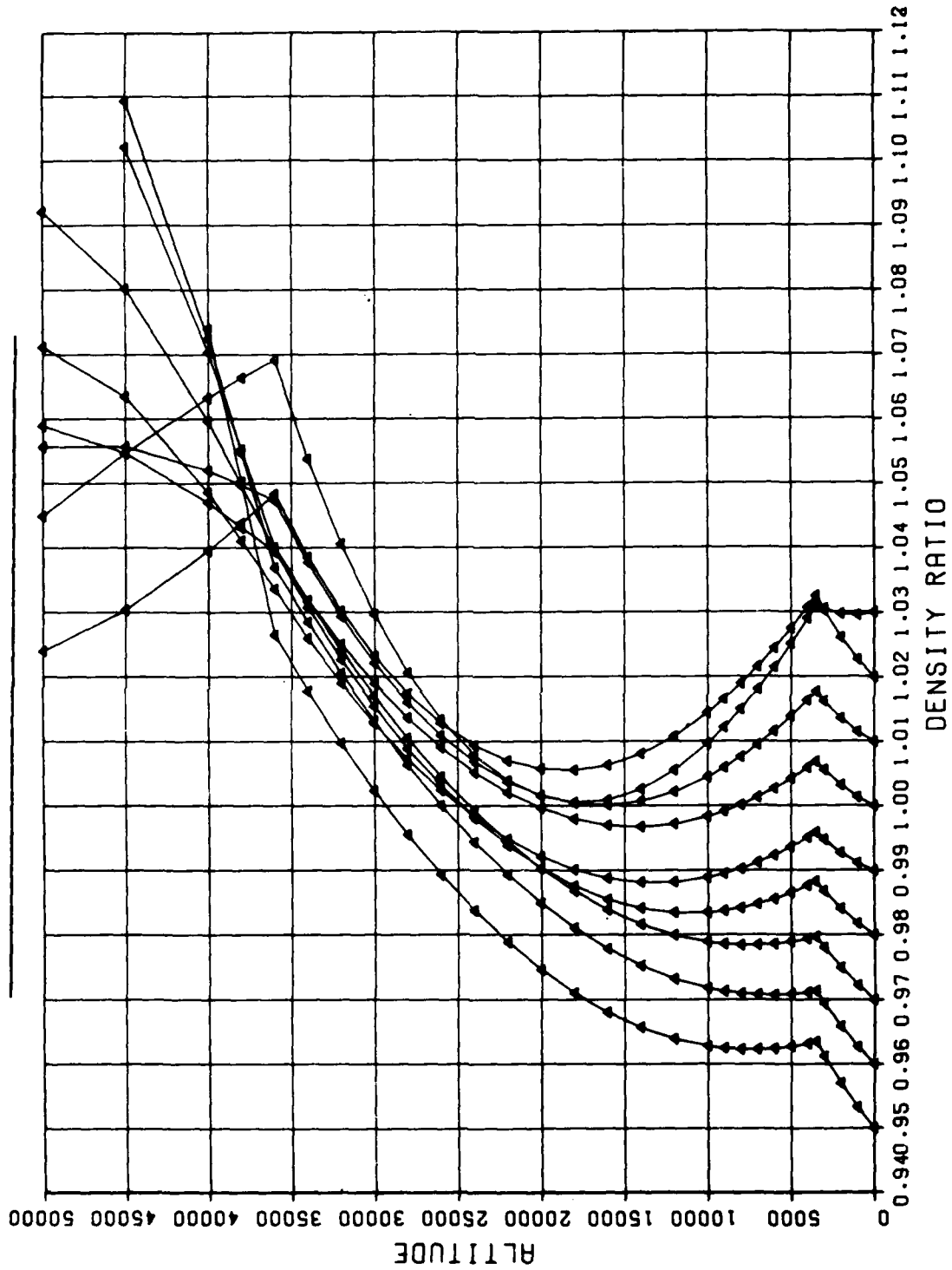




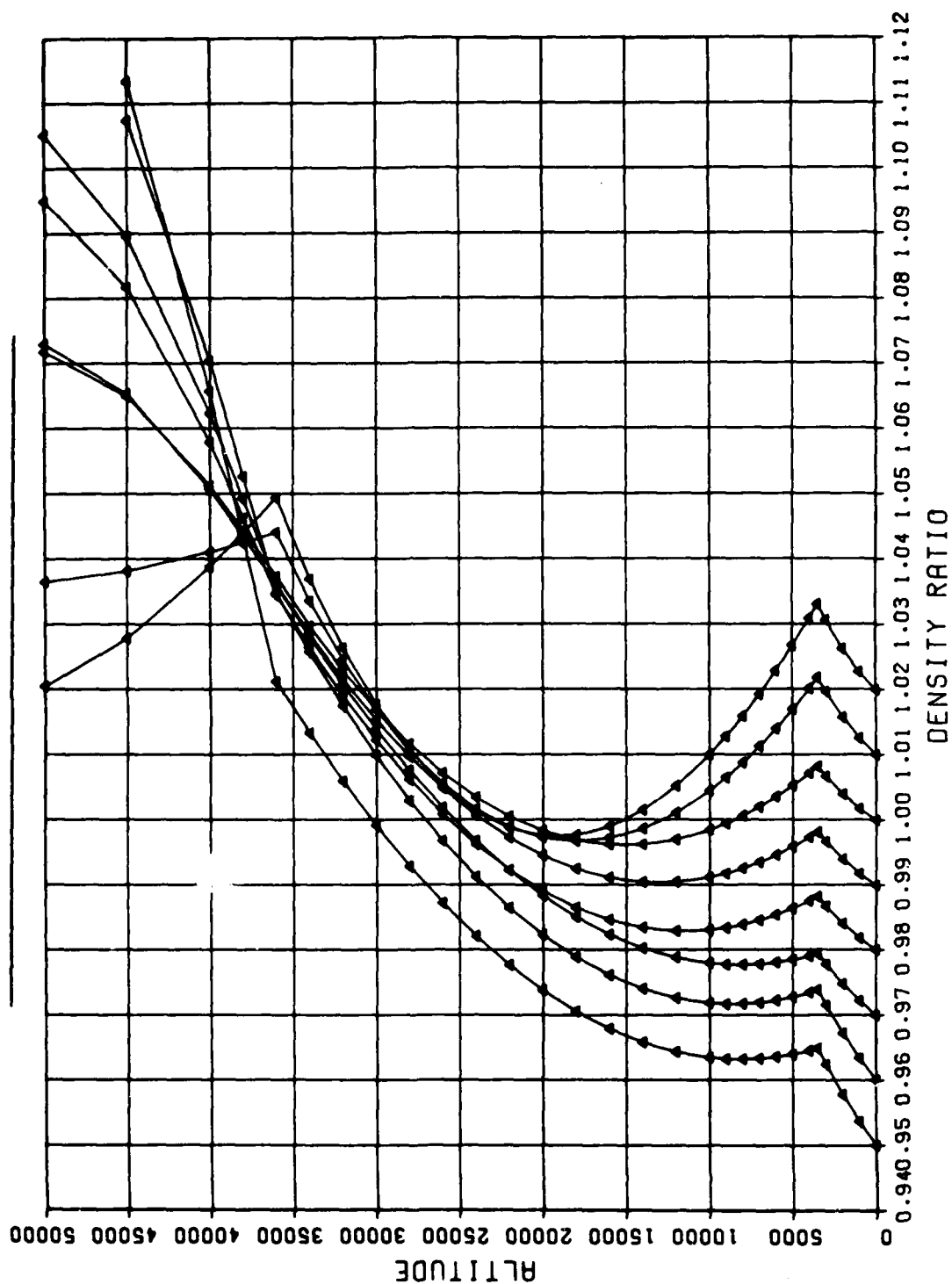
Station E  
Winter 1200 hr G.m.t.  
(8 hr 48 min local time)



Station E  
All Seasons 0000 hr G.m.t.  
(20 hr 48 min local time)



Station E  
All Seasons 1200 hr G.m.t.  
(8 hr 48 min local time)





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APPENDIX E

BALLISTIC DENSITY PROFILES FOR STATION E

AD-A119 496

NAVAL SURFACE WEAPONS CENTER DAHLGREN VA  
A METHOD TO CORRELATE THE UPPER AIR DENSITY WITH SURFACE DENSITY--ETC(U)  
JUL 82 L J MCANELLY

F/G 4/1

UNCLASSIFIED

NSWC/TR-82-81

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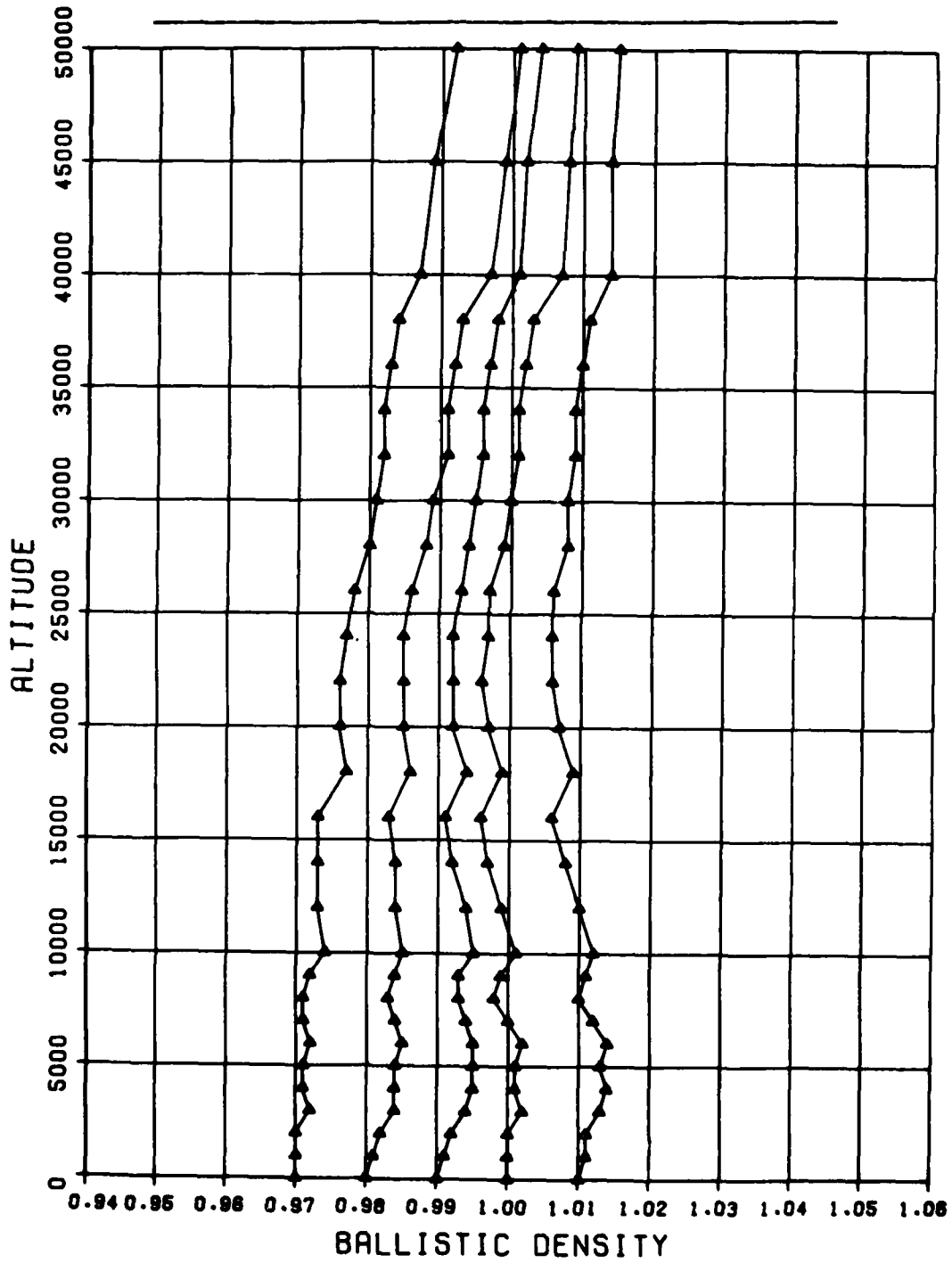
2 of 2  
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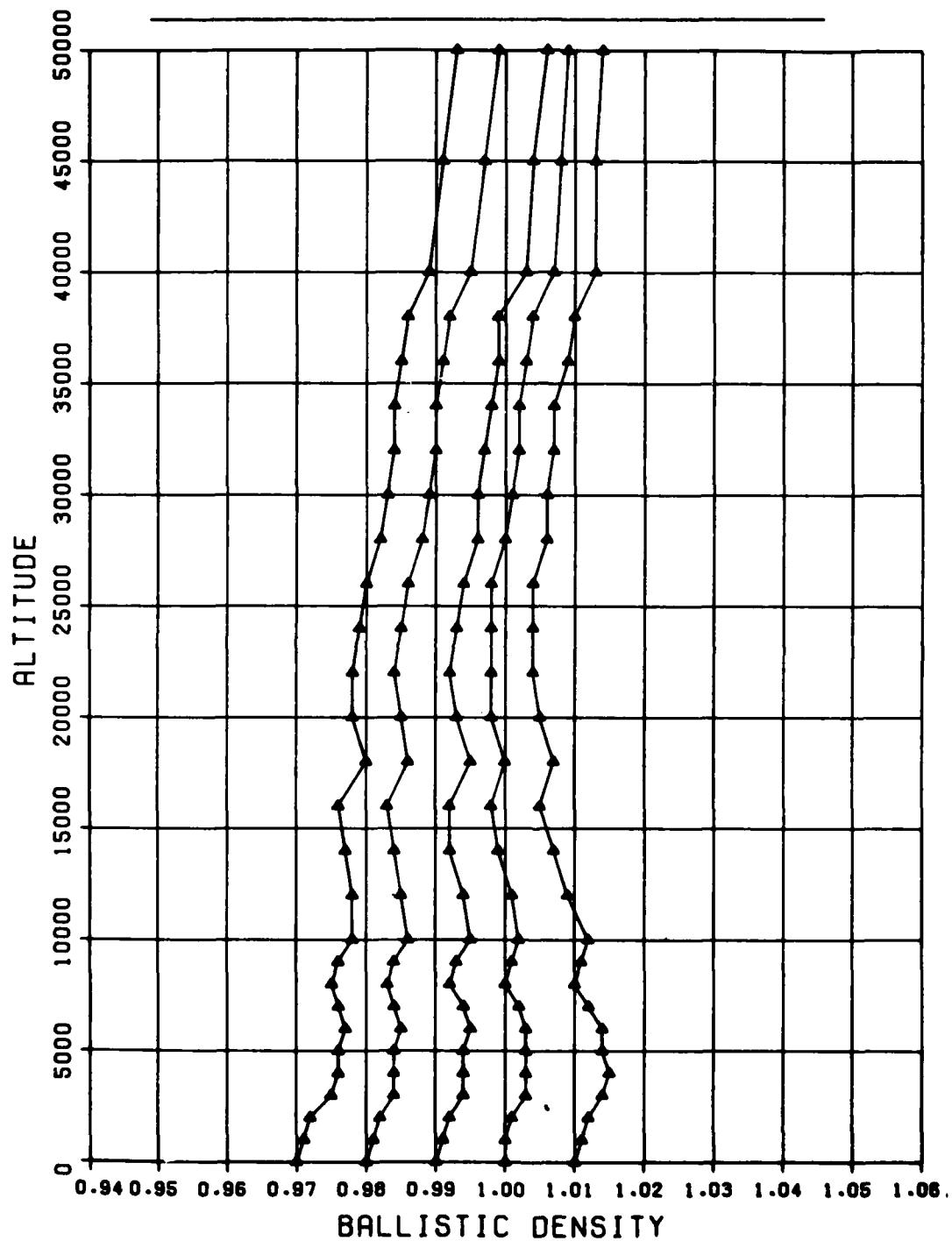
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Station E  
Spring 0000 hr G.m.t.  
(20 hr 48 min local time)



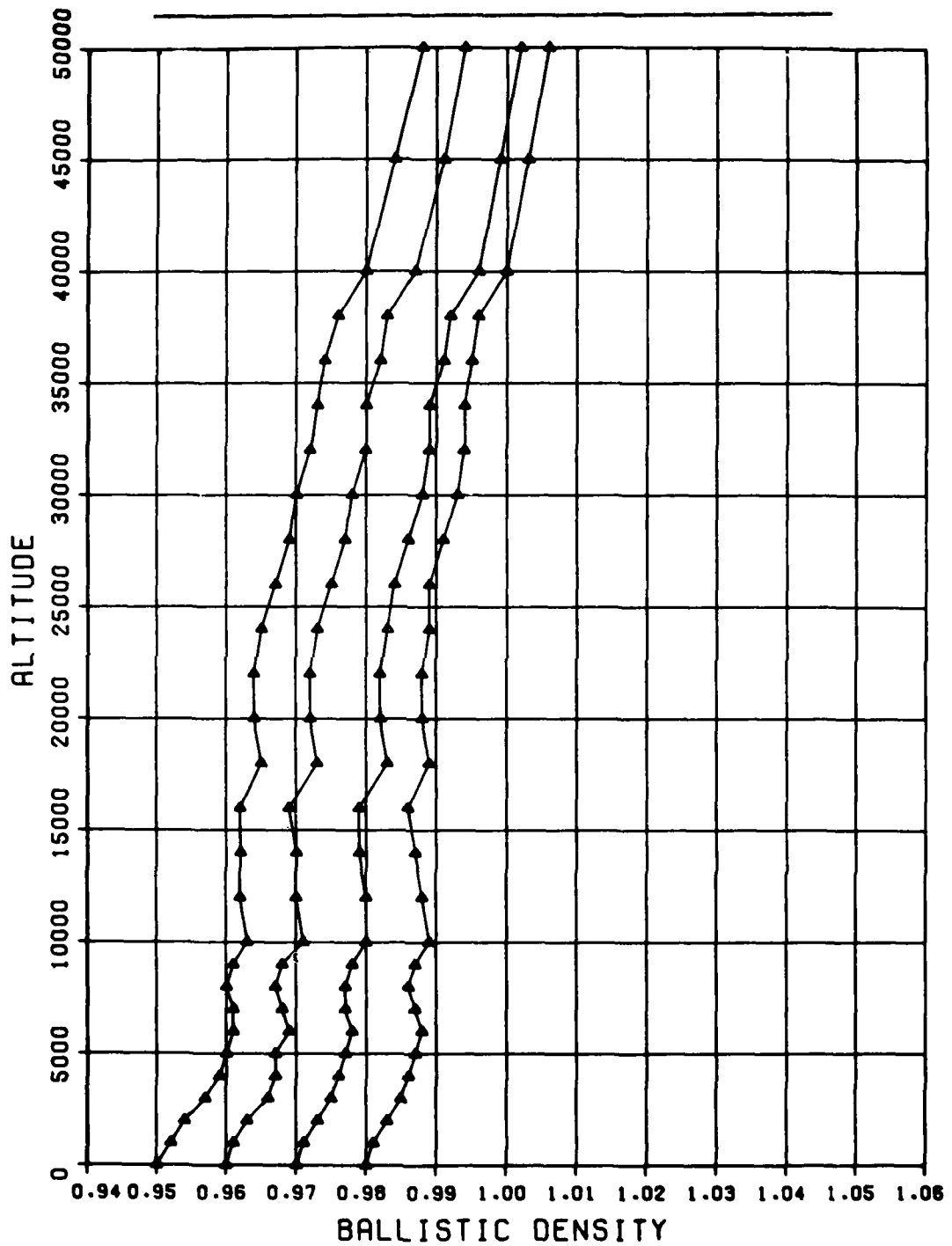
TR 82-81

Station E  
Spring 1200 hr G.m.t.  
(8 hr 48 min local time)



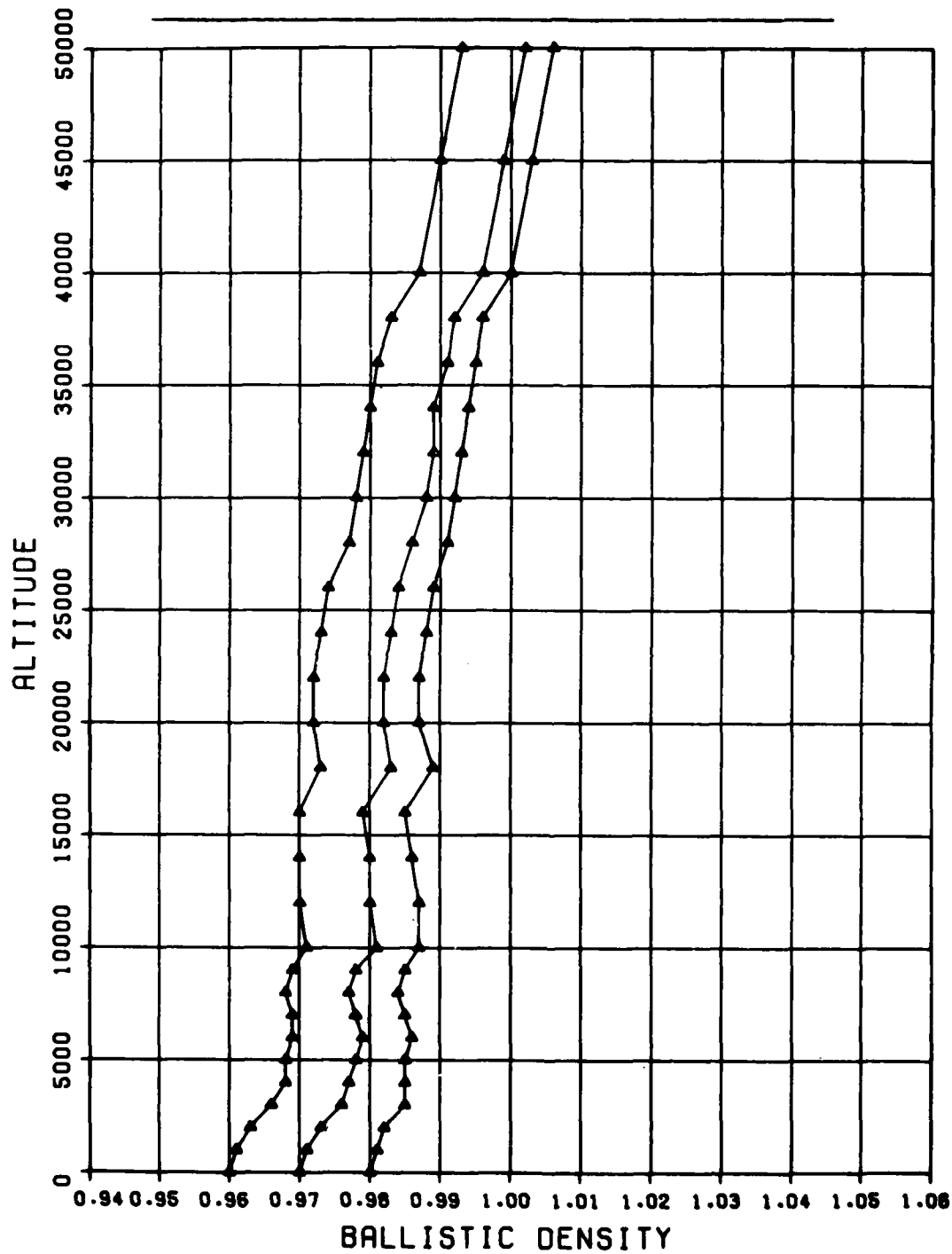
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Station E  
Summer 0000 hr G.m.t.  
(20 hr 48 min local time)



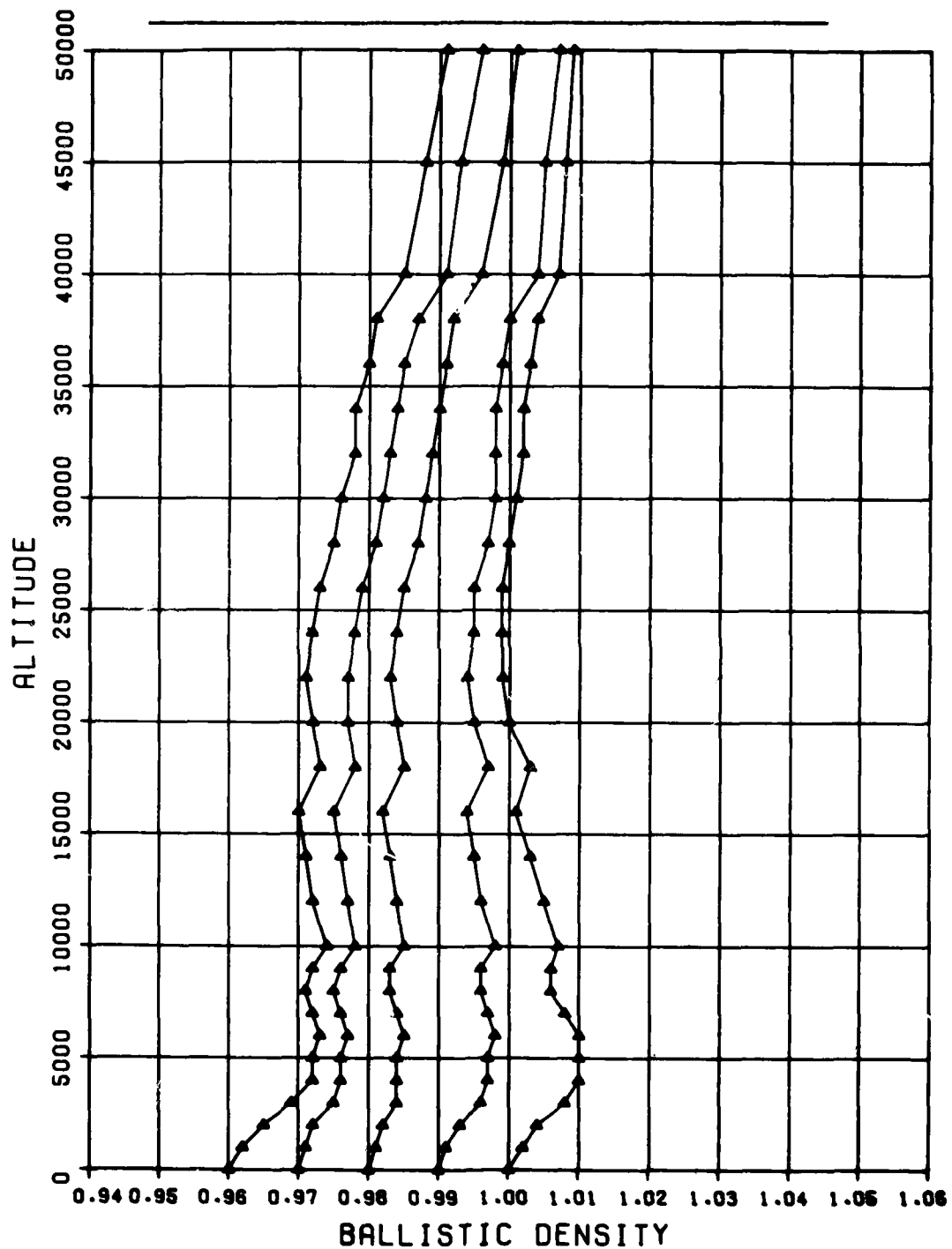
TR 82-81

Station E  
Summer 1200 hr G.m.t.  
(8 hr 48 min local time)



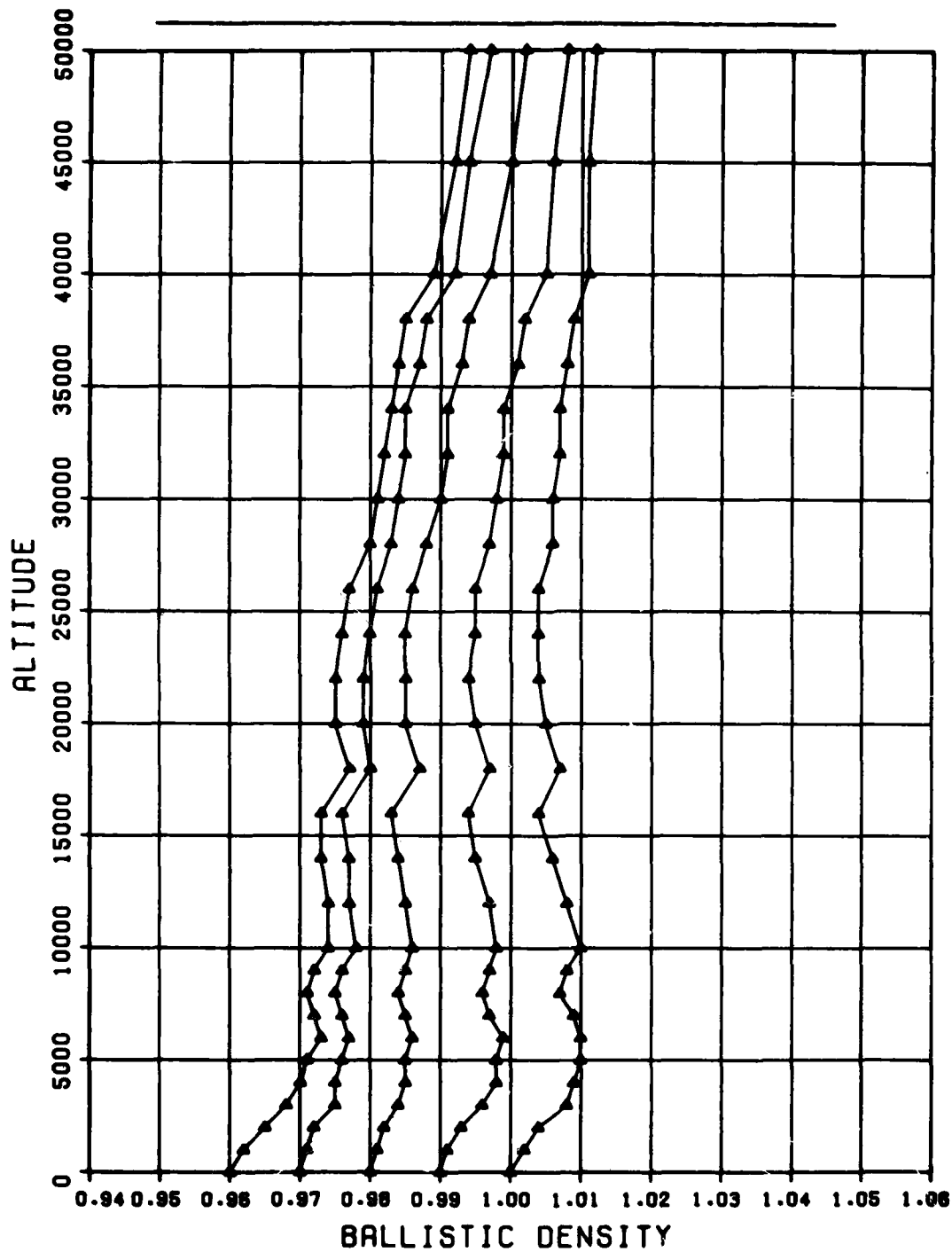
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Station E  
Fall 0000 hr G.m.t.  
(20 hr 48 min local time)



TR 82-81

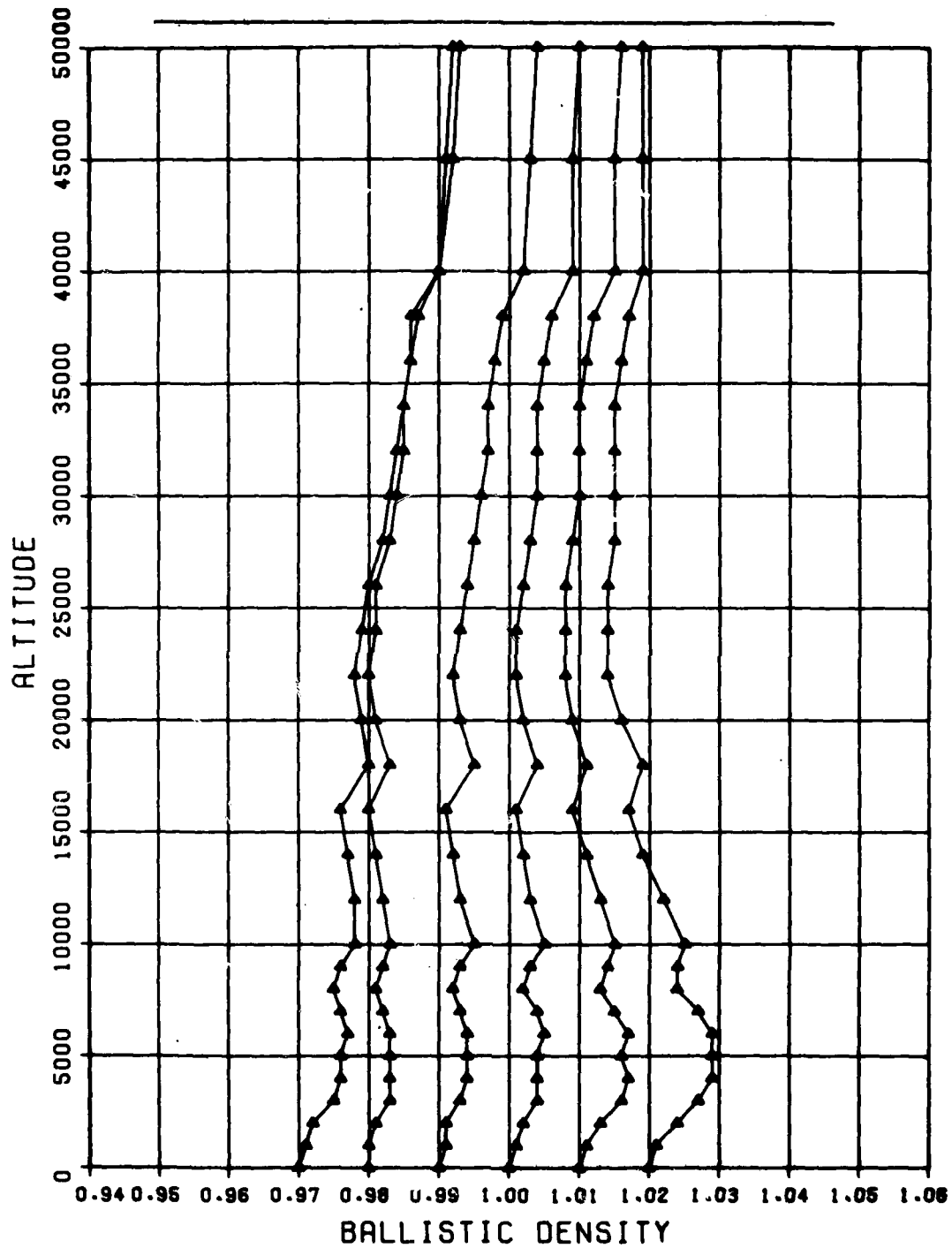
Station E  
Fall 1200 hr G.m.t.  
(8 hr 48 min local time)





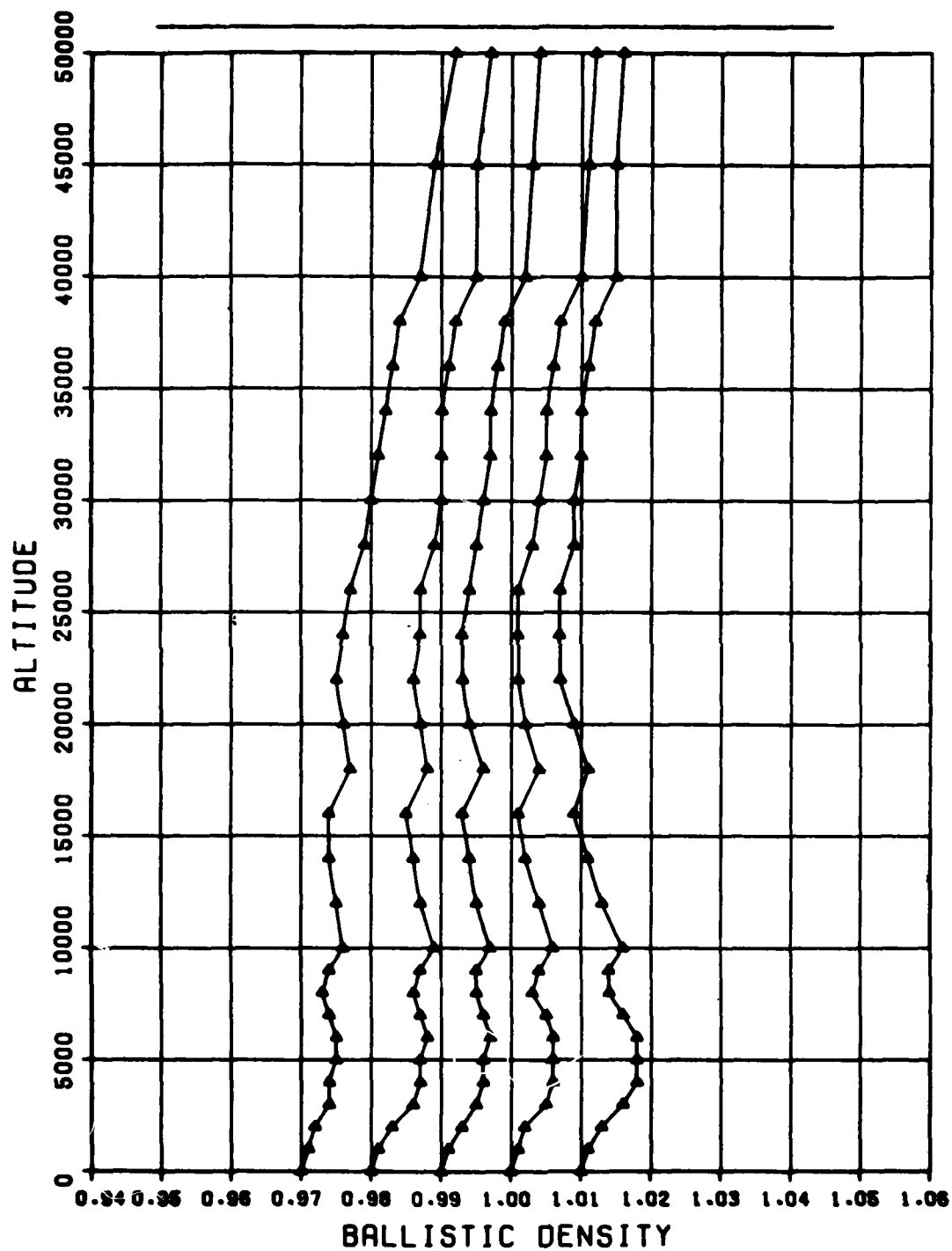
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Station E  
Winter 0000 hr G.m.t.  
(20 hr 48 min local time)



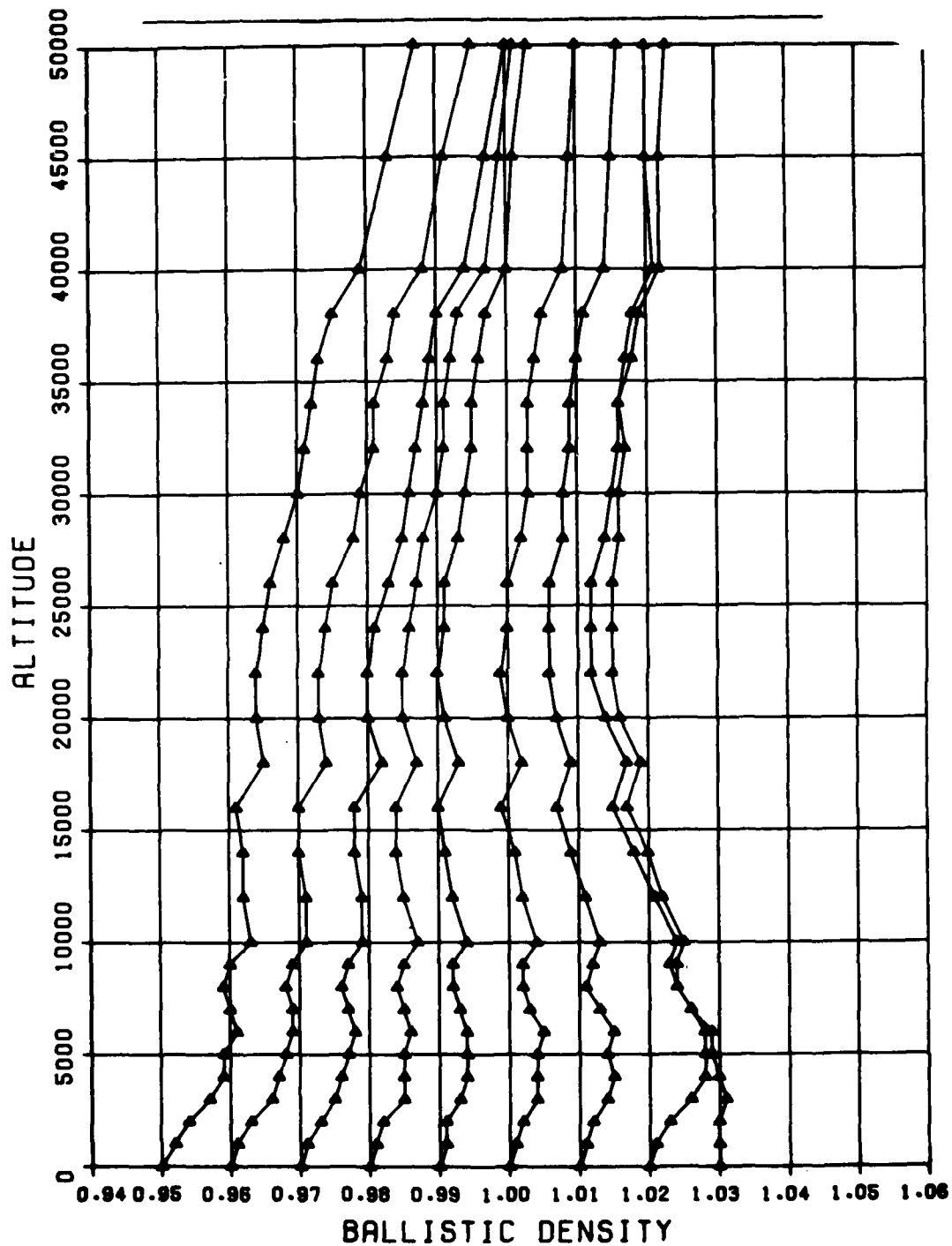
TR 82-81

Station E  
Winter 1200 hr G.m.t.  
(8 hr 48 min local time)



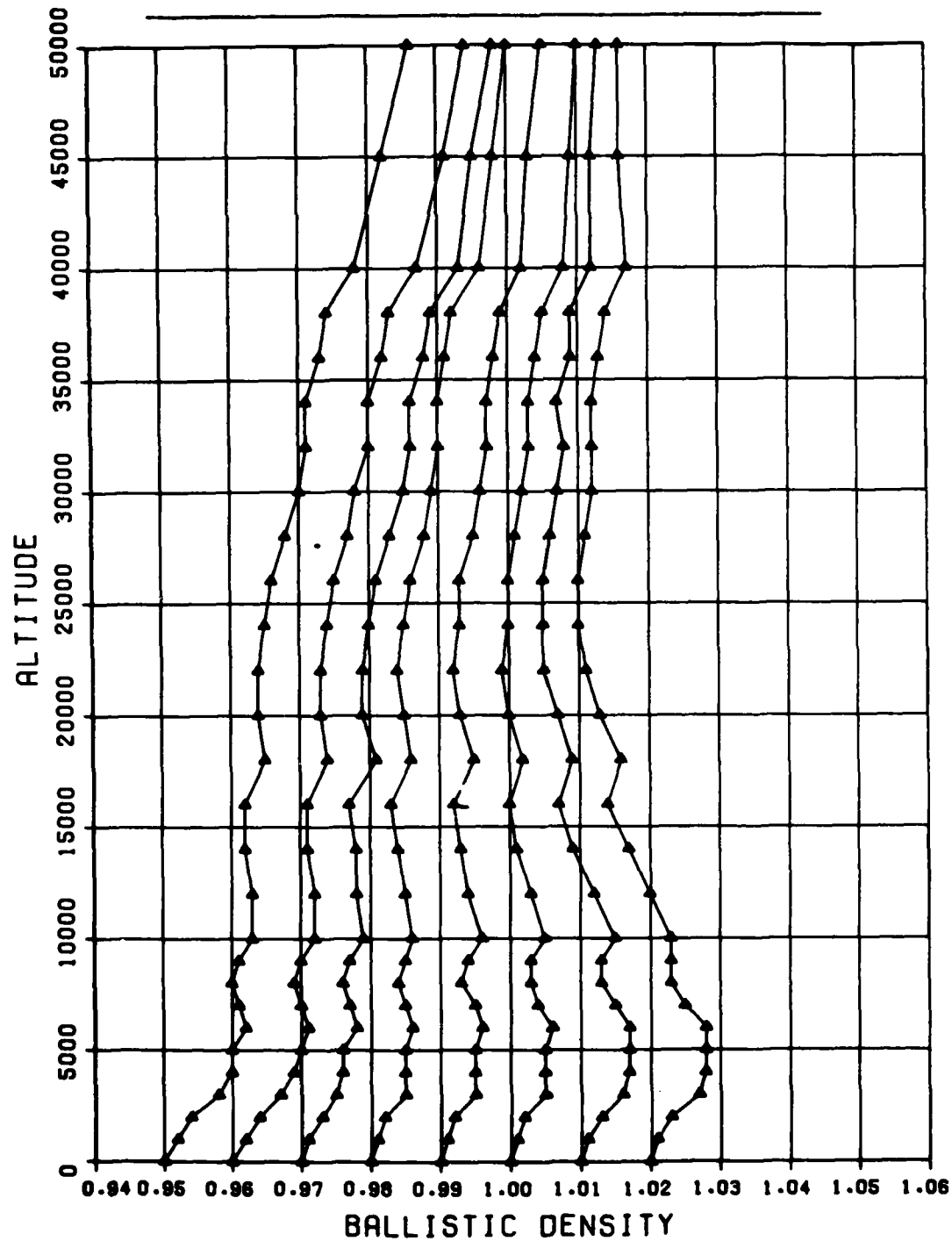
TR 82-81

Station E  
All Seasons 0000 hr G.m.t.  
(20 hr 48 min local time)



TR 82-81

Station E  
All Seasons 1200 hr G.m.t.  
(8 hr 48 min local time)



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APPENDIX F

SELECTED BALLISTIC DENSITIES FOR STATIONS E, N, AND C

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Local time corresponding to:

<u>Station</u>	<u>0000 hr G.m.t.</u>	<u>1200 hr G.m.t.</u>
E	20 hr 48 min	08 hr 48 min
V	10 hr 54 min	22 hr 54 min
C	21 hr 38 min	09 hr 38 min
D	21 hr 16 min	09 hr 16 min
N	14 hr 40 min	02 hr 20 min

(To be used with the following tables.)

# BALLISTIC DENSITY

Altitude = 30,000 ft

Station	Surface Density	0000 hr G.m.t.					1200 hr G.m.t.				
		W	S	SU	F	A	W	S	SU	F	A
E	0.95	-	-	0.970	-	0.970	-	-	-	-	0.970
V		-	-	0.968	0.971	0.968	-	-	0.966	-	0.967
C		-	-	-	-	-	-	-	-	-	-
D		-	-	-	-	-	-	-	-	-	-
N		-	-	-	-	-	-	-	-	-	-
<hr/>											
E	0.96	-	-	0.978	0.981	0.979	-	-	0.978	0.976	0.978
V		-	-	0.975	0.973	0.975	-	-	0.974	0.972	0.974
C		-	-	-	-	-	-	-	-	-	-
D		-	-	-	-	0.967	-	-	0.969	-	0.968
N		-	-	0.981	-	0.979	-	-	-	-	-
<hr/>											
E	0.97	0.983	0.981	0.988	0.984	0.986	0.980	0.983	0.988	0.982	0.985
V		0.971	0.972	0.976	0.978	0.975	-	0.973	0.976	0.977	0.977
C		-	-	-	-	-	-	-	-	-	-
D		-	-	0.978	0.980	0.977	-	-	0.979	0.976	0.978
N		0.982	0.980	0.982	0.983	0.982	0.984	-	0.981	0.983	0.981
<hr/>											
E	0.98	0.984	0.989	0.993	0.990	0.990	0.990	0.989	0.992	0.988	0.989
V		0.984	0.980	0.979	0.986	0.980	0.984	0.980	0.982	0.986	0.981
C		0.971	-	-	0.973	0.972	0.968	-	-	0.972	0.970
D		0.983	-	0.987	0.984	0.985	0.981	0.982	0.985	0.984	0.984
N		0.985	0.986	0.984	0.988	0.985	0.988	0.986	0.986	0.988	0.987

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## BALLISTIC DENSITY

Altitude = 30,000 ft

Station	Surface Density	0000 hr G.m.t.					1200 hr G.m.t.				
		W	S	SU	F	A	W	S	SU	F	A
E	0.99	0.996	0.995	0.987	0.998	0.994	0.996	0.996	-	0.998	0.996
V		0.991	0.986	0.984	0.995	0.991	0.992	0.987	-	0.993	0.989
C		0.977	0.978	0.979	0.980	0.978	0.980	-	0.978	0.980	0.980
D		0.988	0.989	0.992	0.991	0.992	0.990	0.991	0.991	0.990	0.991
N		0.994	0.990	0.989	0.994	0.993	0.993	0.989	0.990	0.996	0.992
E	1.00	1.004	1.000	-	1.006	1.003	1.004	1.001	-	1.001	1.002
V		0.999	0.995	-	1.001	0.998	0.998	0.993	-	1.003	0.995
C		0.986	0.987	0.987	0.987	0.986	0.985	0.983	0.985	0.986	0.984
D		0.996	0.995	0.995	0.998	0.997	0.997	0.995	0.995	0.996	0.994
N		1.003	0.998	-	1.000	1.000	1.001	0.999	-	1.002	1.000
E	1.01	1.010	1.008	-	-	1.008	1.009	1.006	-	-	1.007
V		1.006	1.001	-	-	1.005	1.004	0.999	-	-	1.003
C		0.993	0.992	0.991	0.994	0.993	0.992	0.989	0.990	0.994	0.992
D		1.002	1.002	-	1.000	1.002	1.002	1.000	-	1.002	1.002
N		1.009	-	-	-	1.010	1.011	1.007	-	-	1.009
E	1.02	1.015	-	-	-	1.016	-	-	-	-	1.012
V		1.011	1.009	-	-	1.008	1.008	1.007	-	-	1.009
C		1.002	0.996	0.997	1.001	0.998	1.001	0.999	0.999	1.002	0.999
D		1.009	1.005	-	1.010	1.008	1.008	1.004	-	1.008	1.009
N		-	-	-	-	-	-	-	-	-	-



# BALLISTIC DENSITY

Altitude = 30,000 ft

Station	Surface Density	0000 hr G.m.t.					1200 hr G.m.t.				
		W	S	SU	F	A	W	S	SU	F	A
E	1.03	-	-	-	-	-	-	-	-	-	1.015
V		-	-	-	-	-	-	-	-	-	-
C		1.008	1.006	0.999	1.010	1.006	1.008	1.006	0.998	1.007	1.005
D		1.103	1.011	-	1.012	1.013	1.013	1.010	-	1.013	1.013
N		-	-	-	-	-	-	-	-	-	-
E	1.04	-	-	-	-	-	-	-	-	-	-
V		-	-	-	-	-	-	-	-	-	-
C		1.105	1.013	-	1.014	1.012	1.015	1.013	-	1.015	1.012
D		1.020	-	-	-	1.019	1.022	-	-	-	1.021
N		-	-	-	-	-	-	-	-	-	-
E	1.05	-	-	-	-	-	-	-	-	-	-
V		-	-	-	-	-	-	-	-	-	-
C		1.024	1.018	-	-	1.021	1.019	1.019	-	-	1.018
D		1.028	-	-	-	1.027	1.027	-	-	-	1.026
N		-	-	-	-	-	-	-	-	-	-
E	1.06	-	-	-	-	-	-	-	-	-	-
V		-	-	-	-	-	-	-	-	-	-
C		-	-	-	-	-	1.029	-	-	-	1.028
D		-	-	-	-	-	-	-	-	-	-
N		-	-	-	-	-	-	-	-	-	-

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# BALLISTIC DENSITY

Altitude = 50,000 ft

Station	Surface Density	0000 hr G.m.t.					1200 hr G.m.t.				
		W	S	SU	F	A	W	S	SU	F	A
E	0.95	-	-	0.988	-	0.987	-	-	-	-	0.986
V		-	-	0.986	0.984	0.984	-	-	0.984	-	0.982
C		-	-	-	-	-	-	-	-	-	-
D		-	-	-	-	-	-	-	-	-	-
N		-	-	-	-	-	-	-	-	-	-
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E	0.96	-	-	0.994	0.994	0.995	-	-	0.993	0.991	0.994
V		-	-	0.992	0.998	0.992	-	-	0.991	0.998	0.991
C		-	-	-	-	-	-	-	-	-	-
D		-	-	-	-	0.980	-	-	0.981	-	0.979
N		-	-	0.995	-	0.991	-	-	-	-	-
<hr/>											
E	0.97	0.992	0.992	1.002	0.997	1.000	0.992	0.993	1.002	0.996	0.998
V		0.980	0.988	0.993	0.993	0.991	-	0.990	0.993	0.993	0.994
C		-	-	-	-	-	-	-	-	-	-
D		-	-	0.991	0.985	0.987	-	-	0.991	0.983	0.989
N		0.991	0.995	0.998	0.995	0.996	0.991	-	0.997	0.996	0.996
<hr/>											
E	0.98	0.993	1.001	1.006	1.002	1.001	0.997	0.999	1.006	1.001	1.000
V		0.988	0.994	0.995	0.998	0.993	0.989	0.994	0.997	0.998	0.994
C		0.963	-	-	0.969	0.966	0.951	-	-	0.968	0.963
D		0.986	-	0.999	0.991	0.996	0.982	0.987	0.997	0.991	0.992
N		0.996	1.000	1.000	1.002	1.000	0.999	1.001	1.001	1.001	1.001

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BALLISTIC DENSITY

Altitude = 50,000 ft

Station	Surface Density	0000 hr G.m.t.					1200 hr G.m.t.				
		W	S	SU	F	A	W	S	SU	F	A
E	0.99	1.004	1.004	1.003	1.008	1.003	1.004	1.006	-	1.007	1.005
V		0.996	0.999	1.000	1.004	1.000	0.995	1.000	-	1.003	0.998
C		0.966	0.971	0.980	0.975	0.976	0.965	-	0.980	0.977	0.978
D		0.990	0.995	1.002	0.999	1.001	0.990	0.996	1.004	0.999	1.000
N		1.004	1.004	1.005	1.008	1.007	1.003	1.004	1.005	1.008	1.005
<hr/>											
E	1.00	1.010	1.009	-	1.012	1.010	1.012	1.009	-	1.009	1.010
V		1.000	1.004	-	1.006	1.002	0.998	1.004	-	1.008	1.002
C		0.982	0.984	0.990	0.986	0.988	0.976	0.979	0.989	0.986	0.987
D		0.997	1.003	1.007	1.005	1.005	1.000	1.002	1.006	1.003	1.002
N		1.011	1.010	-	1.012	1.010	1.012	1.010	-	1.013	1.011
<hr/>											
E	1.01	1.016	1.015	-	-	1.016	1.016	1.014	-	-	1.013
V		1.006	1.008	-	-	1.007	1.003	1.009	-	-	1.005
C		0.988	0.991	0.995	0.993	0.993	0.988	0.989	0.996	0.994	0.996
D		1.005	1.006	-	1.004	1.007	1.003	1.006	-	1.006	1.007
N		1.016	-	-	-	1.017	1.017	1.017	-	-	1.017
<hr/>											
E	1.02	1.019	-	-	-	1.020	-	-	-	-	1.016
V		1.009	1.014	-	-	1.011	1.008	1.013	-	-	1.009
C		0.995	0.998	1.002	1.000	0.999	0.997	0.998	1.003	1.001	1.001
D		1.006	1.010	-	1.010	1.009	1.004	1.009	-	1.012	1.008
N		-	-	-	-	-	-	-	-	-	-

# BALLISTIC DENSITY

Altitude = 50,000 ft

Station	Surface Density	0000 hr G.m.t.					1200 hr G.m.t.				
		W	S	SU	F	A	W	S	SU	F	A
E	1.03	-	-	-	-	-	-	-	-	-	1.023
V		-	-	-	-	-	-	-	-	-	-
C		1.000	1.007	1.005	1.008	1.007	1.003	1.006	1.004	1.008	1.004
D		1.010	1.015	-	1.016	1.011	1.009	1.015	-	1.014	1.011
N		-	-	-	-	-	-	-	-	-	-
E	1.04	-	-	-	-	-	-	-	-	-	-
V		-	-	-	-	-	-	-	-	-	-
C		1.008	1.008	-	1.015	1.009	1.009	1.011	-	1.013	1.009
D		1.015	-	-	-	1.015	1.015	-	-	-	1.016
N		-	-	-	-	-	-	-	-	-	-
E	1.05	-	-	-	-	-	-	-	-	-	-
V		-	-	-	-	-	-	-	-	-	-
C		1.019	1.015	-	-	1.018	1.016	1.016	-	-	1.017
D		1.023	-	-	-	1.023	1.024	-	-	-	1.023
N		-	-	-	-	-	-	-	-	-	-
E	1.06	-	-	-	-	-	-	-	-	-	-
V		-	-	-	-	-	-	-	-	-	-
C		-	-	-	-	-	1.022	-	-	-	1.022
D		-	-	-	-	-	-	-	-	-	-
N		-	-	-	-	-	-	-	-	-	-

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